



# site occupancy determination by resonant elastic X-ray scattering

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# name change: AXRD → REXS



- diffraction measurements at various incident X-ray energies near an absorption edge
- different names for the same technique
  - **anomalous X-ray diffraction**
  - resonant anomalous X-ray diffraction
  - **resonant elastic X-ray scattering (REXS)**

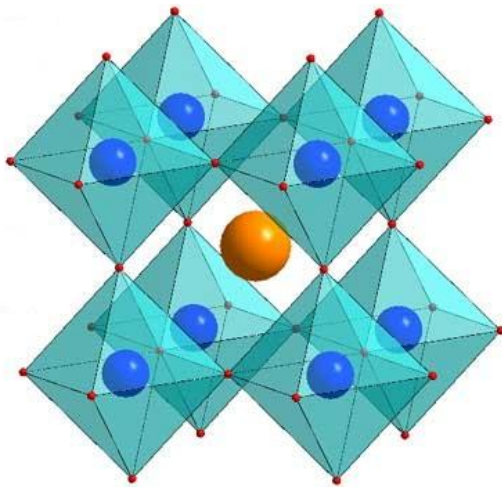


1. motivation: why do we care?
2. technique: how does this work?
3. design experiments: what to consider?

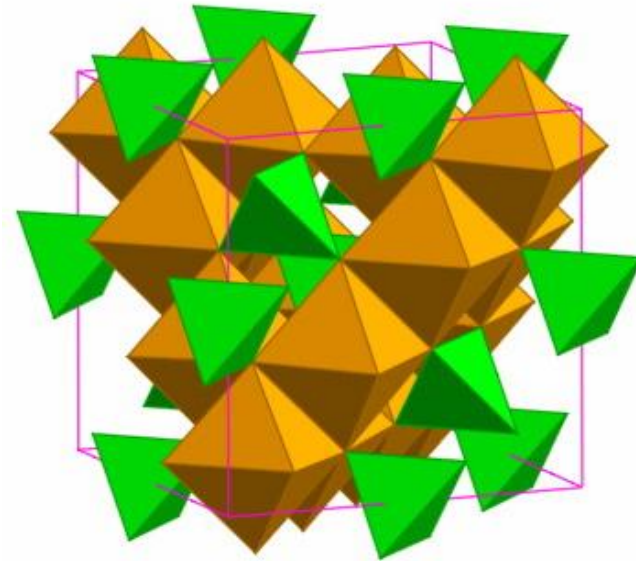
# importance of site occupancy



- materials property depends on site occupancies
- multiple sites, multiple cations/anions



perovskite:  $ABO_3$

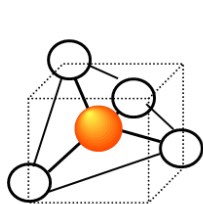
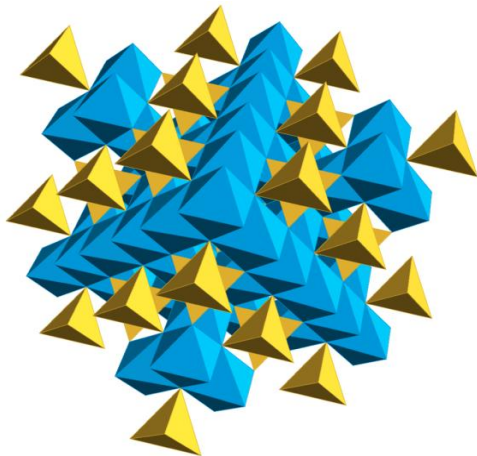


spinel:  $A_2BO_4$

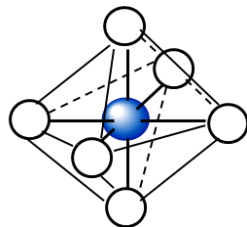
# anti-site defects in $A_2BO_4$ spinel



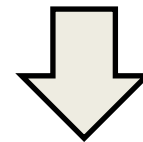
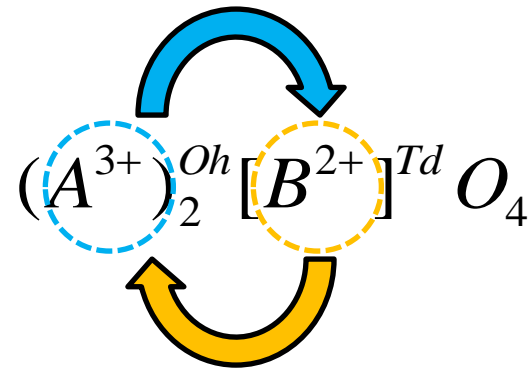
- electronic conductivity of spinels depends on structure
- *intrinsic* anti-site defects created by cross-substitution



Tetrahedral



Octahedral



$B_{Oh}^{2+}$  acceptor states      donor states       $A_{Td}^{3+}$

# attributes of an ideal technique



- **chemical selectivity:** distinguish elements with similar atomic numbers
- **site selectivity:**
  - site A *vs.* site B
  - substitution *vs.* interstitial
- **common techniques**
  - extended X-ray absorption fine structures (EXAFS)
  - diffraction + Rietveld refinement
    - X-ray diffraction
    - neutron diffraction



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# REXS: chemical selectivity

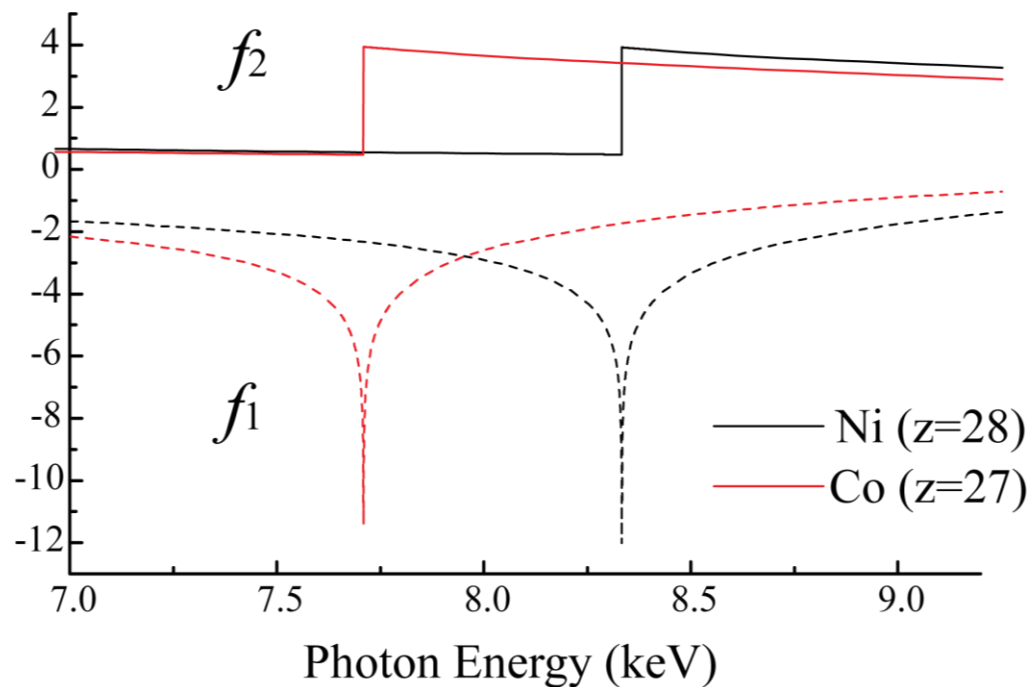


- offers both chemical and site selectivities

$$I(E) \propto |F_{hkl}|^2 \quad F_{hkl} = \sum_i x_i f_i(q, E) e^{2\pi i(hx+ky+lz)}$$

$$f = f_o(q) + f_1(E) + if_2(E)$$

chemical  
selectivity





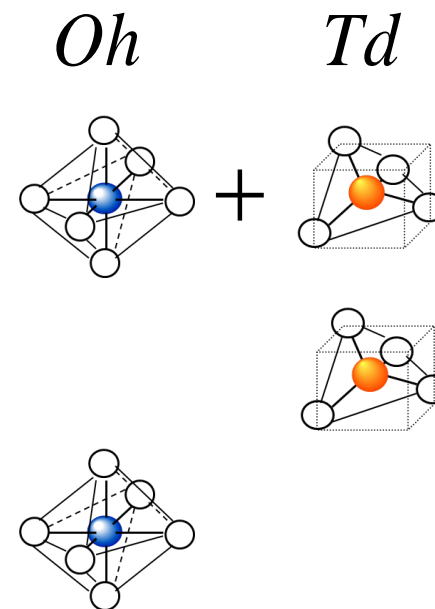
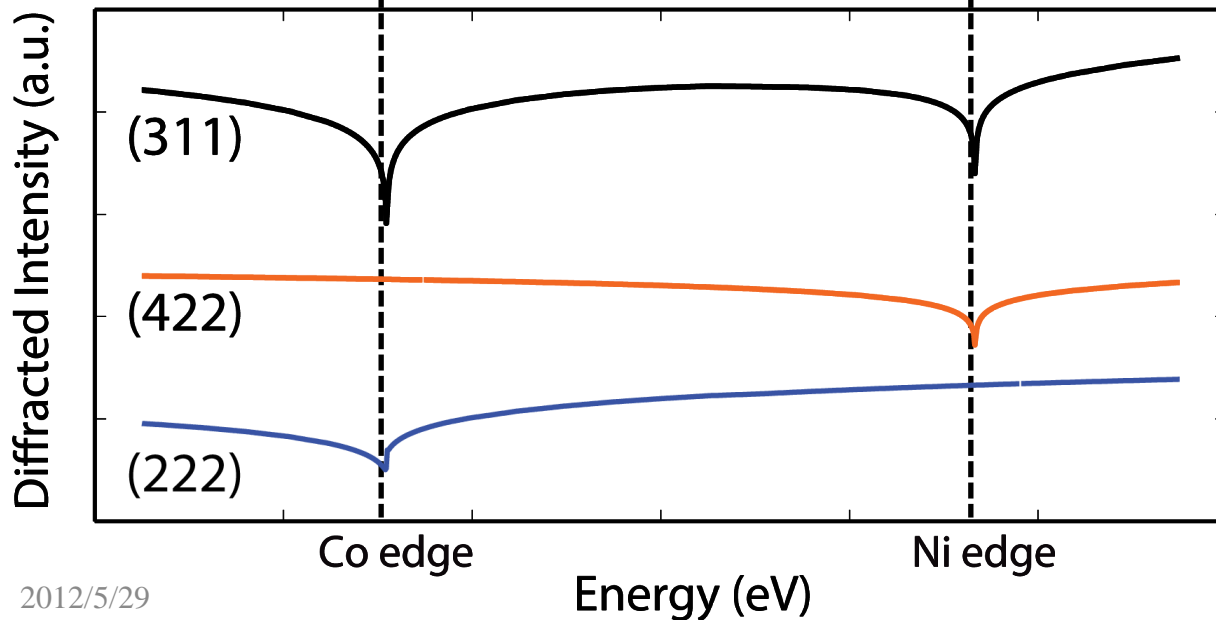
# REXS: site selectivity



- offers both chemical and site selectivities

$$F_{hkl} = \sum_i x_i f_i(q, E) \cdot e^{2\pi i(hx+ky+lz)}$$

cation site  
selectivity



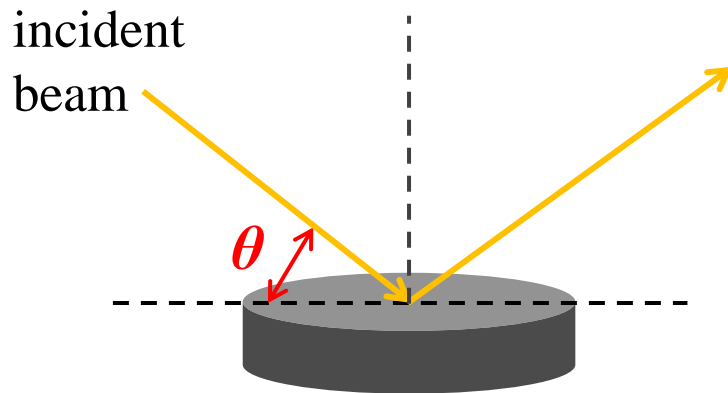
# REXS: multiple-energy scans



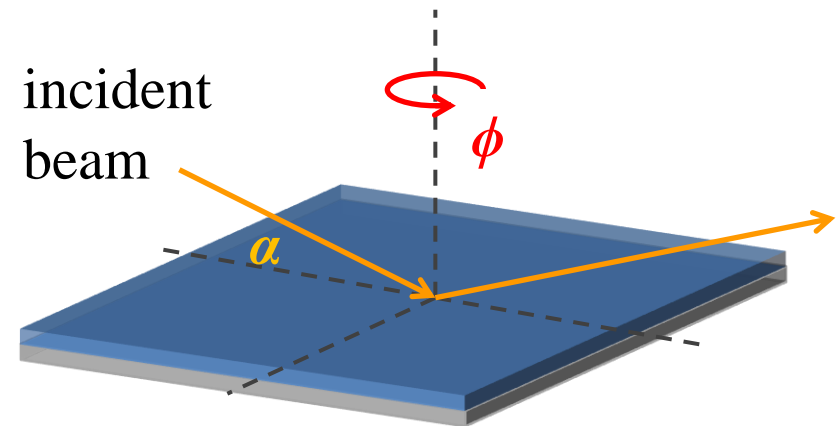
$$I(E) \propto |F_{hkl}|^2$$

$$F_{hkl} = \sum_i x_i f_i(q, E) \cdot e^{2\pi i(hx+ky+lz)}$$

## Powder



## Thin films



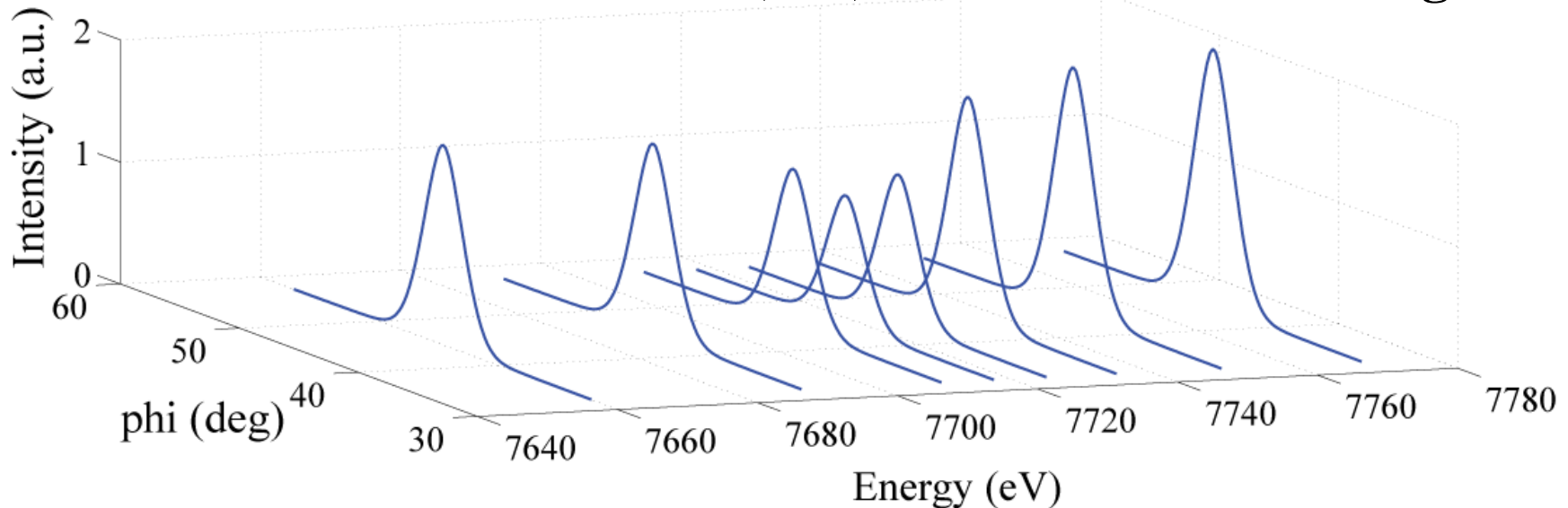
# REXS: multiple-energy scans



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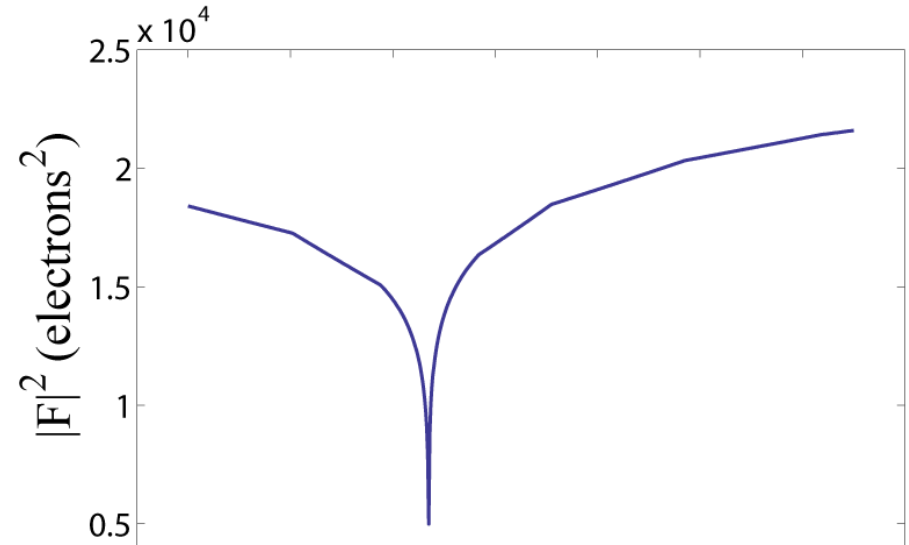
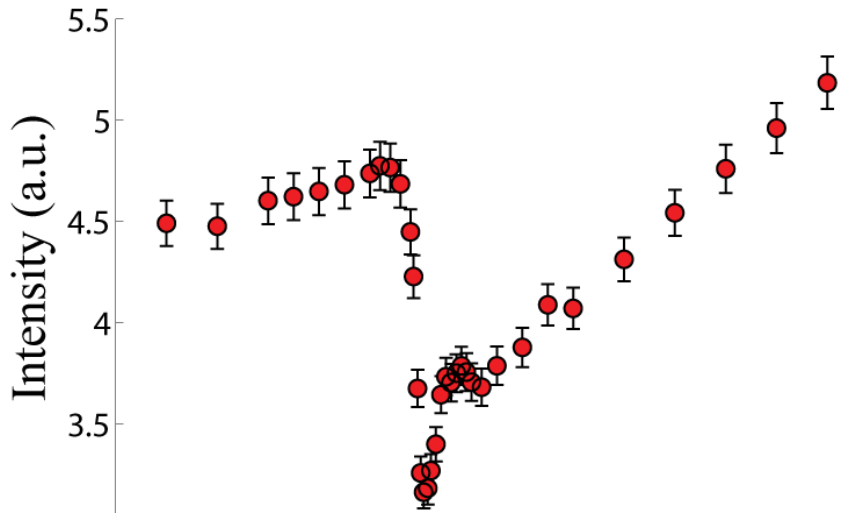
|  
**occupancy**

**(422) reflections near Co edge**



Y. Shi *et al.* manuscript in preparation.

# experiment vs. simulation: $\text{Cr}_2\text{MnO}_4$



○  $I_{obs}(E) = C \cdot I_{calc}(E, x)$

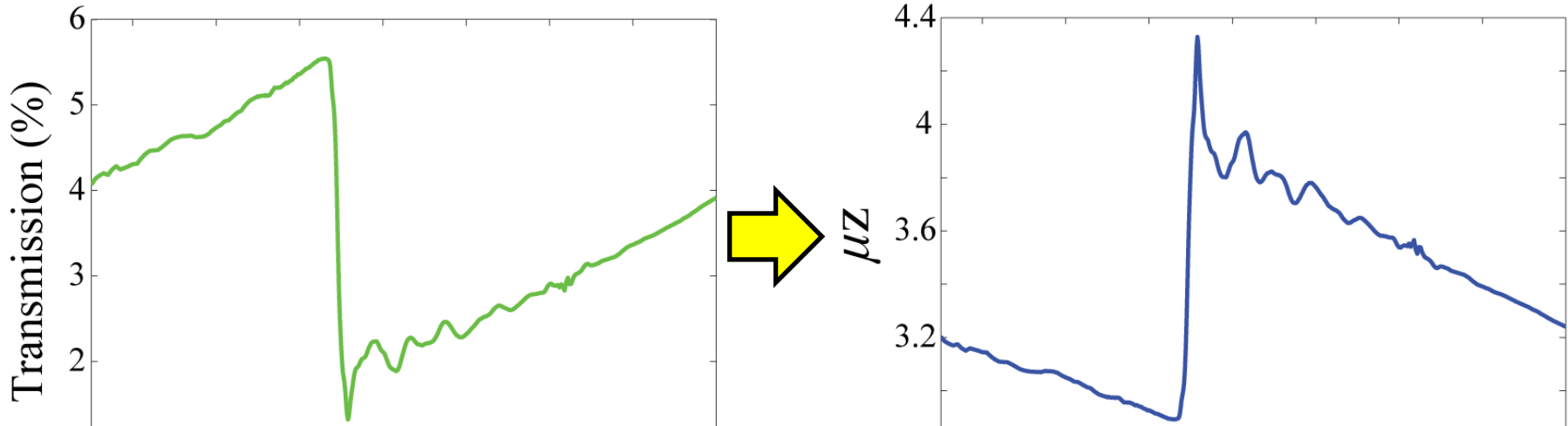
$f_{calc}(q, E) = f_o(q) + f_{1,exp}(E) + f_{2,exp}(E)$

obtain  $f_1$  and  $f_2$  with fine features

# measuring X-ray abs. spectroscopy



Beer-Lambert's Law  $\text{transmission} = \frac{I}{I_o} = \exp(-\mu \cdot z_{\text{sample}})$

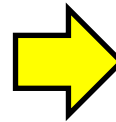
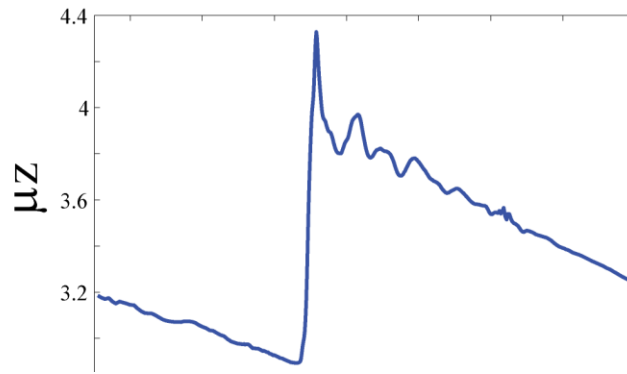


- powder samples: transmission XAS
- thin films: fluorescence XAS

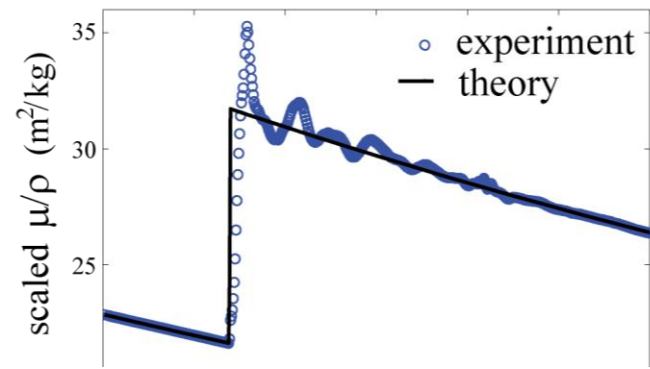
scaling:  $\mu z \rightarrow \mu/\rho \rightarrow f_2$



measured  $\mu z$



scale  $\mu$  to  
theoretical  $\mu/\rho$



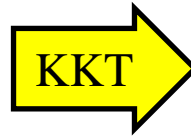
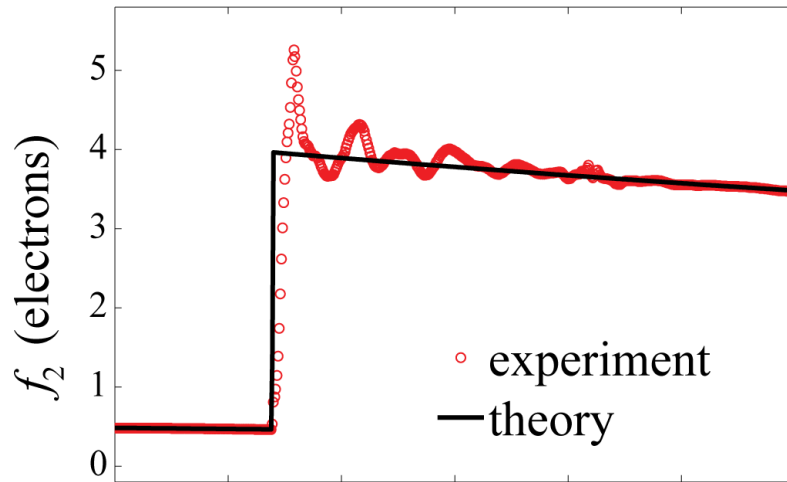
- calculate  $f_2$  from mass. abs. coeff.

$$\left(\frac{\mu}{\rho}\right)_{\text{element}} = \frac{2f_{2,\text{element}}r_e\lambda}{Am_u}$$

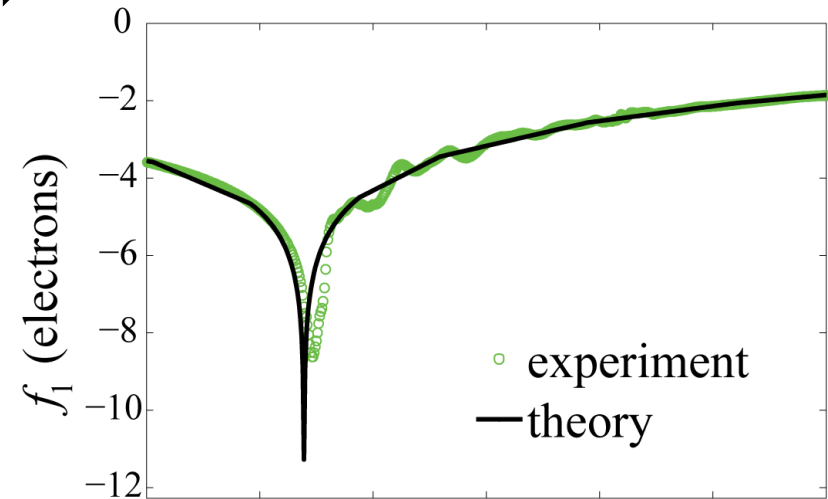
# converting $f_2$ to $f_1$



imaginary part:  $f_2$

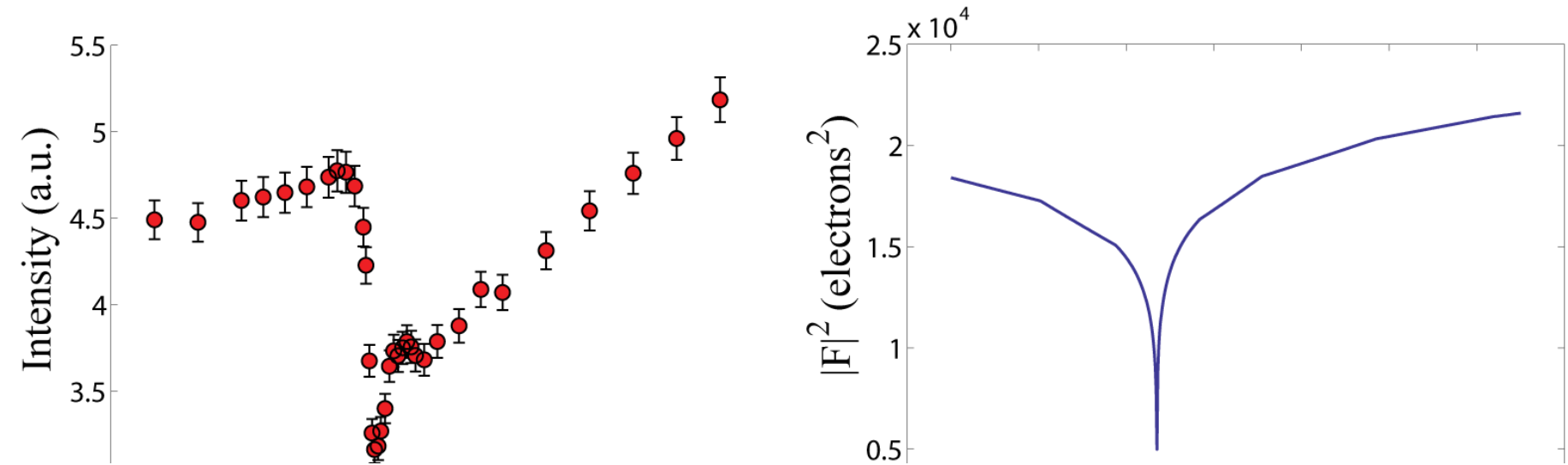


real part:  $f_1$



- Kramers-Krönig transform (KKT): 
$$f_1(E_o) = \frac{2}{\pi} \int_0^{\infty} \frac{E \cdot f_2(E)}{E_o^2 - E^2} dE$$
- near edge: resonant features
- away from edge: good agreement

# experiment vs. simulation: $\text{Cr}_2\text{MnO}_4$



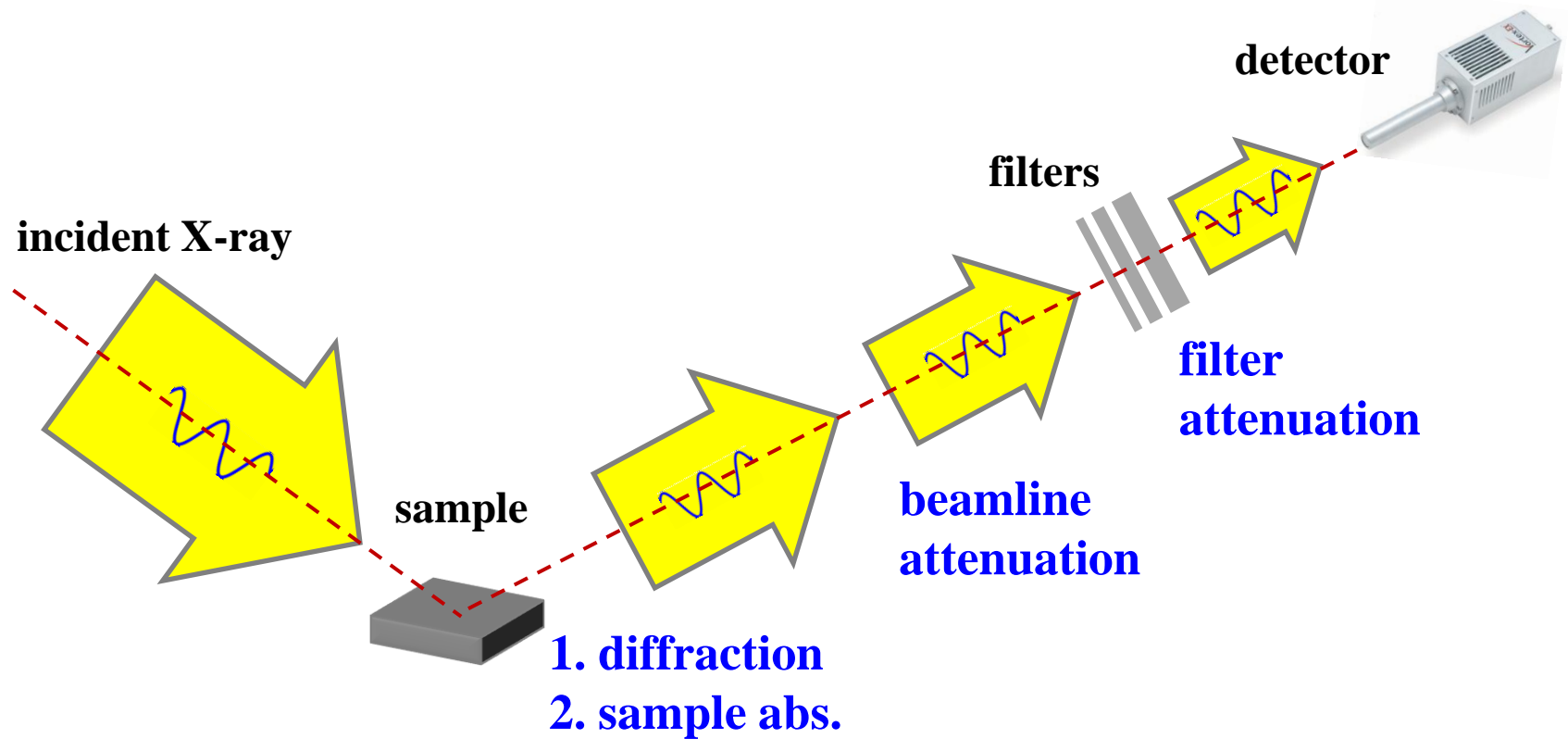
- evident differences: slope, step, and near-edge fine features

- $I_{obs}(E) = C \cdot I_{calc}(E, x) \cdot A(E)$

correct for absorptions



# absorptions in the experiment

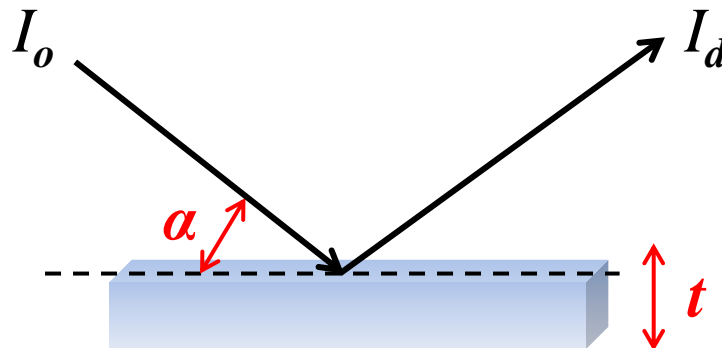


- size of the arrows symbolizes light intensity
- filter attenuation: can be measured
- beamline attenuation: need control samples

# correct sample absorption



- calculate absorption in the sample
- tricky because *both* resonant diffraction and strong absorption features are near the edge



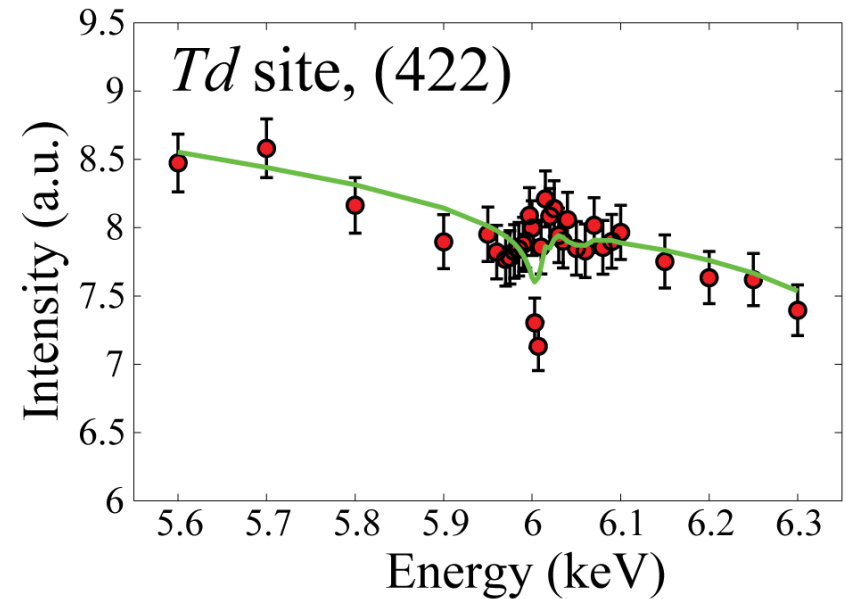
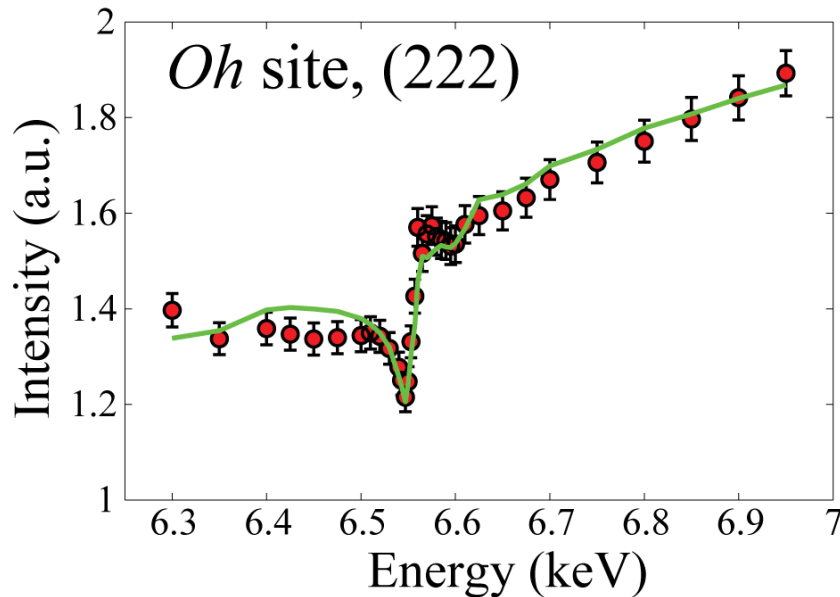
**Powder**

$$\frac{I_d}{I_o} \propto \frac{1}{\mu_{(E)}}$$

**Thin films**

$$\frac{I_d}{I_o} \propto \frac{1 - \exp(-2\mu_{(E)}t / \sin \alpha_{(E)})}{2\mu_{(E)}}$$

# fit calculation to experiment



- good agreement between data and fit
- capture the near-edge features and the slope



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# practical considerations

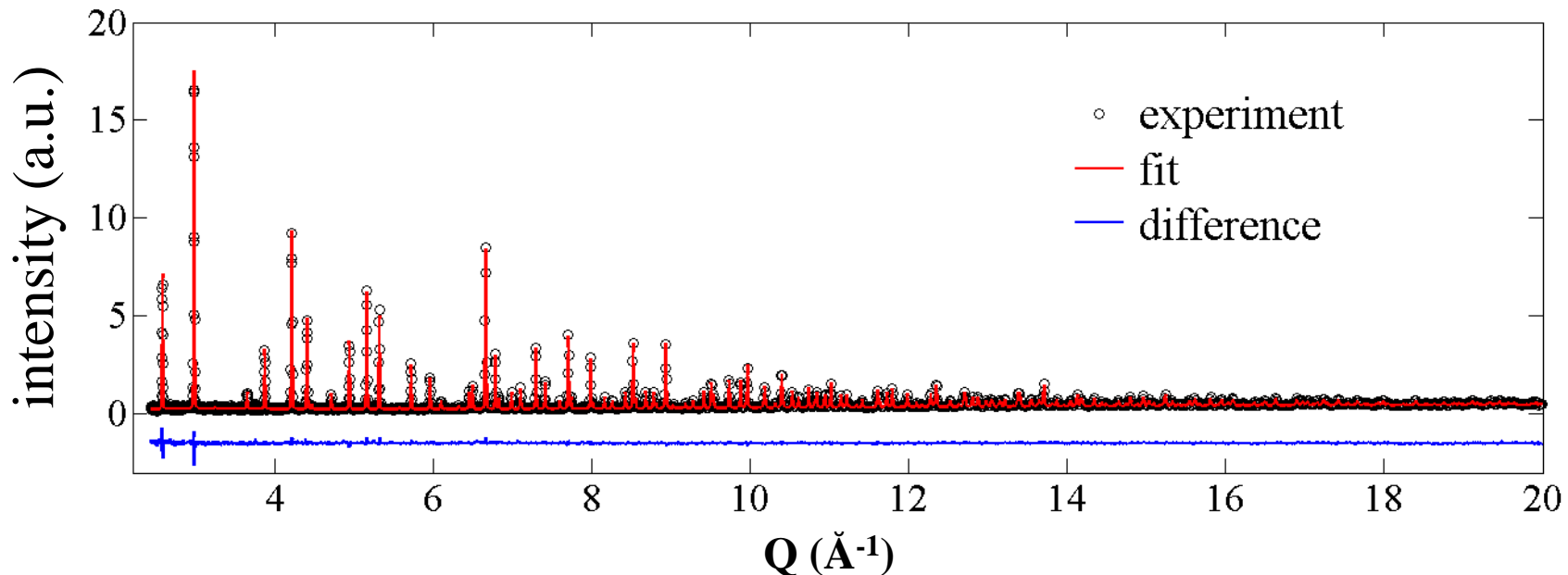


- fraction site occupancy in multiple cation and/or multiple site
- energy compatibility with beamlines
- forms of samples
  - single phase with known composition
  - polycrystalline films or nanocrystals: very difficult
  - powder/bulk ceramic: OK
  - textured thin films/single crystals: the best
  - surfaces: good?
- is this the appropriate technique?

# powder sample: co-refinement of XRD and neutron data



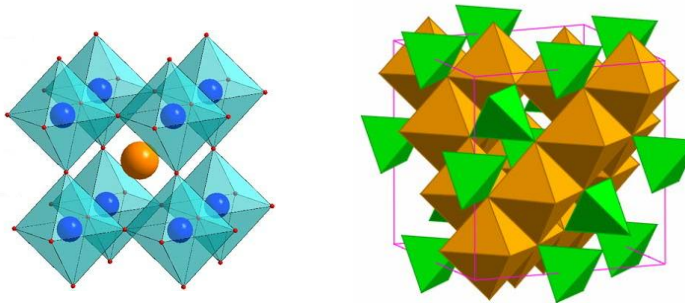
- material: Li doped  $\text{Cr}_2\text{MnO}_4$  powder
- refine cation site occupancy:  $(\text{Cr}_{1-x-y}\text{Mn}_x\text{Li}_y)_2^{\text{Oh}}[\text{Mn}_{1-z}\text{Li}_z]^{\text{Td}}\text{O}_4$
- neutron diffraction done at Oak Ridge National Lab
- complimentary XRD at SSRL



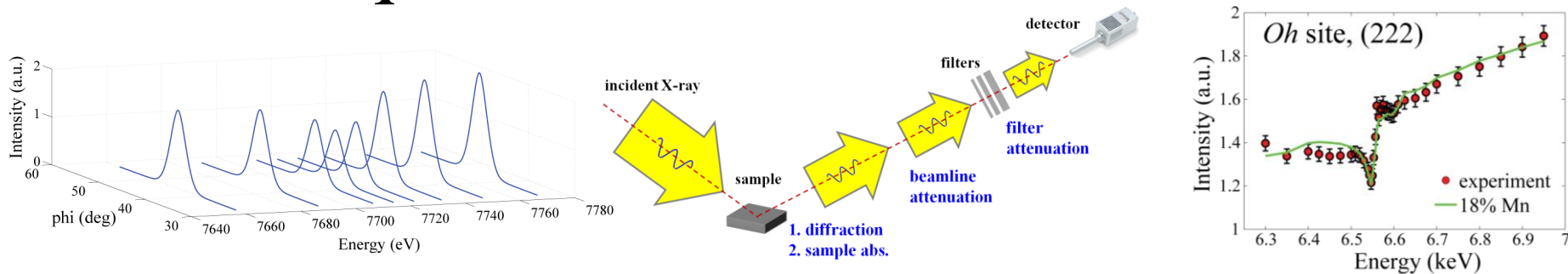
# summary



## 1. motivation



## 2. technique



## 3. design experiments

- sample form
- energy compatibility

# acknowledgment



- Toney group at
- Salleo Group at
- collaborators at
- beamline staff at
- funding from



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**ENERGY**

thank you for the attention