

# Angle Resolved Photoemission Spectroscopy

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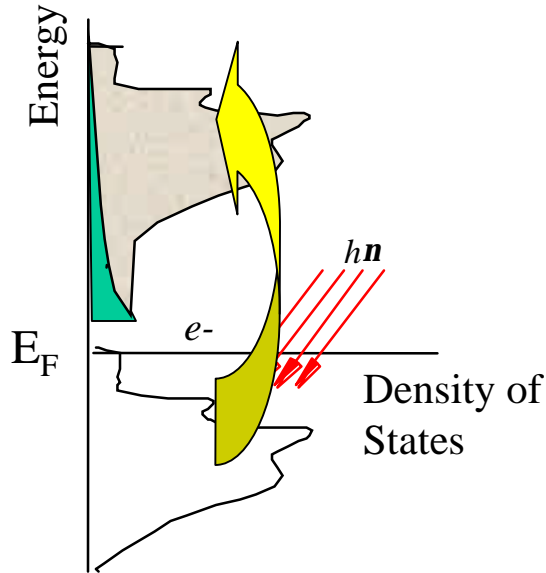
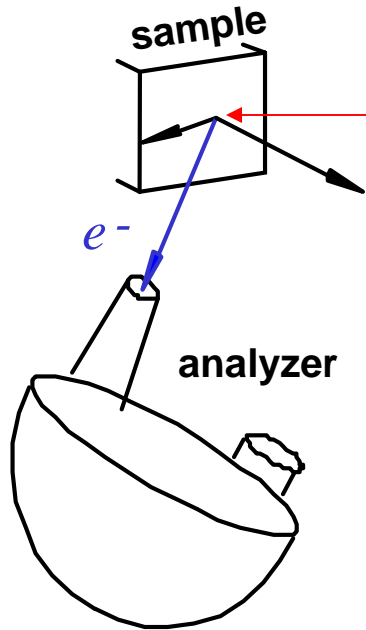
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STANFORD SYNCHROTRON RADIATION LABORATORY



# Photoemission Spectroscopy



High K.E. Low B.E.

Low K.E. High B.E.

Primary electrons – no scattering events.  
Contain information of density of states

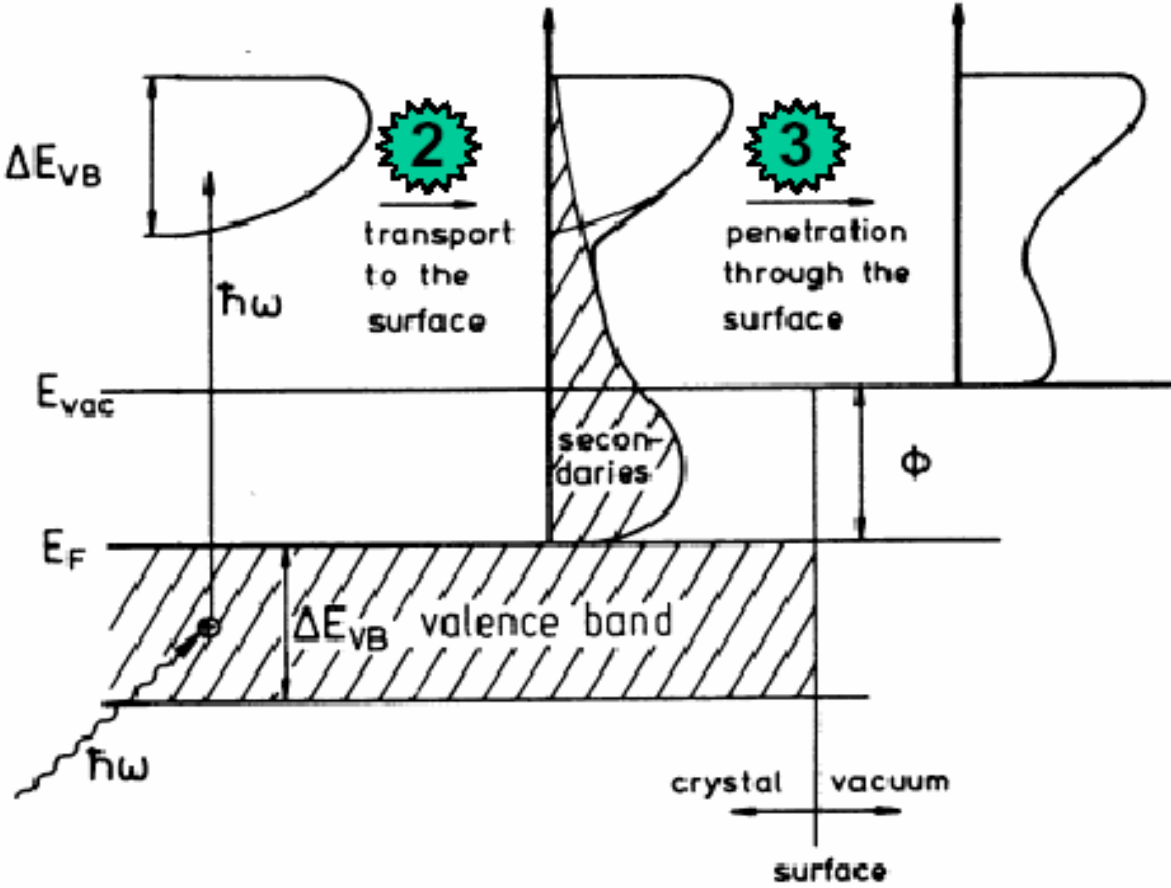
Secondary electrons (inelastic background) – increases with decreasing kinetic energy.

$$E_{kin} = \hbar\omega - \Phi - |E_B|$$

# Three Step Model W.E. Spicer

1

photoexcitation  
of the electron

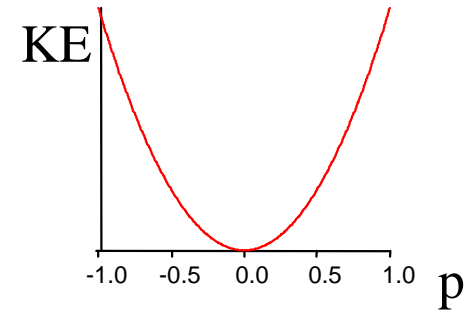


# Angle resolved photoemission spectroscopy

- Angle-dependent core level spectroscopy (not this talk)
  - To vary the surface sensitivity of an experiment
    - normal emission – more bulk sensitive
    - glancing emission – more surface sensitive
  - To perform X-ray photoelectron Diffraction (XPD)
    - Obtain local structural information (similar to EXAFS)
- Angle-dependent valence band spectroscopy (this talk)
  - To measure the  $k$  (momentum) dependence of valence band states
  - To measure electronic band dispersions and Fermi Surfaces
  - To measure symmetries of states
  - To obtain many-body phenomena (e.g. correlated electron systems).

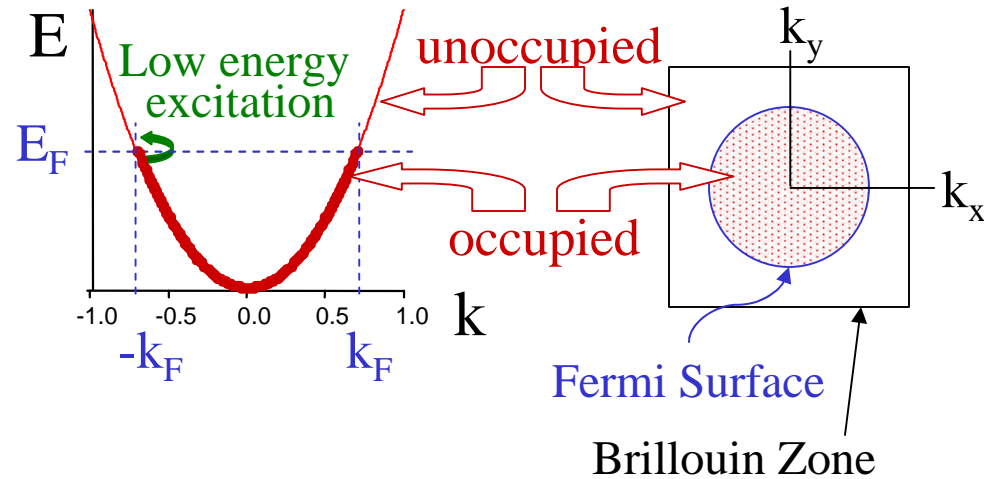
# Quantum numbers E,k

Newton :  $KE = 0.5 mv^2 = p^2/2m$   
 $p = mv, p = \hbar k$

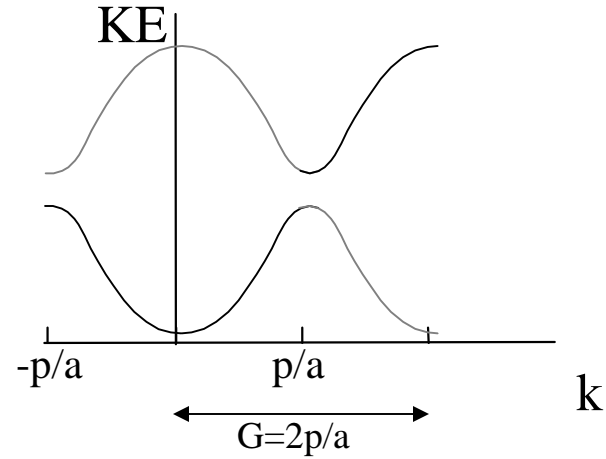


Energy (E) and momentum (p or k) are the most important quantum numbers in a solid. Specifying these specifies behavior of electrons.

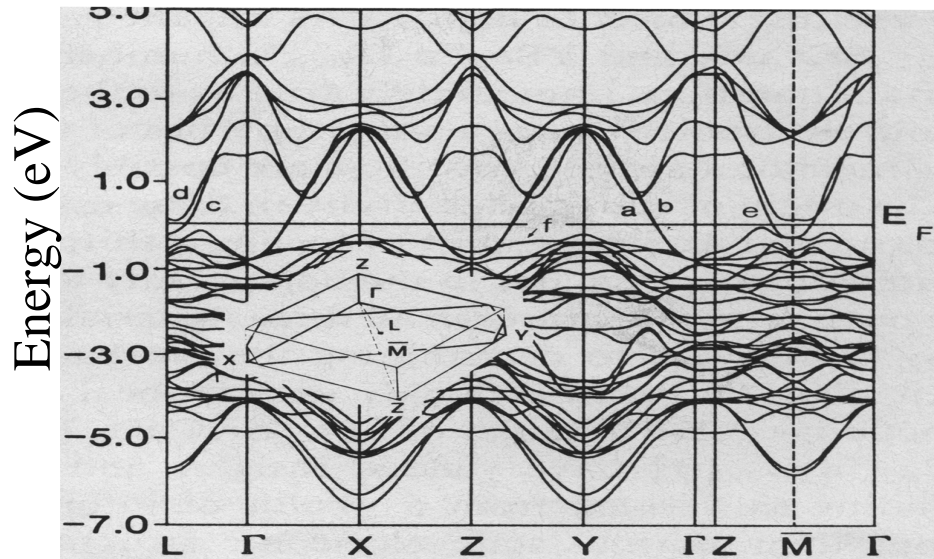
Pauli Principle - each electron goes into its own individual quantum state (new E,k). Fill lowest energy states first. Highest energy electrons are at Fermi Energy  $E_F$ , with a momentum  $\hbar k_F$ . These are the most important electrons. All low energy excitations come from near  $E_F$ .



# Electrons in a periodic potential



Band Structure calculation of  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$  (Bi2212).

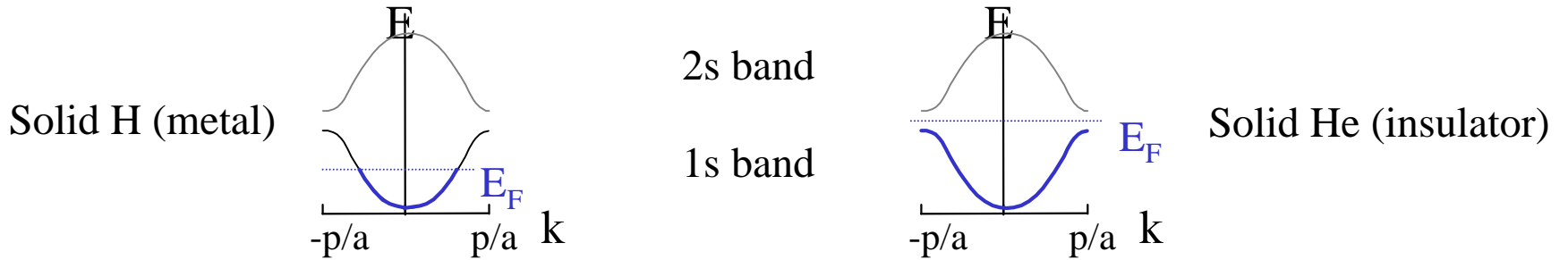


S. Massidda et al, Physica C **152**, 251 (1988)

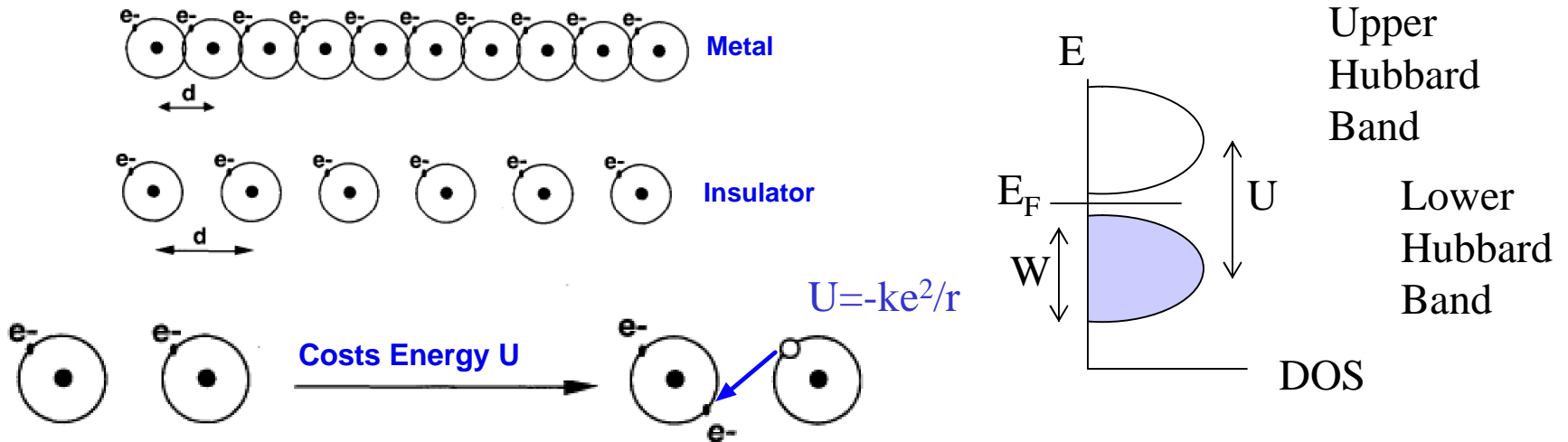
Everything still mean-field or static - no correlation effects yet.

# Metals and Insulators

Band theory:  $E_F$  in a band  $\rightarrow$  Metal.  $E_F$  in a gap between bands  $\rightarrow$  insulator



## Mott Insulators - Failure of this model

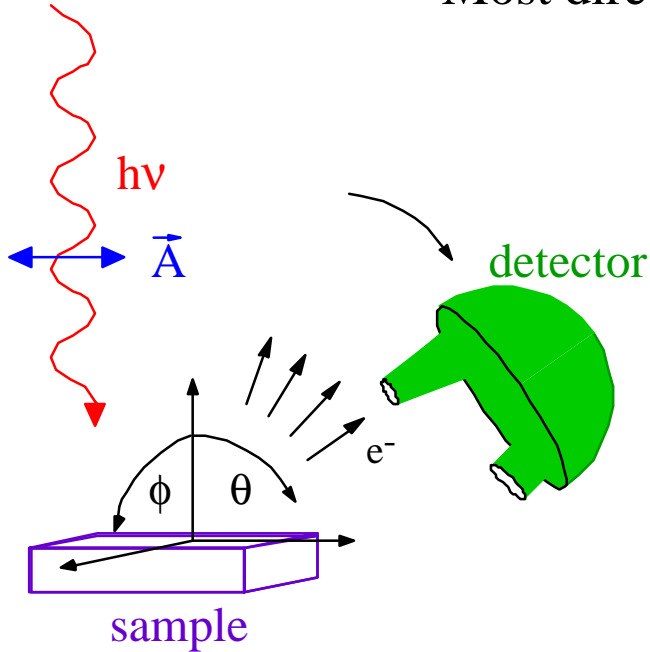


Effects most important in localized (d- and f-electron systems).  
 $\Rightarrow$  High  $T_c$  superconductors, Colossal Magnetoresistive oxides, etc.

# Angle Resolved Photoemission (ARPES)

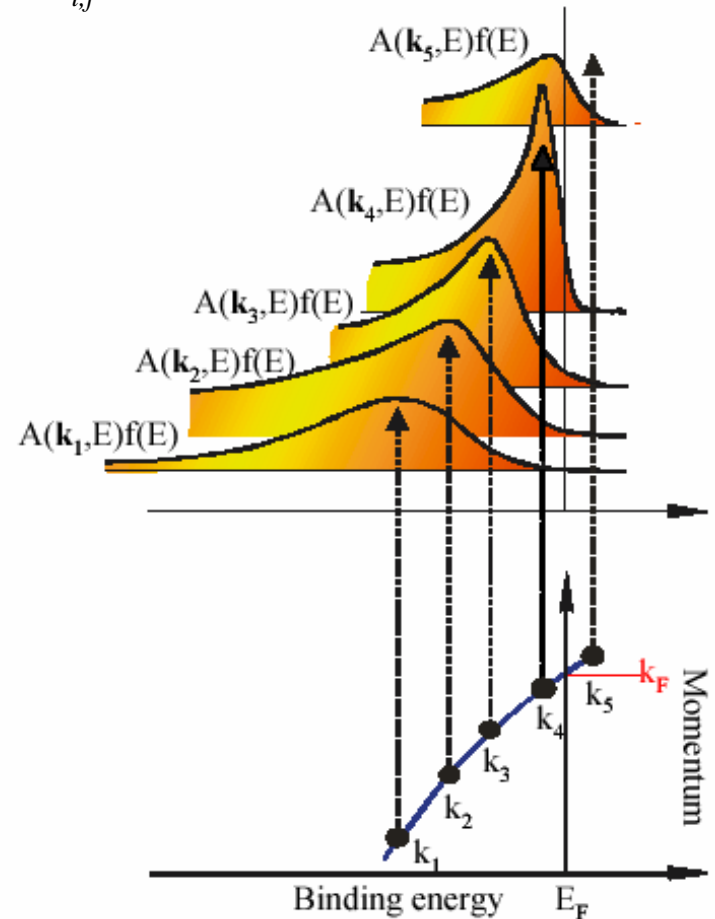
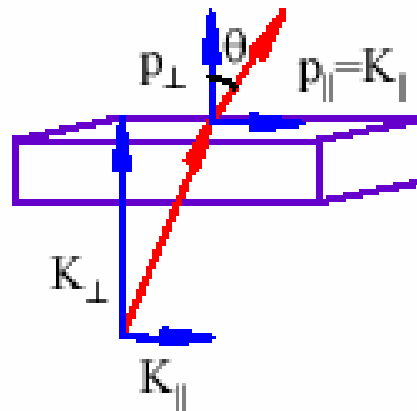
## A momentum resolved spectroscopy

Most direct way to measure E vs. k of a solid.



$$\text{Intensity} \propto \sum_{i,f} \left| \langle f | \vec{p} \cdot \vec{A} | i \rangle \right|^2 A(\vec{k}, E) f(E)$$

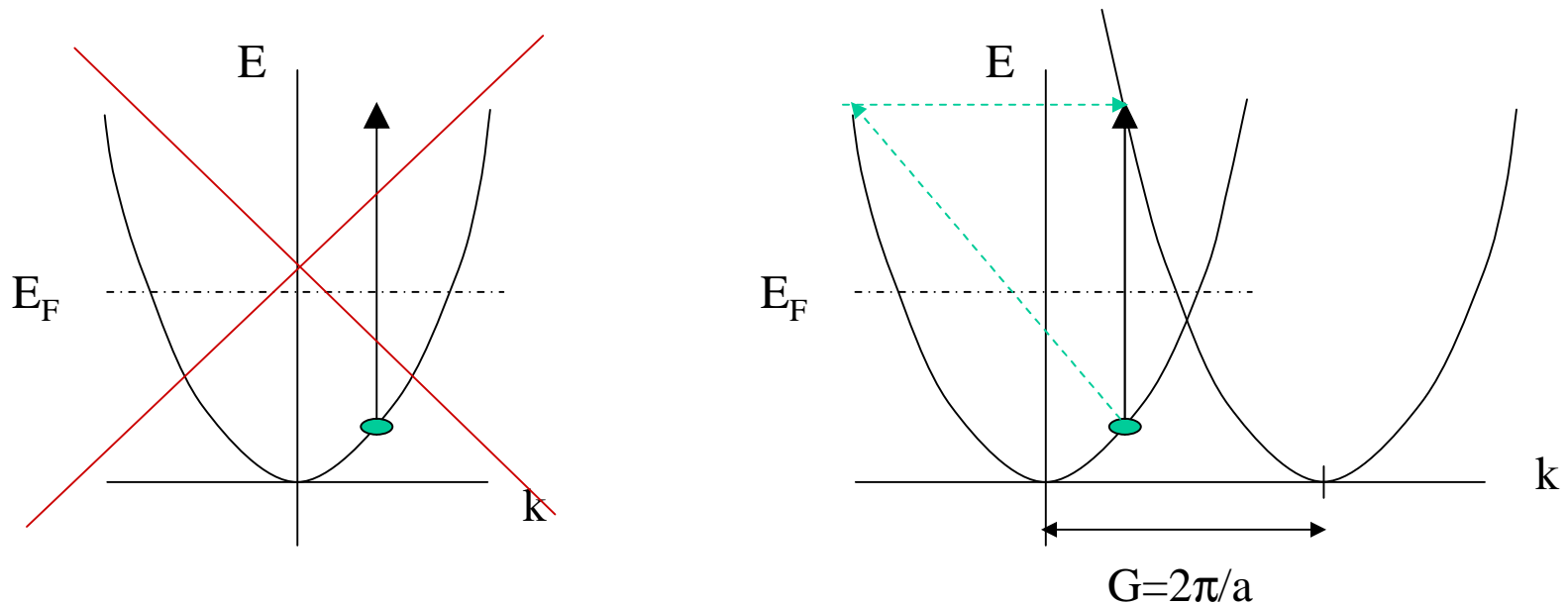
Electron momentum  
Parallel to the surface is  
conserved



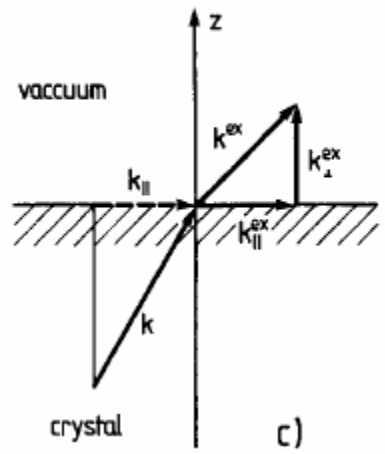
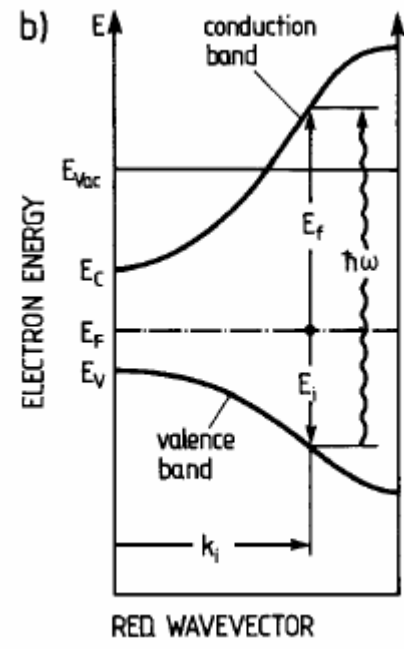
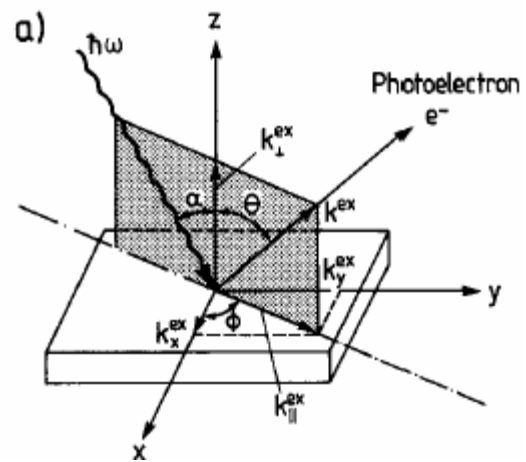
# Momentum Conservation

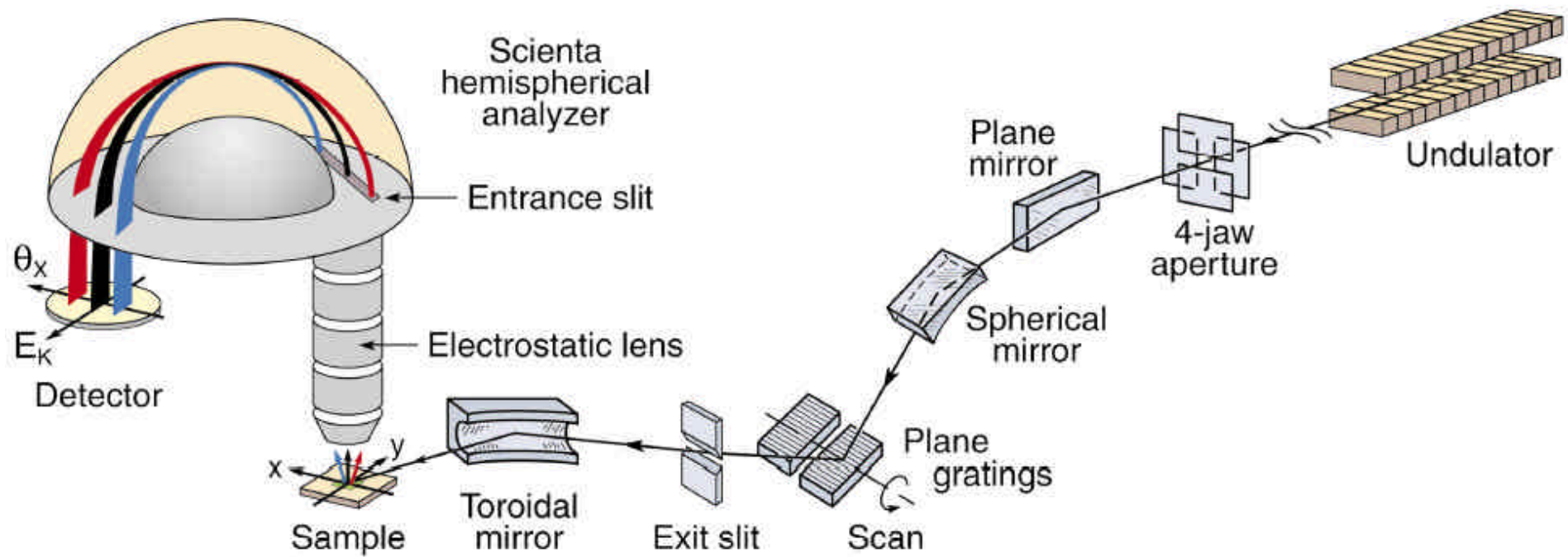
Photons of a few hundred eV or less carry negligible momentum compared to the typical electron momentum scales in a solid.

Therefore we consider “vertical” transition processes. For a free electron parabola there would be no final state and the process is forbidden.

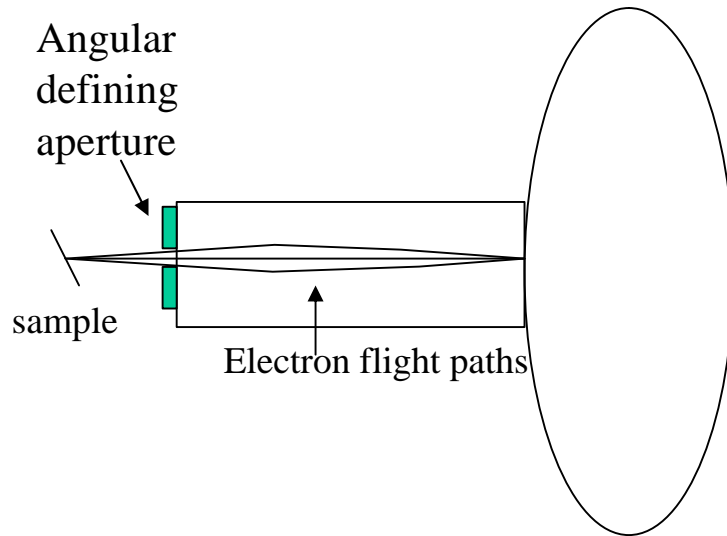


The vertical transition is allowed by considering the extended zone scheme and employing a reciprocal lattice vector  $G=2\pi/a$  (the lattice degree of freedom takes care of the “missing” momentum).



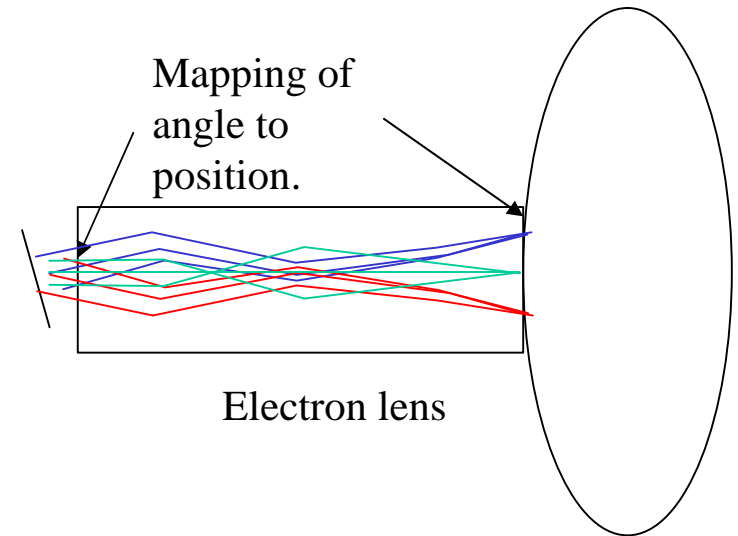


## Conventional mode of performing ARPES

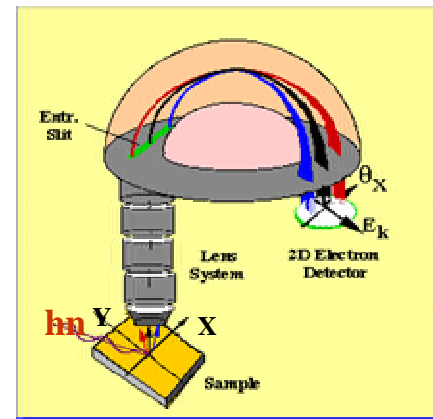


Hemispherical electron detector

## Angle-mode in modern ARPES analyzers

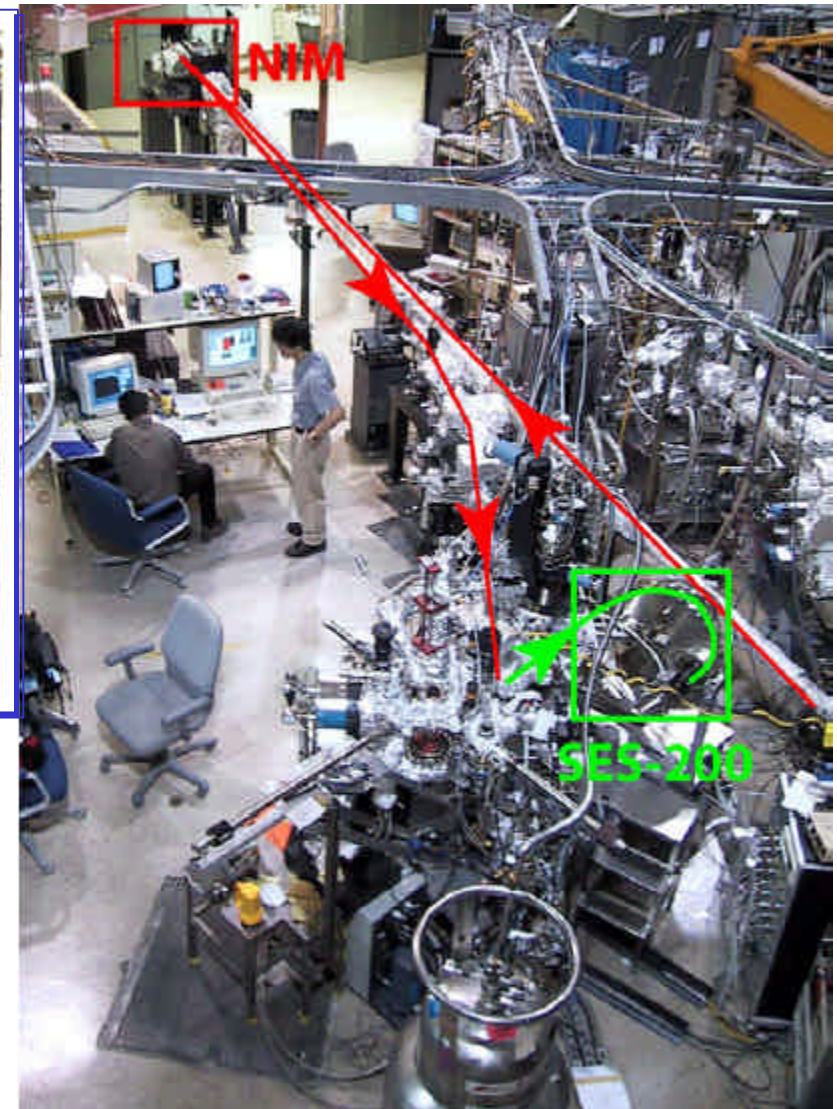
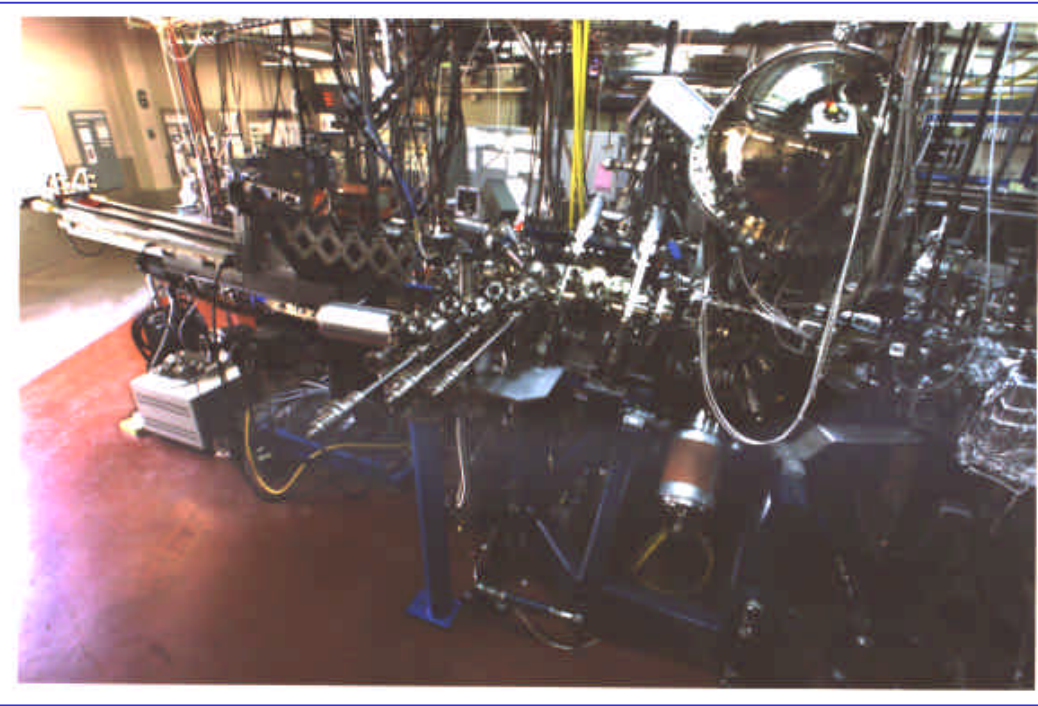


Hemispherical electron detector





STANFORD SYNCHROTRON RADIATION LABORATORY



- UHV analysis chamber ( $10^{-11}$  Torr)
- 5 axis, He cooled sample manipulator
- Load-Lock transfer system
- Samples may be cleaved in UHV

## Angle-resolved photoemission, valence-band dispersions $E(\vec{k})$ , and electron and hole lifetimes for GaAs

T.-C. Chiang, J. A. Knapp,\* M. Aono,<sup>†</sup> and D. E. Eastman  
*IBM Thomas J. Watson Research Center, Yorktown Heights, New York 10598*  
 (Received 3 December 1979)

$E_f(\vec{k}) = \hbar^2 |\vec{k}|^2 / 2m + E_0 = \hbar^2 (k_{\parallel}^2 + k_{\perp}^2) / 2m + E_0$  Final Bloch states.  $E_0$  = "bottom of Muffin tin" – starting point for parabolic band dispersions = -9.34 eV for GaAs.

$E_f(\vec{k}) = E_i(\vec{k}) + h\nu$  Direct or k-conserving transitions.

$E_f = E_k + e\Phi$   $e\Phi$  = work function of sample,  $E_k$  = kinetic energy

$$\begin{aligned} \hbar k_{\parallel} &= (2mE_k)^{1/2} \sin\theta \\ &= [2m(E_i + h\nu - e\Phi)]^{1/2} \sin\theta \end{aligned}$$

$$\begin{aligned} \hbar k_{\perp} &= [2m(E_k \cos^2\theta - V_0)]^{1/2} \\ &= \{2m[(E_i + h\nu - e\Phi) \cos^2\theta - V_0]\}^{1/2} \end{aligned}$$

$V_0 = E_0 - e\Phi$  = "Inner potential". Usually just a fitting parameter.

Normal emission:  $\theta = 0$        $\hbar k_{\parallel} = 0$        $\hbar k_{\perp} = [2m(E_i + e\Phi - E_0)]^{1/2}$

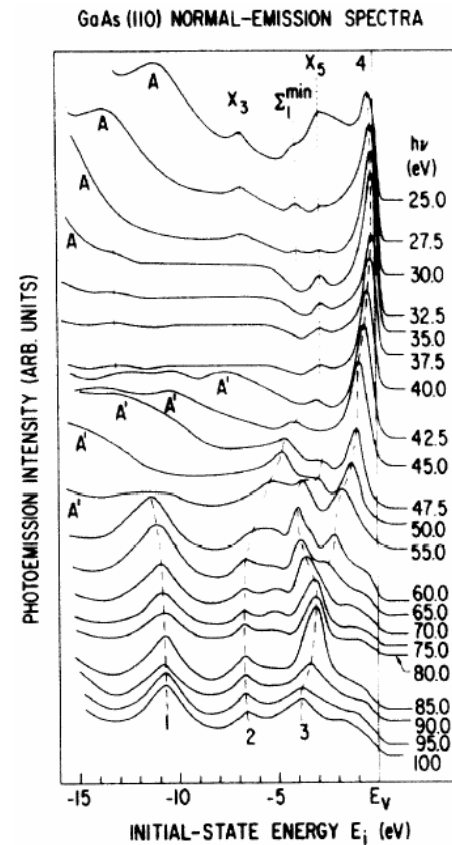
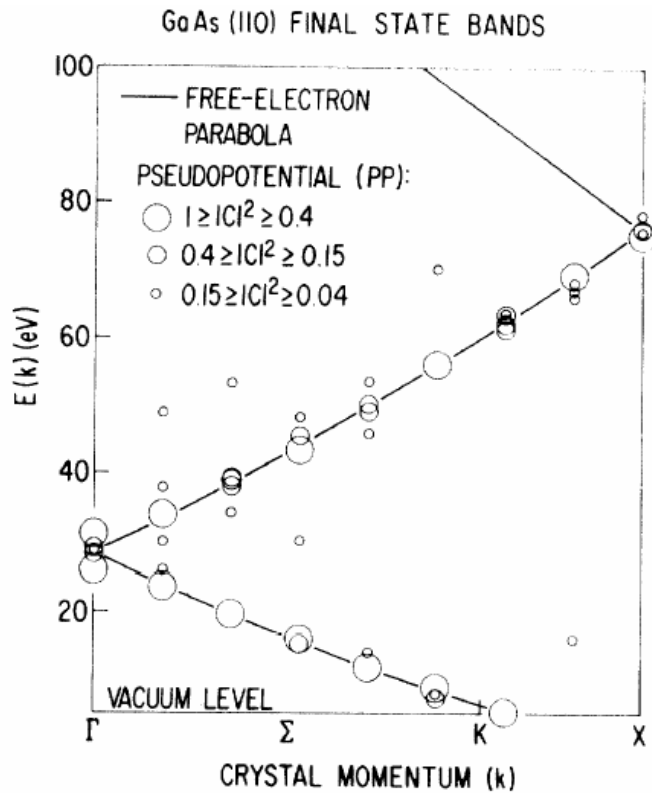
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Normal emission:  $\theta = 0$

$$\hbar k_{\parallel} = 0$$

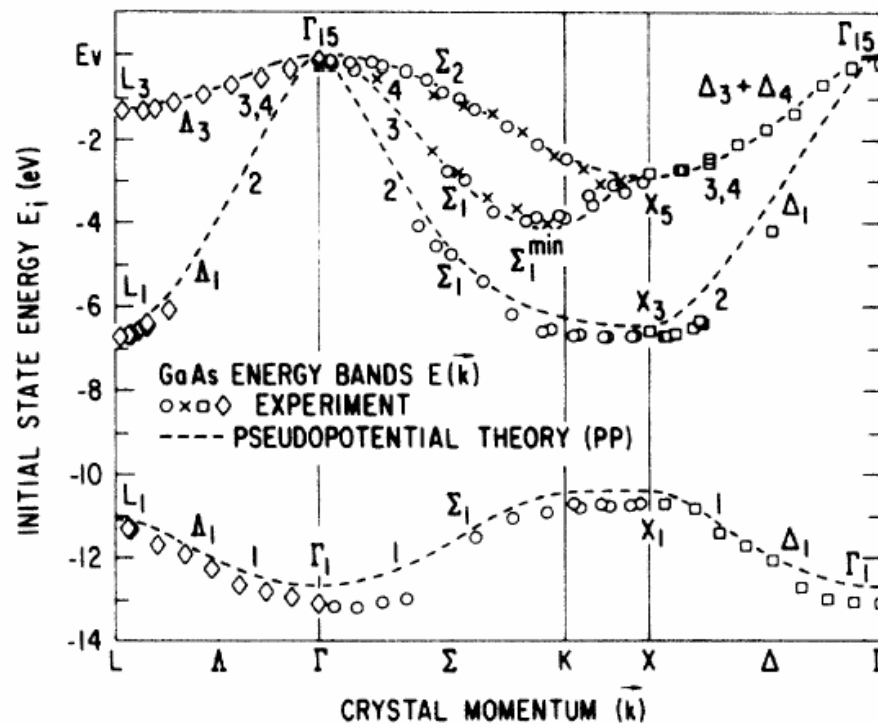
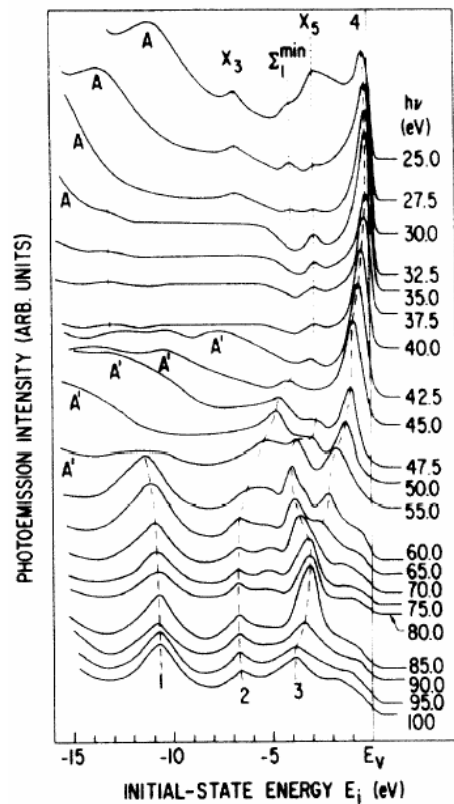
$$\hbar k_{\perp} = [2m(E_i + e\Phi - E_0)]^{1/2}$$

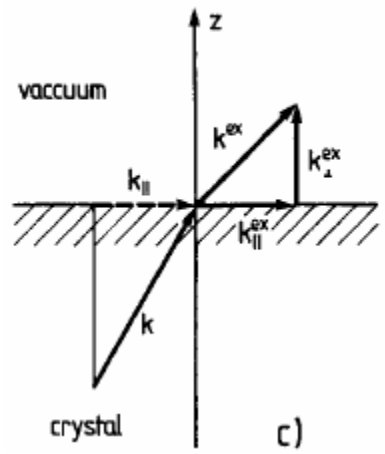
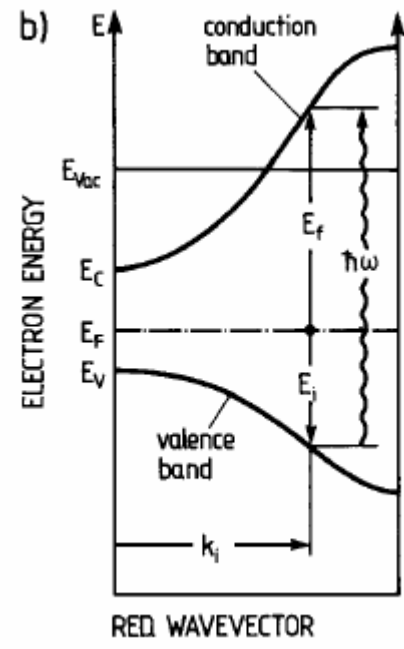
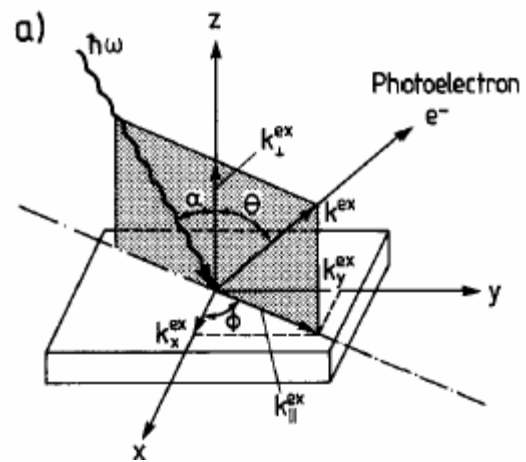


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GaAs (110) NORMAL-EMISSION SPECTRA





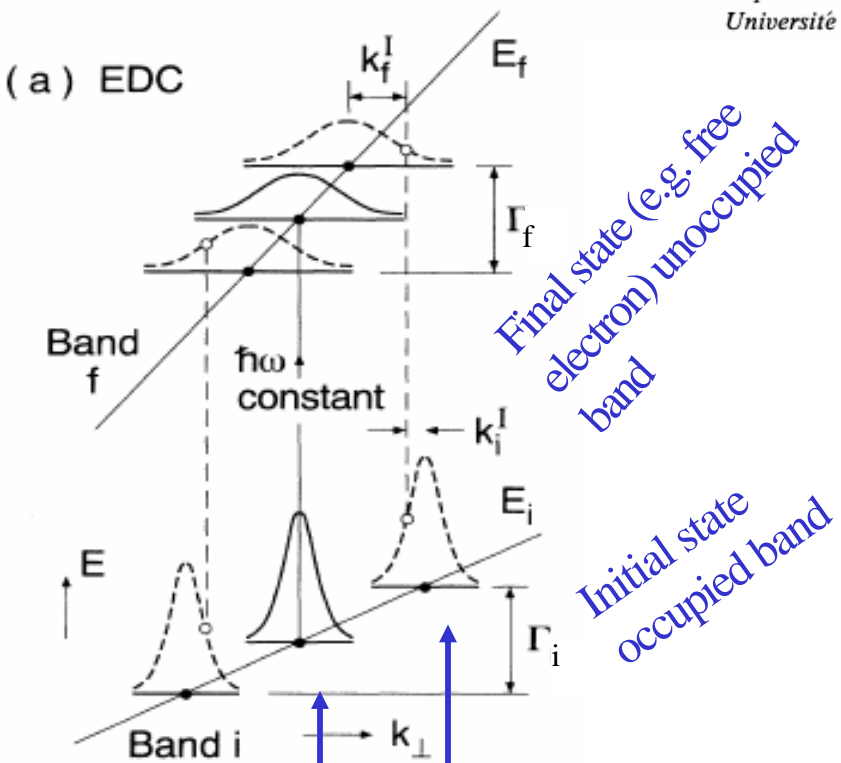
### Photoemission linewidths and quasiparticle lifetimes

N. V. Smith

*AT&T Bell Laboratories, Murray Hill, New Jersey 07974*

P. Thiry and Y. Petroff\*

*Laboratoire pour l'Utilisation du Rayonnement Electromagnétique,  
Université de Paris-Sud, F-91405 Orsay, France*



Measured linewidths  $\Gamma_m$  have a contribution from the lifetimes of the initial state (lifetime  $\Gamma_i$ ) and final state (lifetime  $\Gamma_f$ ).

$$\Gamma_m = \frac{\Gamma_i / |v_{i\perp}| + \Gamma_f / |v_{f\perp}|}{\left| \frac{1}{v_{i\perp}} \left[ 1 - \frac{mv_{i\parallel} \sin^2 \theta}{\hbar k_{\parallel}} \right] - \frac{1}{v_{f\perp}} \left[ 1 - \frac{mv_{f\parallel} \sin^2 \theta}{\hbar k_{\parallel}} \right] \right|}$$

Nearly 2D limit:  $v_{i\text{perp}}$  small. Near isolation of  $\Gamma_i$ .

$$\Gamma_m = \Gamma_i + \left| \frac{v_{i\perp}}{v_{f\perp}} \right| \Gamma_f$$

$k_{\text{perp}}$  (and  $h\nu$ ) value with half maximum intensity

$k_{\text{perp}}$  (and  $h\nu$ ) value with maximum intensity (cross section)

## 2D compounds

- Can ignore  $k_z$  dispersion.
- Need not vary photon energy to map out Fermi surface and high symmetry directions.
- Less final state broadening. Intrinsic initial-state linewidths can be studied.

## Fermi Surface, Surface States, and Surface Reconstruction in $\text{Sr}_2\text{RuO}_4$

A. Damascelli, D. H. Lu, K. M. Shen, N. P. Armitage, F. Ronning, D. L. Feng, C. Kim, and Z.-X. Shen

*Department of Physics, Applied Physics and Stanford Synchrotron Radiation Laboratory,  
Stanford University, Stanford, California 94305*

T. Kimura and Y. Tokura

*Department of Applied Physics, The University of Tokyo, Tokyo 113-8656, Japan  
and JRCAT, Tsukuba, 305-0046, Japan*

Z. Q. Mao and Y. Maeno

*Department of Physics, Kyoto University, Kyoto 606-8502, Japan  
and CREST-JST, Kawagushi, Saitama 332-0012, Japan*

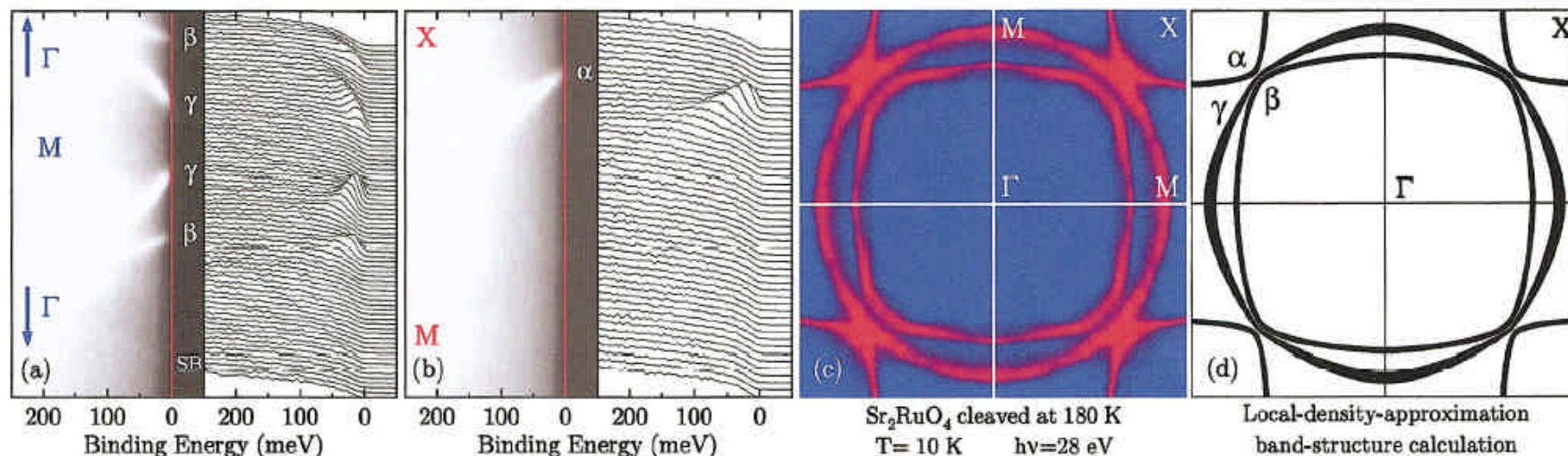
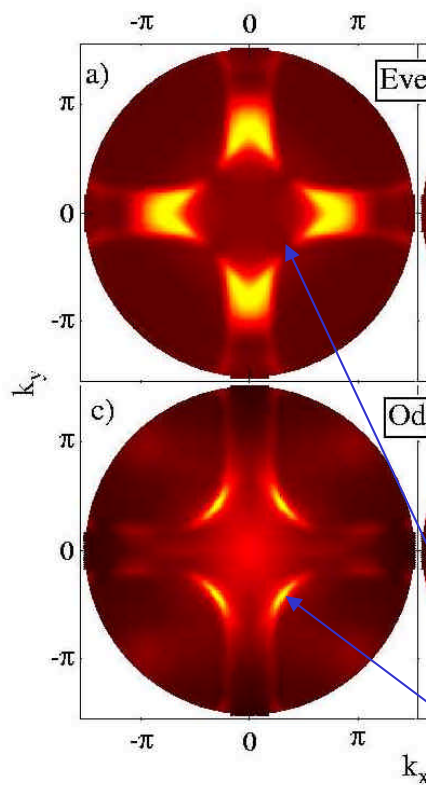


FIG. 9. Photoemission results from  $\text{Sr}_2\text{RuO}_4$ : ARPES spectra and corresponding intensity plot along (a)  $\Gamma$ -M and (b) M-X; (c) measured Fermi surface; (d) calculated Fermi surface (Mazin and Singh, 1997). From Damascelli *et al.*, 2000 (Color).

# How different Fermi surface maps emerge in photoemission from Bi2212

M.C. Asensio<sup>1,2,\*</sup>, J. Avila<sup>1,2</sup>, L. Roca<sup>1,2</sup>, A. Tejeda<sup>1,2,\*</sup>, G.D. Gu<sup>3</sup>, M. Lindroos<sup>4,5</sup>, R.S. Markiewicz<sup>5</sup>, and A. Bansil<sup>5</sup>

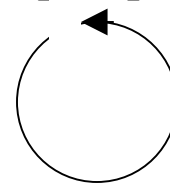


Photon E field  
(Polarization direction)

Electron emission  
direction

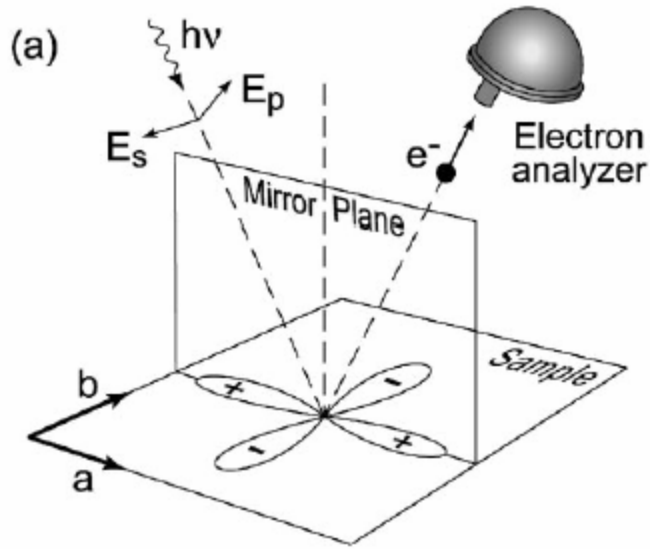


Sample spins



Zeros shifted by 45 degrees.

# Symmetry Analysis

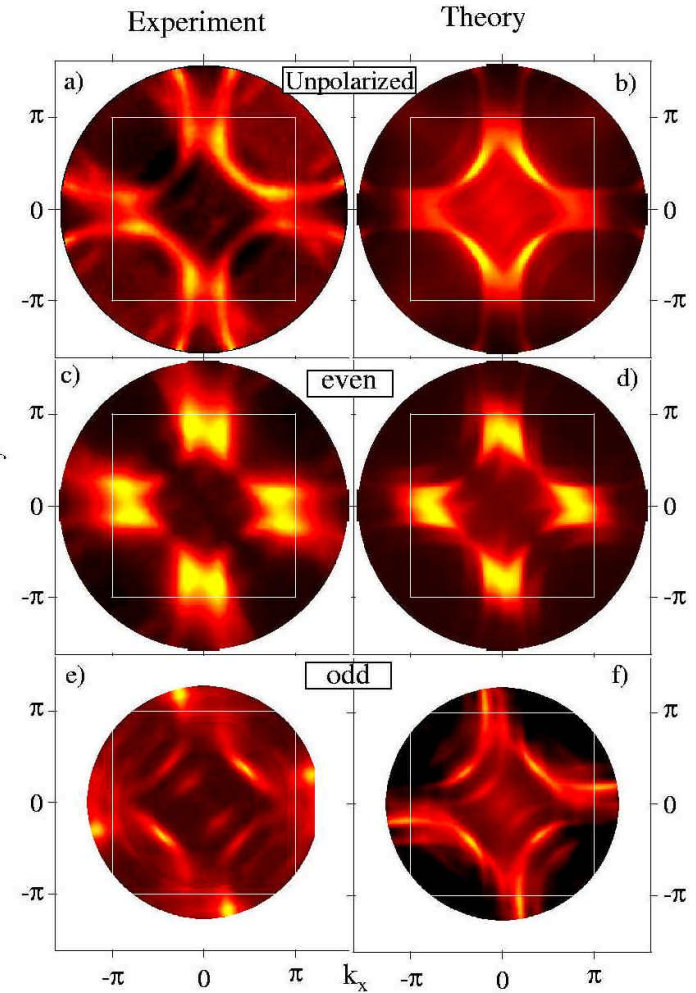


E field



$$\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle \begin{cases} \phi_i^{\mathbf{k}} \text{ even } \langle + | + | + \rangle \Rightarrow \mathbf{A} \text{ even} \\ \phi_i^{\mathbf{k}} \text{ odd } \langle + | - | - \rangle \Rightarrow \mathbf{A} \text{ odd.} \end{cases}$$

The matrix element is integrated over all space. The integration axis of interest here is perpendicular to a chosen mirror plane. If net odd symmetry, then the matrix element integrates to exactly zero.



## Matrix Element for Photoemission

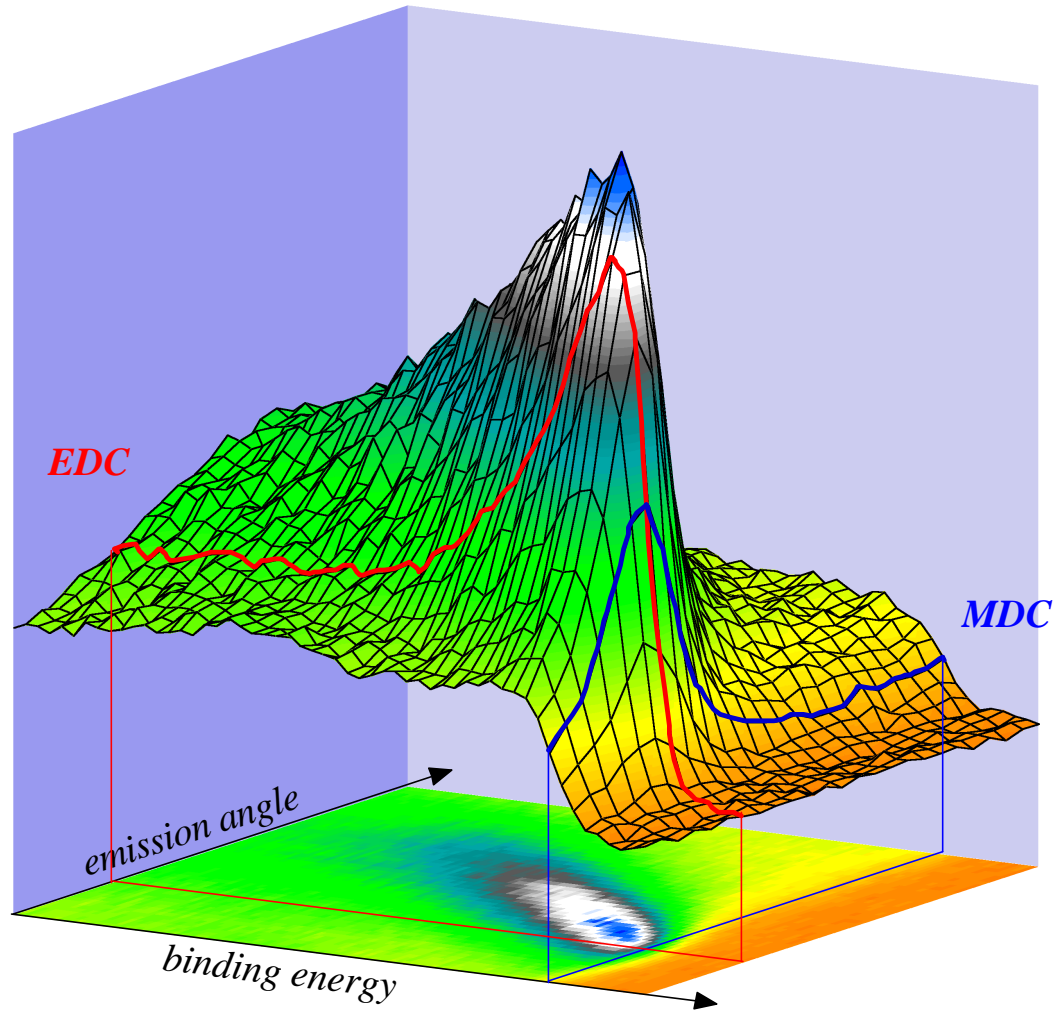
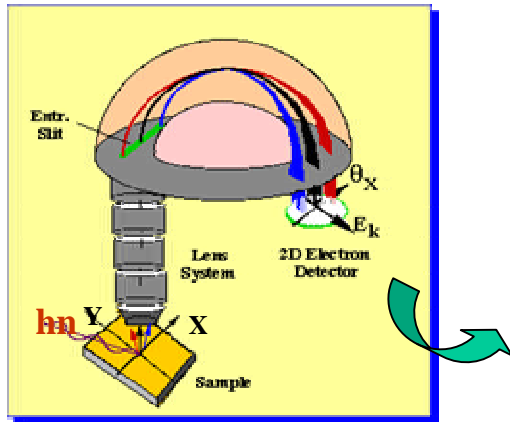
**Perturbation Theory gives Fermi's Golden Rule for transition probability**

$$w = \frac{2\pi}{\hbar} \left| \langle \psi_f | H_{\text{int}} | \psi_i \rangle \right|^2 \delta(E_f - E_i - \hbar\omega)$$

**For dipole allowed transitions,**

$$H_{\text{int}} = \frac{e}{mc} \mathbf{A} \cdot \mathbf{p}$$

# Two dimensional electron detection



Energy Distribution Curve (EDC)

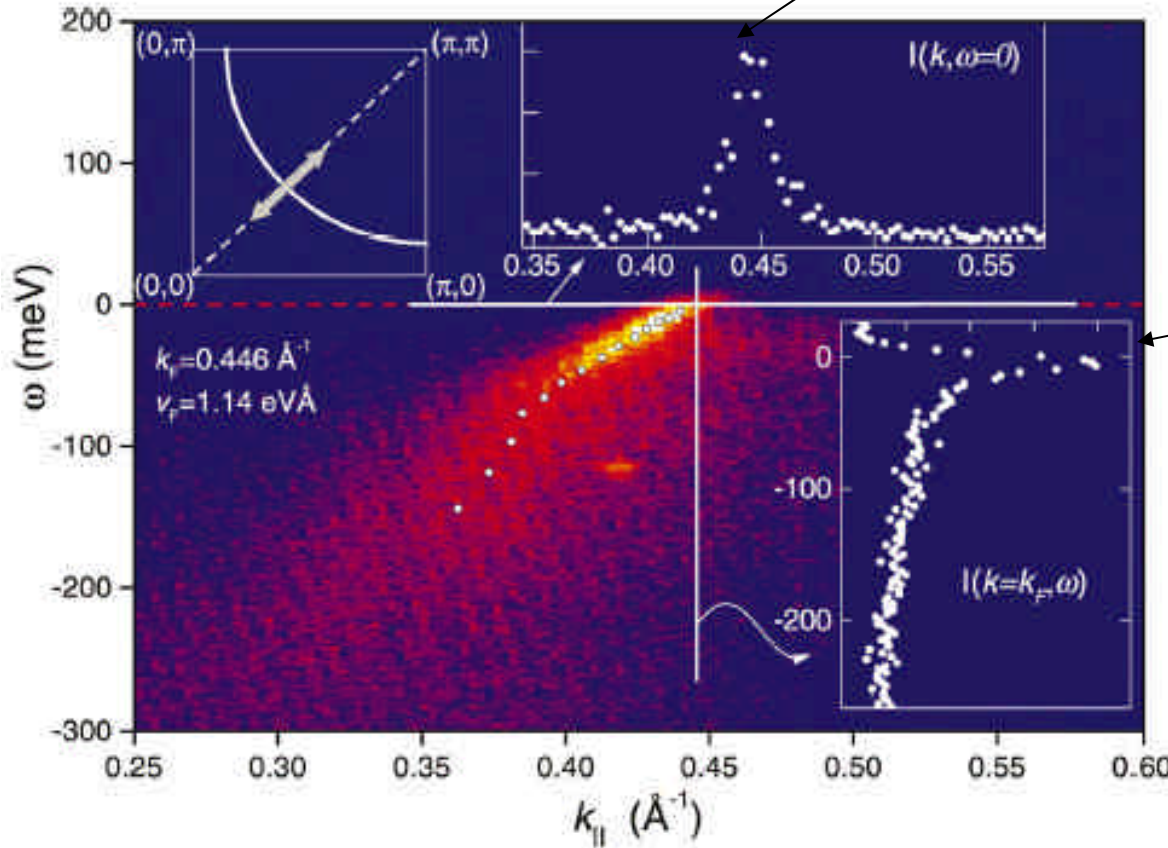
Momentum Distribution Curve (MDC)

# 2D detection on the high $T_c$ superconductor $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$

T. Valla,<sup>1</sup> A. V. Fedorov,<sup>1</sup> P. D. Johnson,<sup>1</sup> B. O. Wells,<sup>1,4</sup>  
 S. L. Hulbert,<sup>2</sup> Q. Li,<sup>3</sup> G. D. Gu,<sup>5</sup> N. Koshizuka<sup>6</sup>

Momentum Distribution Curve (MDC)

Peak width  $\Delta k = 1/l$  :  $l$  = electron mean free path.



Energy Distribution Curve (EDC)

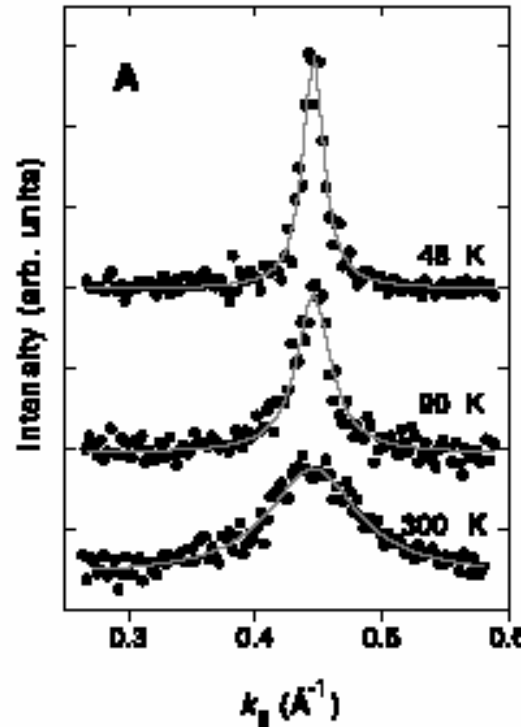
Peak width  $\Delta E = \hbar/\tau$   
 $1/\tau$  = scattering rate  
 $\tau$  = quasiparticle lifetime

$$\Delta E = \Delta k * dE/dk = \Delta k * v$$

MDCs are usually more symmetric than EDCs (simple Lorentzian). → easier to fit

# 2D detection on the high T<sub>c</sub> superconductor Bi<sub>2</sub>Sr<sub>2</sub>CaCu<sub>2</sub>O<sub>8</sub>

Valla et al., Science (1999)



Lorentzian MDC fits as a function of temperature.

Broader peaks at higher T  $\rightarrow$  shorter photohole lifetimes.

Origin: Electron-electron scattering? Electron-phonon? Electron-impurity?

The same mechanisms for scattering also affect other probes (optics, transport, etc.).

Also the interactions responsible for the superconducting pairing?

# Many-Body Effects in Angle-Resolved Photoemission: Quasiparticle Energy and Lifetime of a Mo(110) Surface State

T. Valla,<sup>1</sup> A. V. Fedorov,<sup>1</sup> P. D. Johnson,<sup>1</sup> and S. L. Hulbert<sup>2</sup>

$$A(\mathbf{k}, \omega) \propto \frac{\text{Im}\Sigma(\mathbf{k}, \omega)}{[\omega - \varepsilon_{\mathbf{k}} - \text{Re}\Sigma(\mathbf{k}, \omega)]^2 + [\text{Im}\Sigma(\mathbf{k}, \omega)]^2}$$

“spectral function” = ARPES weight ( $\mathbf{k}, \omega$ )

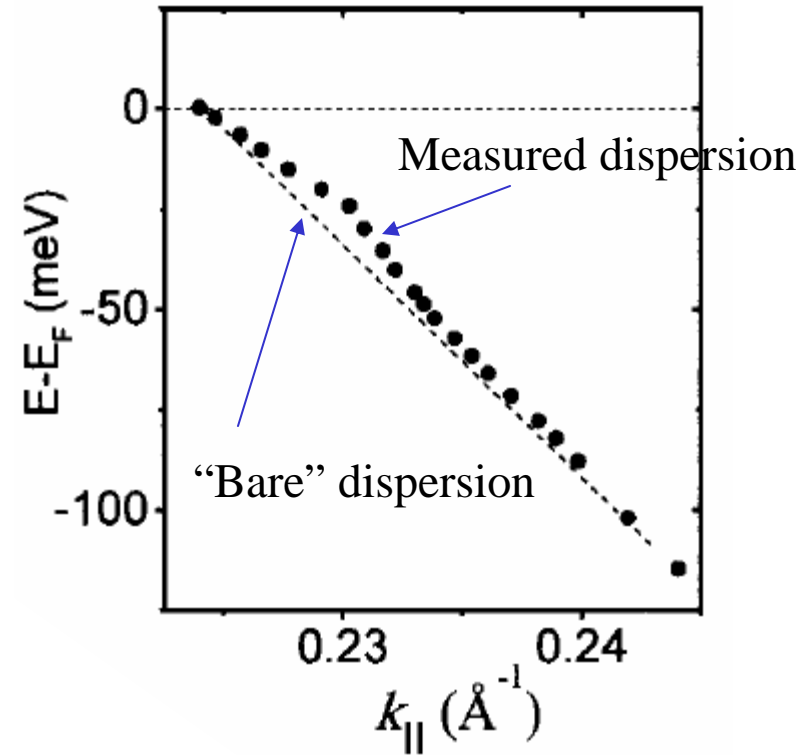
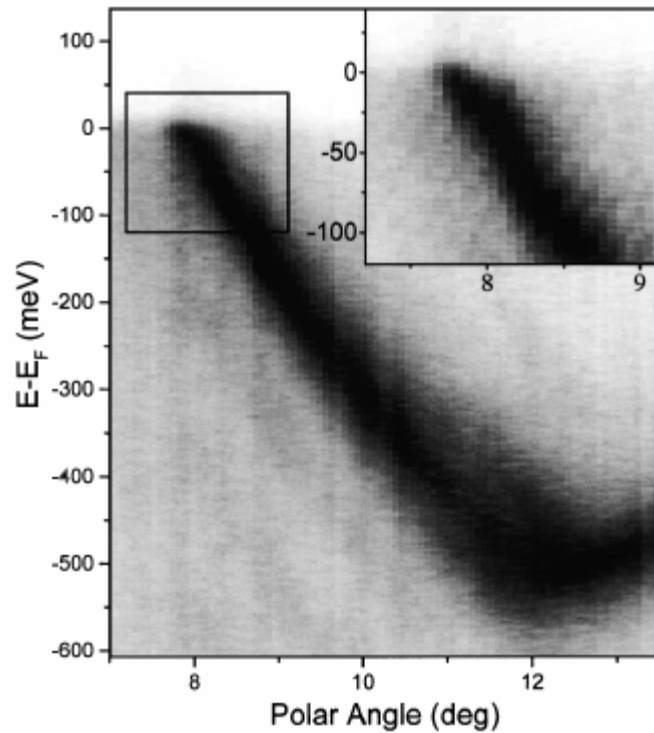


FIG. 1. ARPES intensity plot of the Mo(110) surface recorded along the  $\bar{\Gamma}$ - $\bar{N}$  line of the surface Brillouin zone at 70 K. Shown in the inset is the spectrum of the region around  $k_F$  taken with special attention to the surface cleanliness.

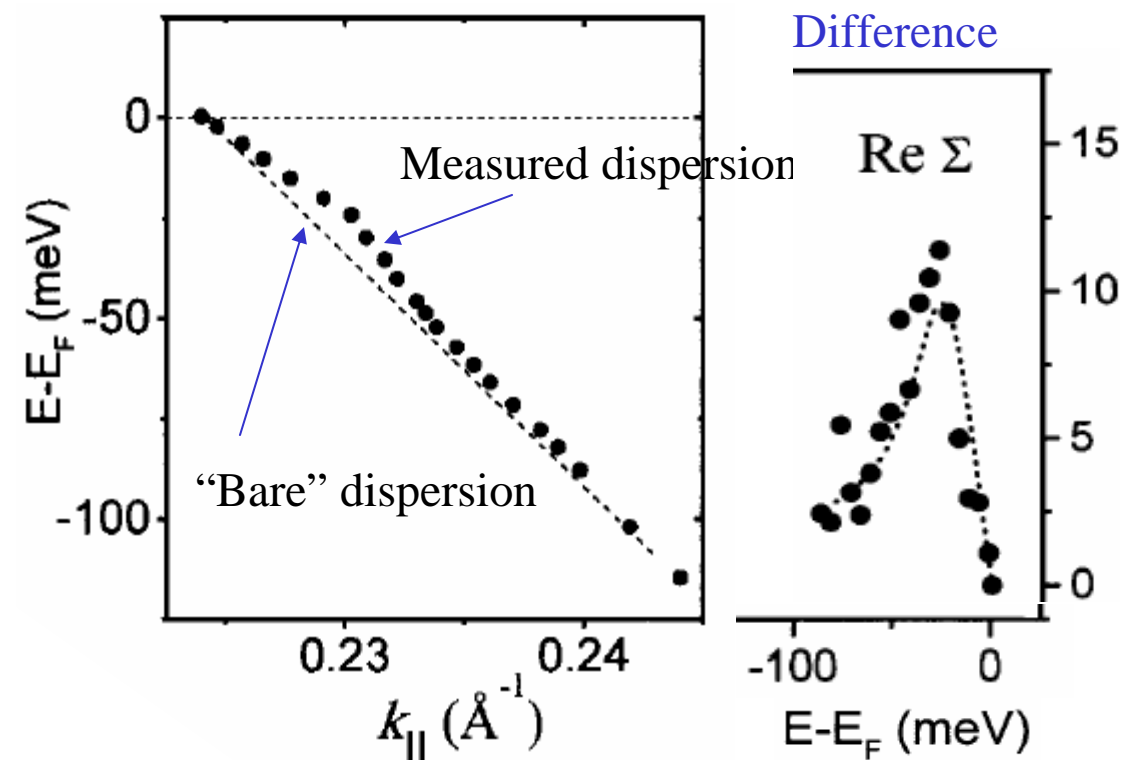
“Kink effect”

## Many-Body Effects in Angle-Resolved Photoemission: Quasiparticle Energy and Lifetime of a Mo(110) Surface State

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“spectral function” = ARPES weight ( $\mathbf{k}, \omega$ )



$A(\mathbf{k}, \omega)$  peaks when  $[\omega - \varepsilon_{\mathbf{k}} - \text{Re}\Sigma] = 0$

or when

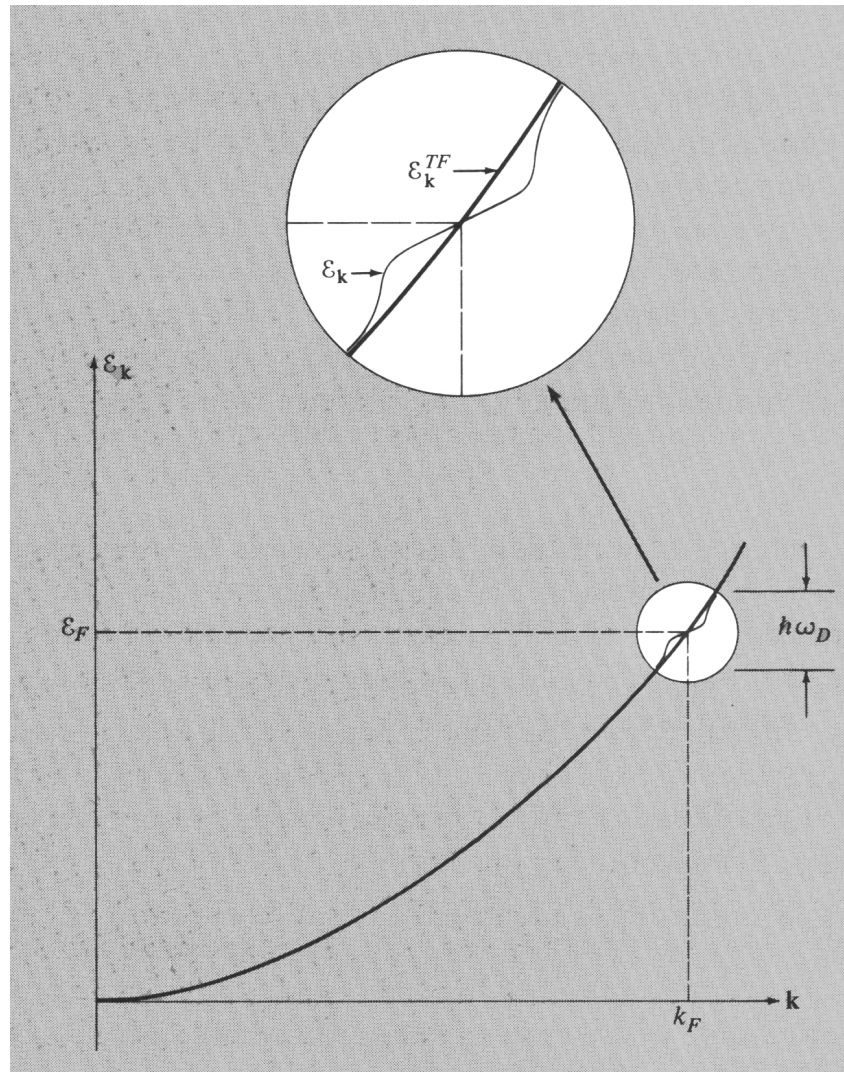
$$\omega = \varepsilon_{\mathbf{k}} + \text{Re}\Sigma$$

Bare band:  $\text{Re}\Sigma = 0$

Measured:  $\text{Re}\Sigma = \text{finite}$ .

$\Sigma$  = electron “self energy”. Here the “kink” is due to electron-phonon scattering. (Phonon lives at kink scale or  $\sim 30 \text{ meV}$ ).

Changes in the carrier mass due to electron-phonon coupling only affects the near- $E_F$  states  
From Ashcroft and Mermin, Solid State Physics, 1976

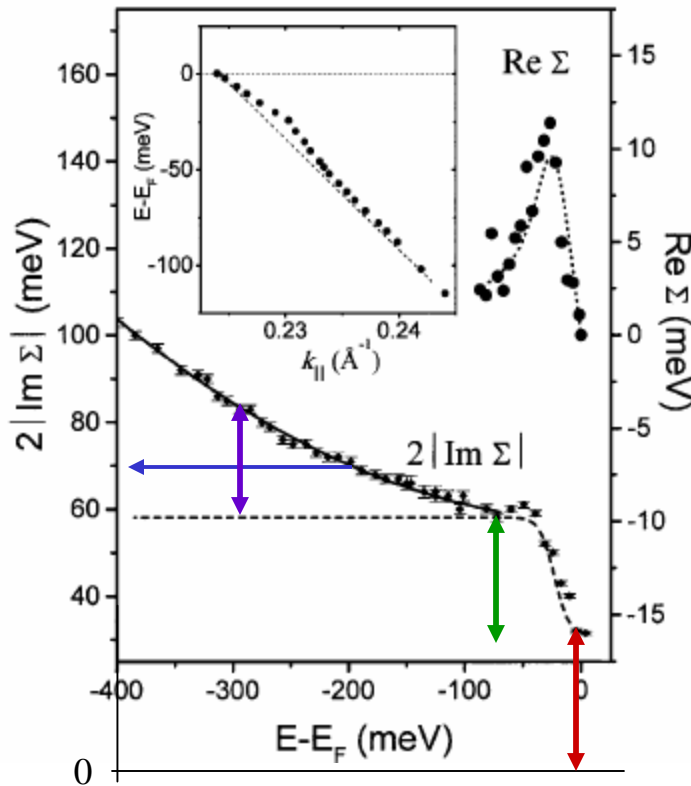


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FWHM of  
quasiparticle peak



$\text{Im}\Sigma$  = width of spectral peak  
Measurable in the same spectra.

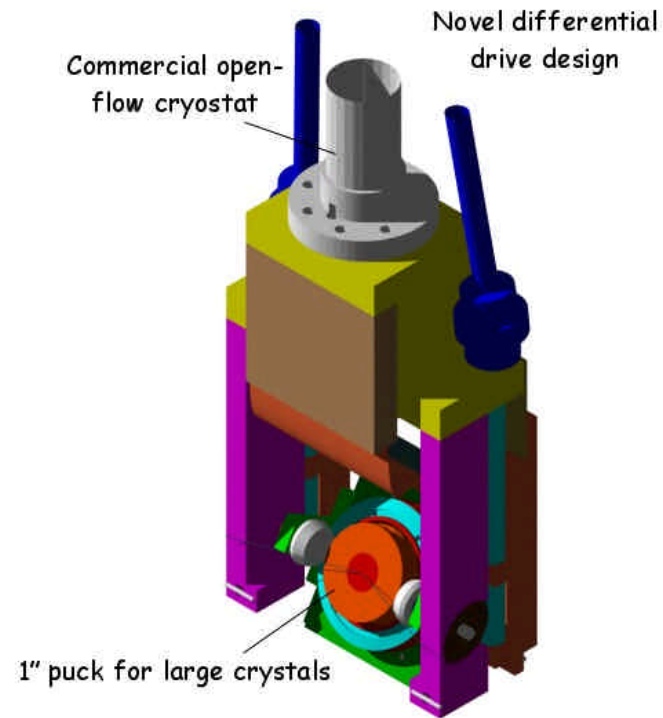
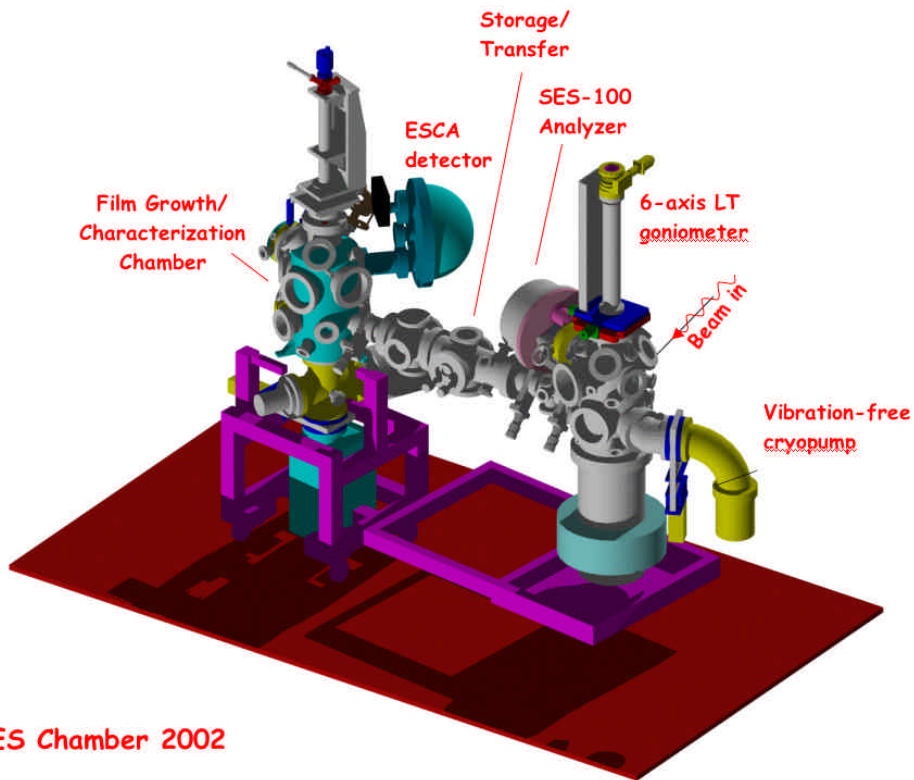
$\text{Im}\Sigma$  and  $\text{Re}\Sigma$  related through Kramers-Kronig relations.

Electron-electron scattering

Coupling to phonons

Impurities, finite resolution,  
final state effects, etc.

# Electronic Structure Factory at beamline 7, ALS



[A data set.](#)

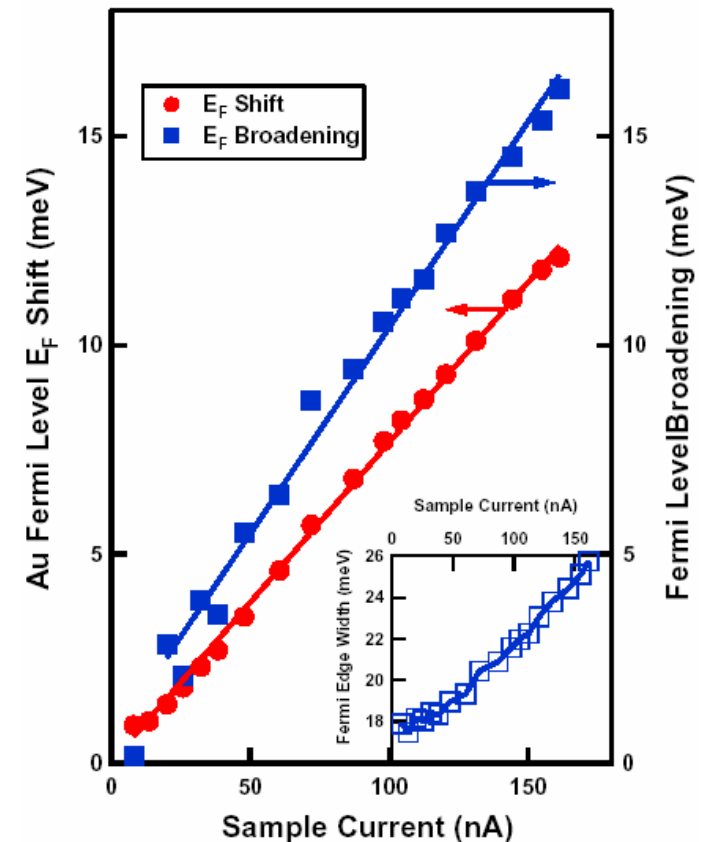
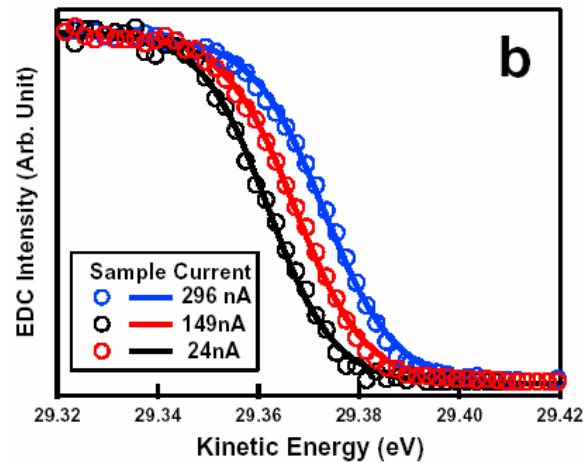
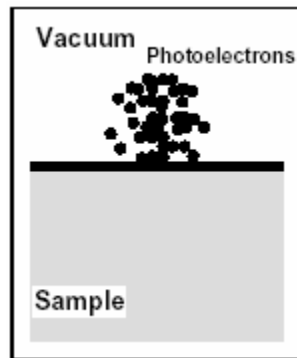
## Experimental issues:

- a) Sample charging – for insulating or weakly insulating samples.
  - Vary the photon flux and look for energy shifts.
  - Raise the sample temperature
  - Electron flood gun to replenish lost electrons
- b) Space-charge effect – for high beam intensities.
  - Shifts and broadens peaks.
  - Only an issue for highest beam intensities, highest resolution.
  - Test by adjusting beam intensity.
  - May defocus beam on sample.
- c) Sample ageing during measurements
  - Gas chemisorption or physisorption. Warming may regenerate.
  - Gas leaving the sample (e.g. oxides). Low temp helps.
  - Photon beam damage. Lower energy photons may help.
  - Measure quickly!
  - Measure many samples, doing different aspects in a different order.
- d) Surface/cleave quality
  - Especially relevant for high angular resolution experiments.
  - Defects/impurities/step edges.
  - Different work functions for different faces.

## Space charge effect and mirror charge effect in photoemission spectroscopy

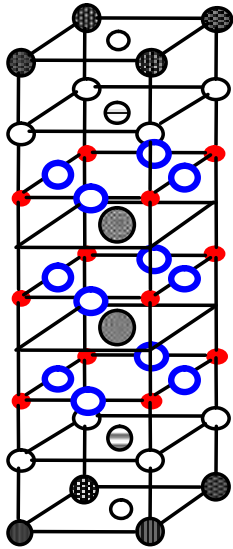
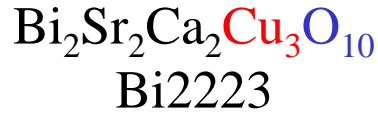
X.J. Zhou<sup>a,b,\*</sup>, B. Wannberg<sup>c</sup>, W.L. Yang<sup>a,b</sup>, V. Brouet<sup>a,b</sup>, Z. Sun<sup>d</sup>, J.F. Douglas<sup>d</sup>, D. Dessau<sup>d</sup>,  
Z. Hussain<sup>b</sup>, Z.-X. Shen<sup>a</sup>

From ALS undulator beamline 10.0.1

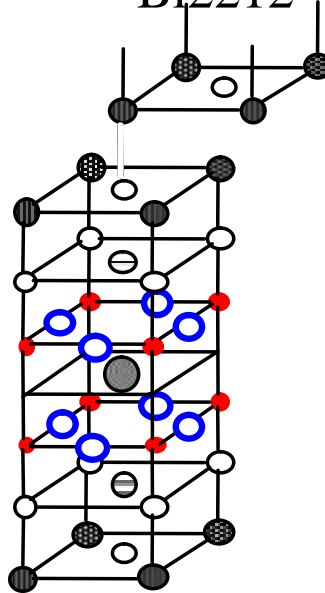
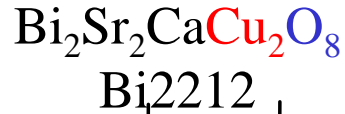


# Bi-Sr-Ca-Cu-O family crystal structure

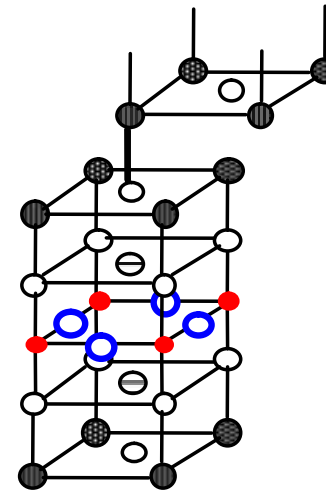
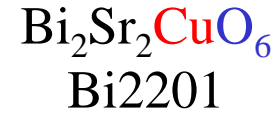
Superconductivity occurs in the  $\text{CuO}_2$  planes



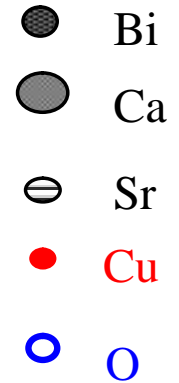
( 3  $\text{CuO}$  L )  
 $T_c = 105$  K



( 2  $\text{CuO}$  L )  
 $T_c = 92$  K



( 1  $\text{CuO}$  L )  
 $T_c = 0 \sim 20$  K

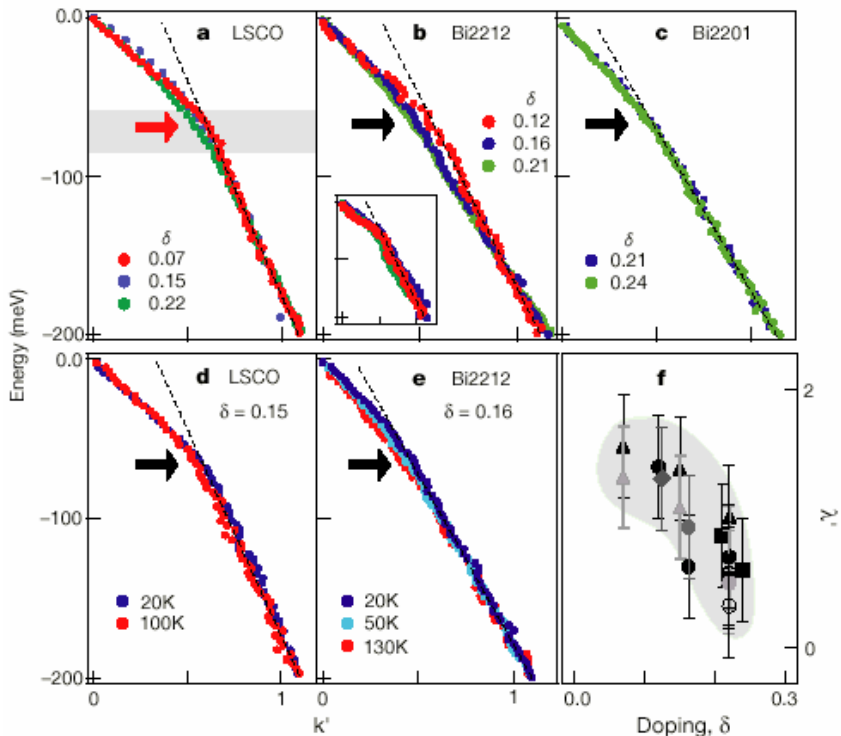


↑ Main compound studied

# Recent ARPES results - kinks in HTSC's (p,p) direction (nodal direction of d-wave gap)

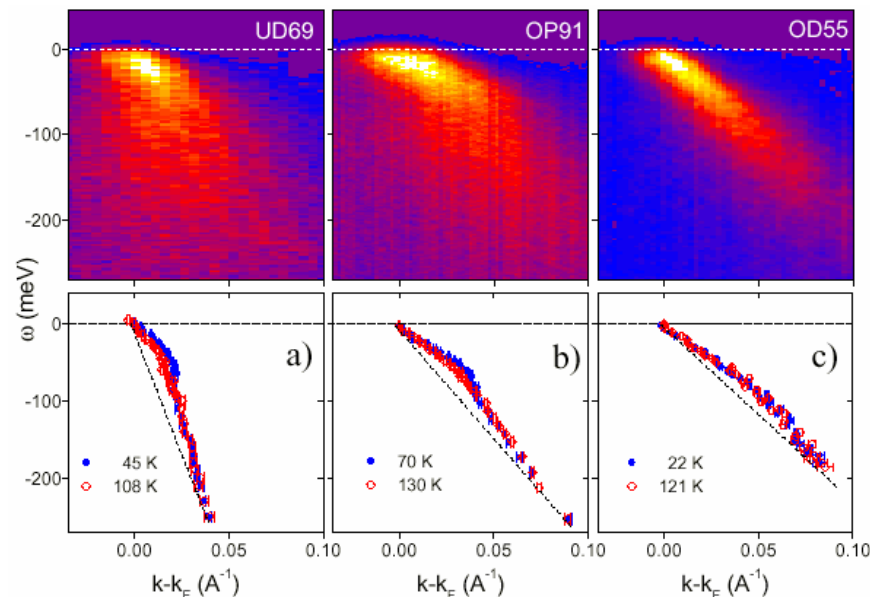
Stanford Group  
Lanzara et al.

Nature **412**,510 (2001)

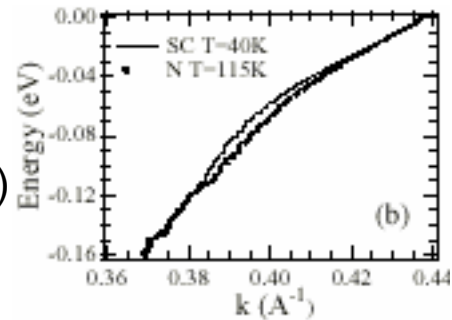


Brookhaven Group  
Johnson et al.

*cond-mat/0102260* (2001).



Argonne Group  
Kaminski et al.  
PRL **86**, 1070 (2001)



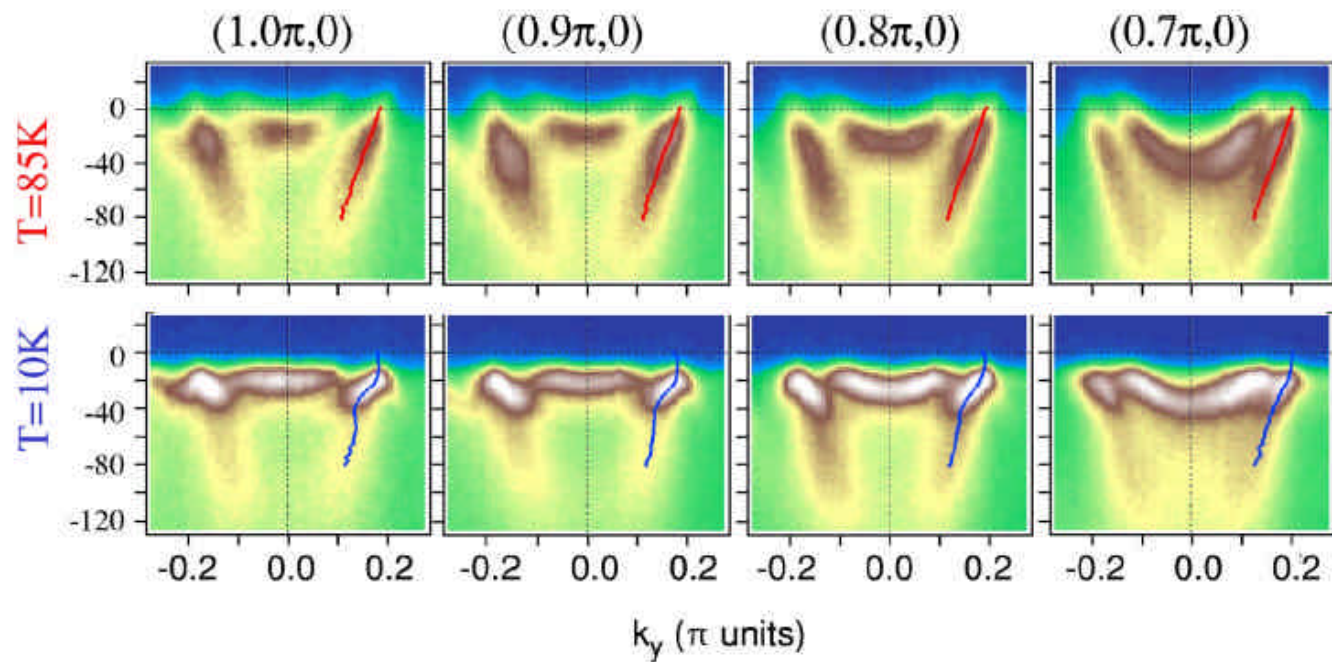
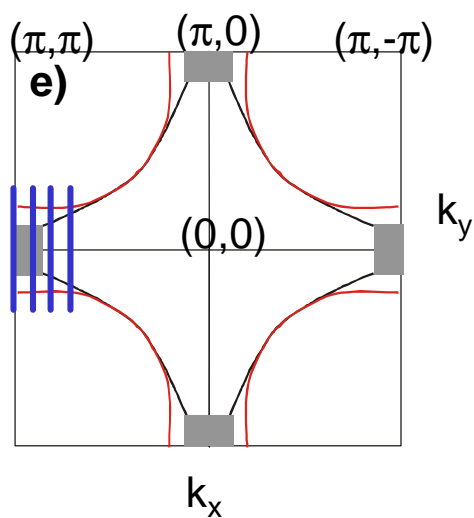
## Mass-renormalized electronic excitations at $(\pi,0)$ in the superconducting state of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

A. D. Gromko,<sup>1</sup> A. V. Fedorov,<sup>1,2</sup> Y.-D. Chuang,<sup>1,2</sup> J. D. Koralek,<sup>1</sup> Y. Aiura,<sup>3</sup> Y. Yamaguchi,<sup>3</sup> K. Oka,<sup>3</sup> Yoichi Ando,<sup>4</sup> and D. S. Dessau<sup>1</sup>

Kinks are strongly  $k$ -dependent.

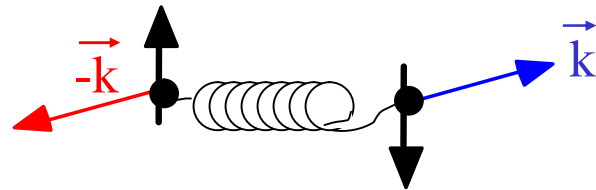
Kinks are temperature-dependent (strong below  $T_c$ ).

Difficult for phonons? Magnetic interactions instead?

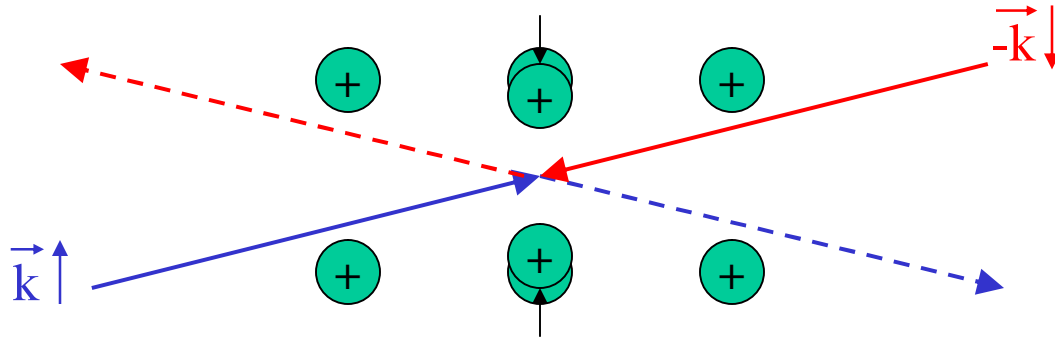


# Reason for SC - formation of Cooper Pairs (two electrons form a Boson) Pairs condense into macroscopic quantum SC state

## Cooper Pair

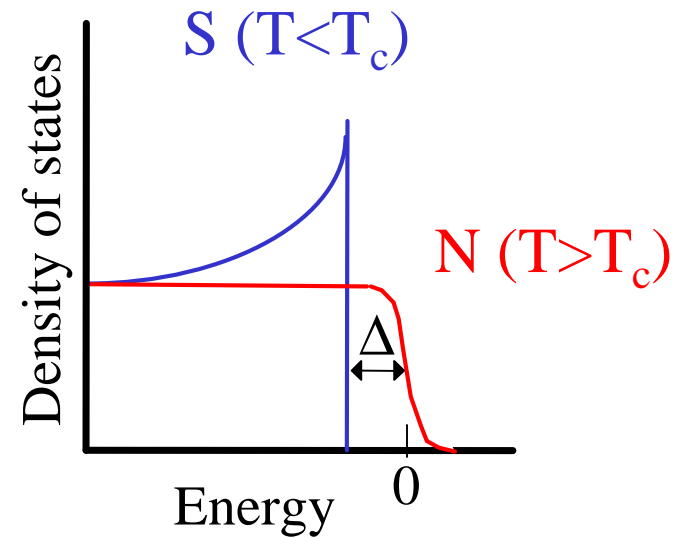
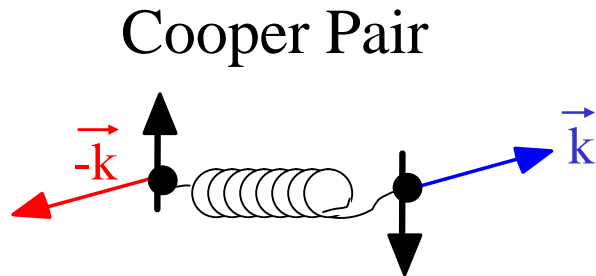


Conventional SC - pairing mediated by electron-phonon interaction



# The superconducting gap ?

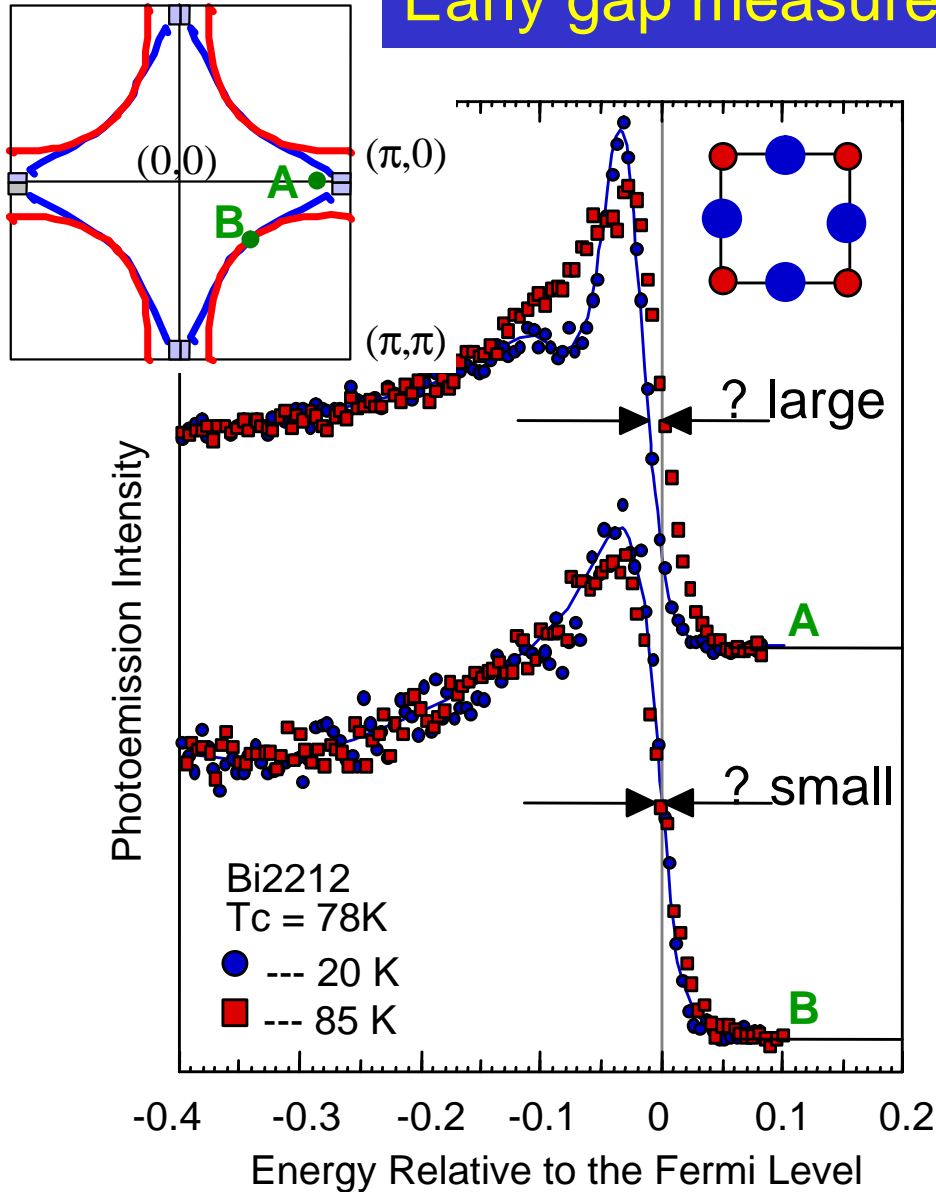
Energy to remove an electron from system - 1/2 of binding energy of the pair



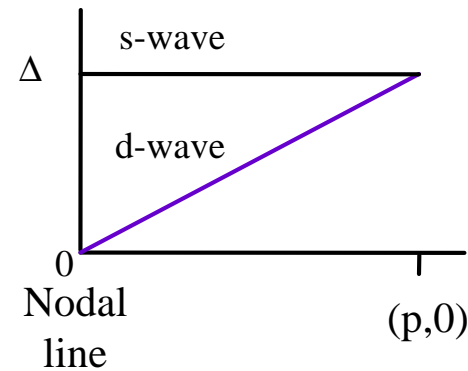
Conventional SCs:  $T_c \sim 0-30\text{K}$ ,  $\Delta \sim 1-2\text{meV}$

HTSCs:  $T_c \sim 100\text{K}$ ,  $\Delta \sim 20-40\text{meV}$

# Early gap measurements on HTSCs



Gap magnitude maximal at  $(p,0)$ , minimal or zero along  $(0,0)$ - $(p,p)$  “nodal line.”  
 -->  $d_{x^2-y^2}$  symmetry order parameter



Famous peak-dip-hump structure at  $(p,0)$ .  
 --> interaction with some mode?

# Superconducting order parameter symmetry

SC gap ? = magnitude of order parameter. Varies as a function of k in a d-wave SC

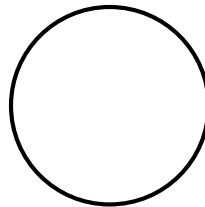
$$\Psi(r_1, \sigma_1; r_2, \sigma_2) = \psi(\text{orbital}) \cdot \chi(\text{spin})$$

Antisymmetric under exchange

$\chi(\text{spin})$  : known to be a singlet ( $S=0$ )  $\downarrow\uparrow$

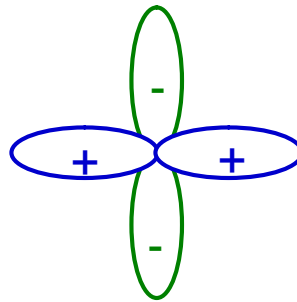
$S = 0, l = 0$

-- s-wave superconductor  
(conventional SC)

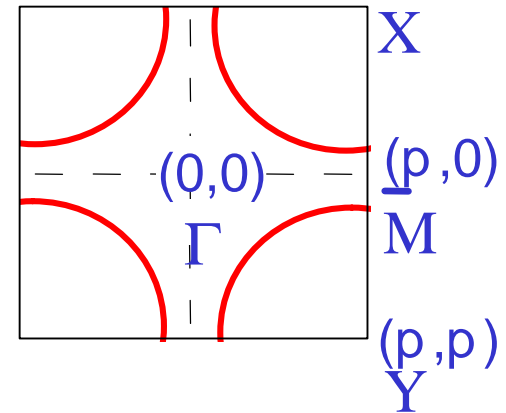


$S = 0, l = 2$

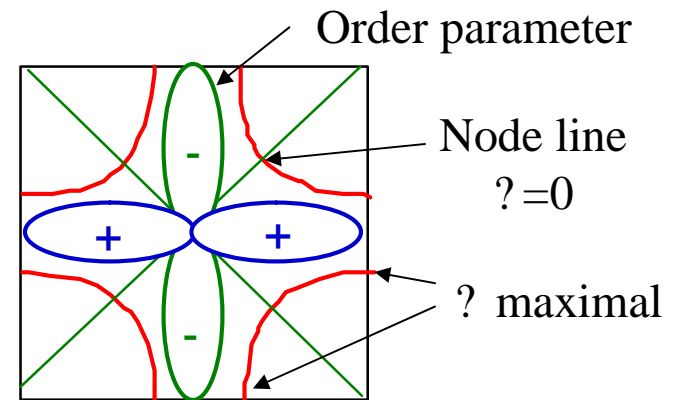
-- d-wave superconductor  
(HTSCs - pretty sure)



## Hole-like Fermi Surface



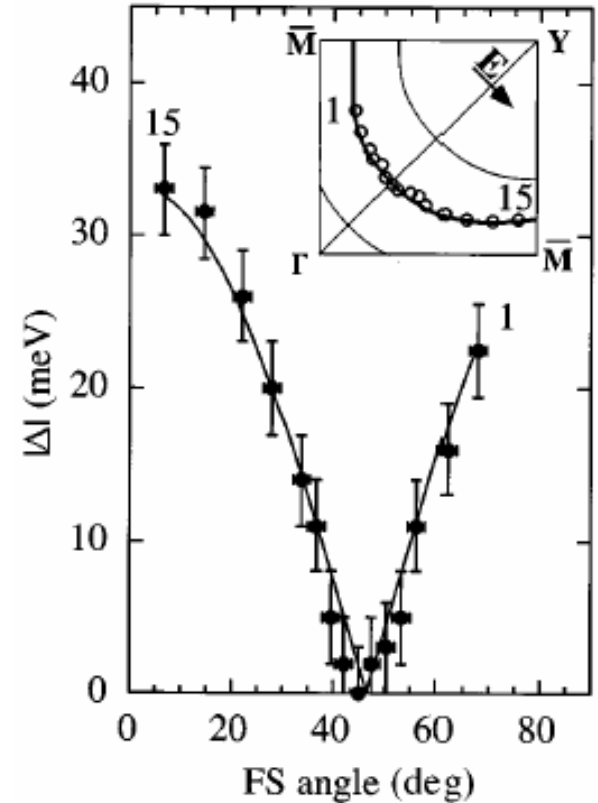
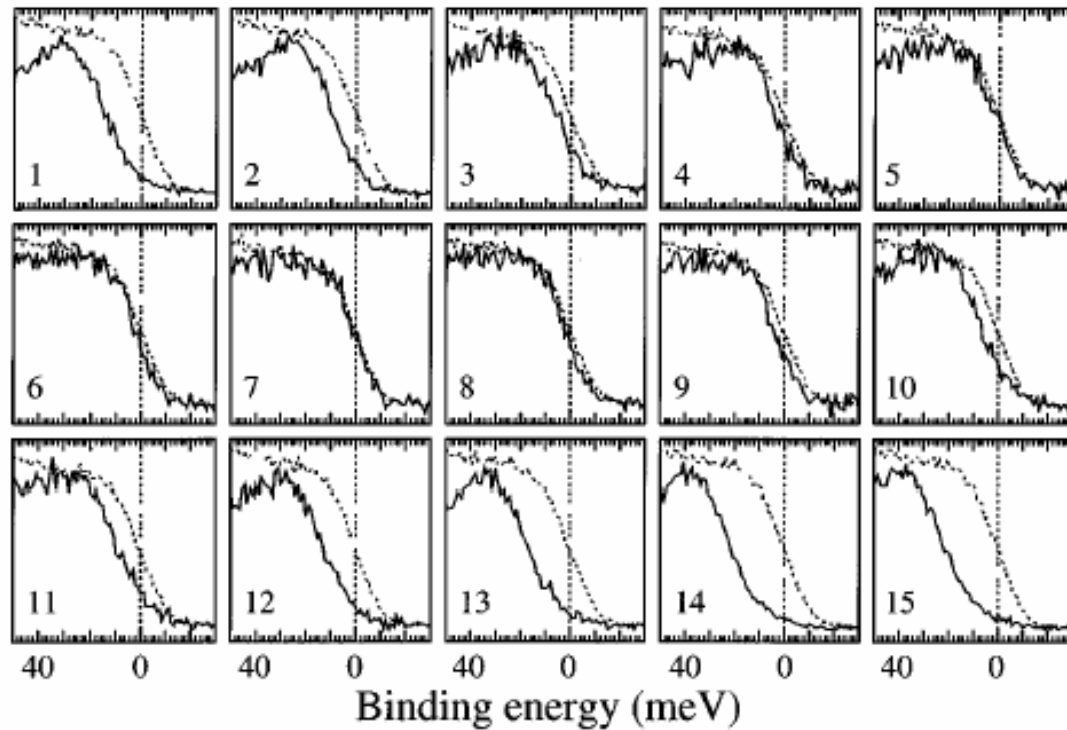
## d-wave SC gap - maximal near (p,0)



Z-X Shen, D.S. Dessau et al,  
PRL **70**, 1553 (1993).

# Angle-resolved photoemission spectroscopy study of the superconducting gap anisotropy in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$

H. Ding, M.R. Norman, J.C. Campuzano, et al.

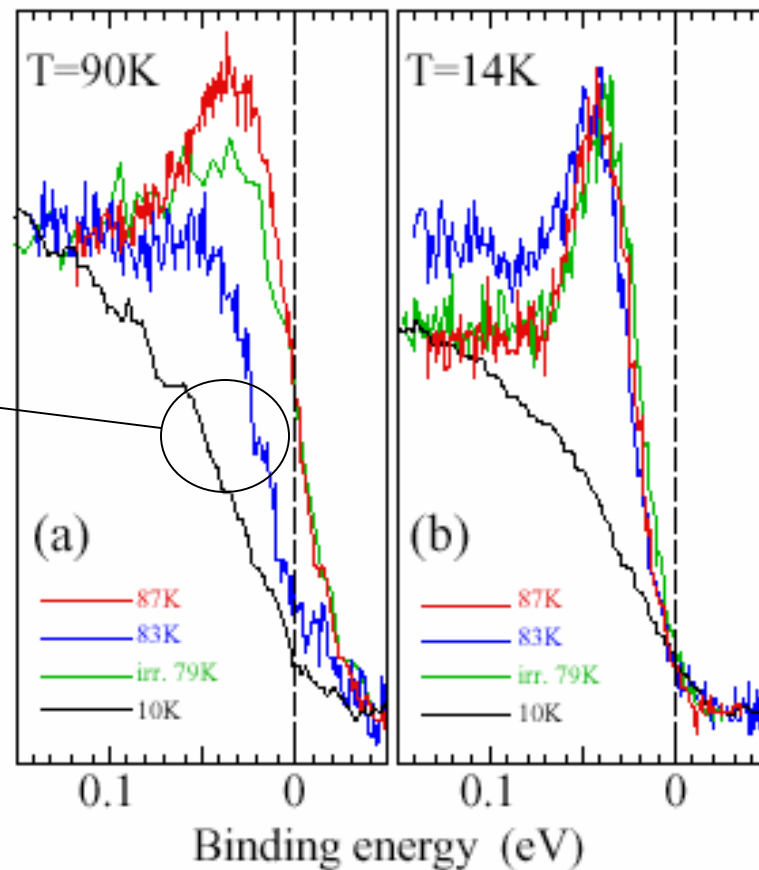


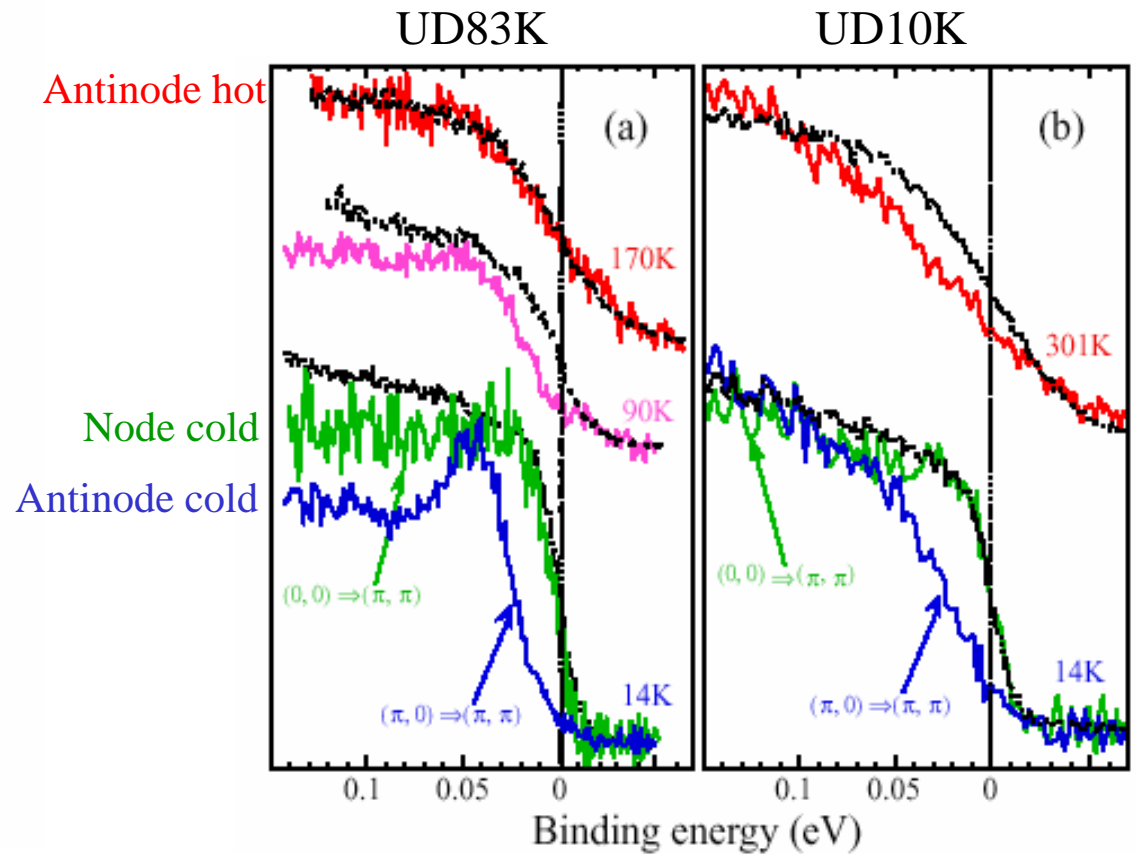
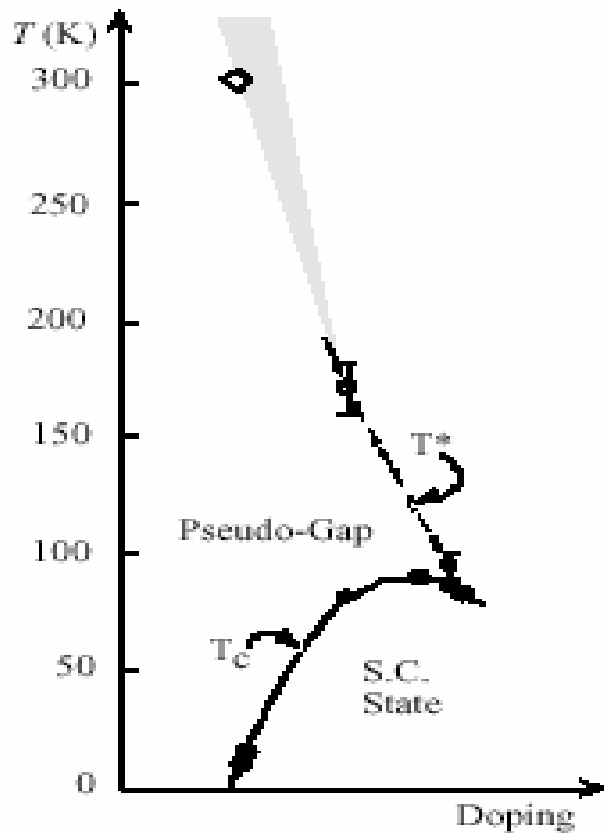
# Spectroscopic evidence for a pseudogap in the normal state of underdoped high $T_c$ superconductors

*H. Ding et al. Nature 382, 51 (1996).*

antinode

UD samples  
“gapped” even  
above  $T_c$ .





Thought to exist between  $T_c$  and  $T^*$  for UD samples.

Similar magnitude as SC gap.

Similar  $k$ -dependence as SC gap (d-wave).

Obtained from leading edge analysis.

Also

*M. Norman et al, Nature 392, 157(1998).*

*D.S. Marshall et al, PRL 76, 4841 (1996).*

*A.G. Loeser et al. Science 273, 325 (1996).*

