

# Measurements of Short Bunches at SPPS and E-164X

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# OUTLINE

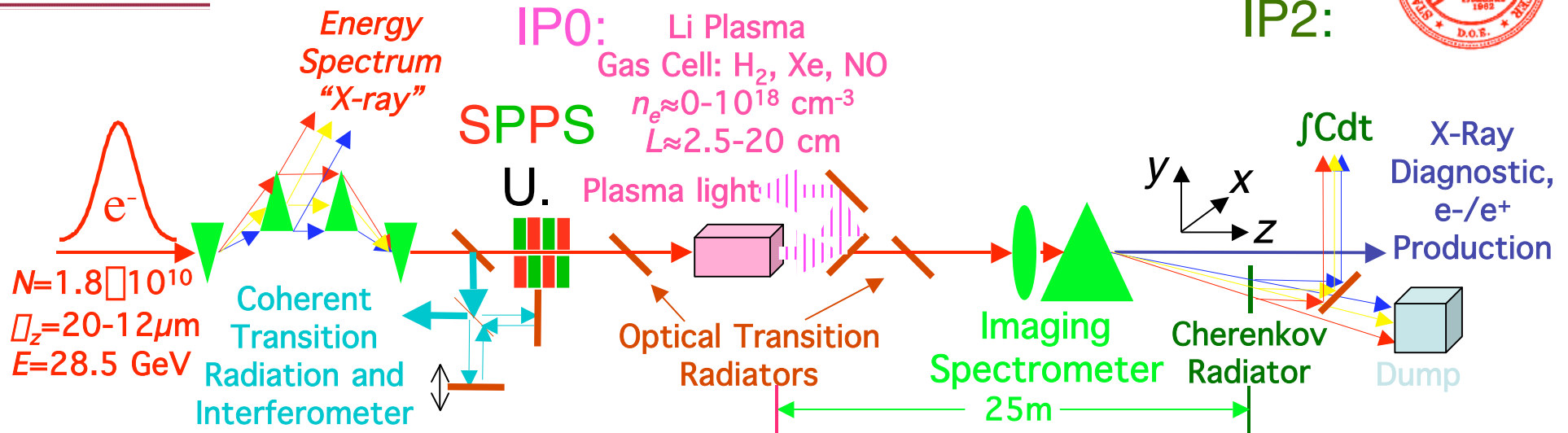


- Motivation
- CTR Interferometry\*
- Bunch energy spectrum measurements
- Application to E-164X
- Conclusions

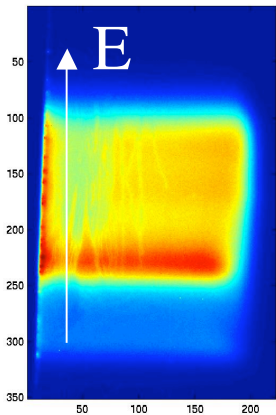
\*C. Settakorn, PhD thesis, Stanford (2001).

- Length of SLAC ultra-short bunches was never measured!
- In E-164X plasma wakefield acceleration (PWFA) experiment, the accelerating gradient increases as  $1/\lambda_z^2$  with matching plasma density increasing as  $1/\lambda_z$
- Bunch incoming energy spectrum and CTR energy varies significantly from bunch to bunch (especially at 1 Hz rep. rate)
- Outcome of E-164X ...

# EXPERIMENTAL SET UP

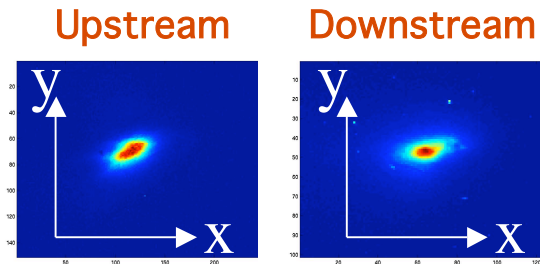


• X-ray Chicane



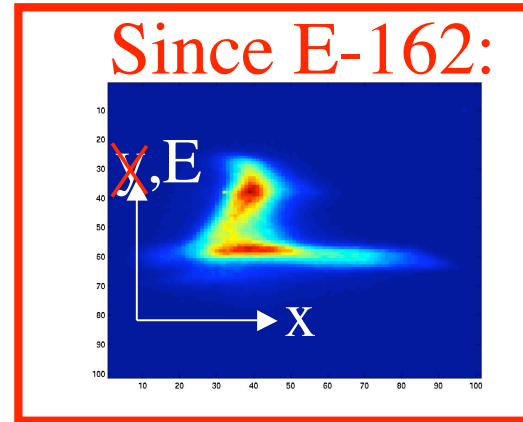
-Energy resolution  $\approx 60$  MeV

• Optical Transition Radiation (OTR)



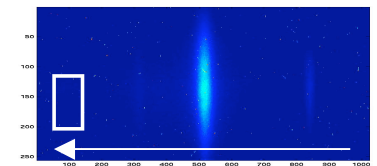
-1:1 imaging, spatial resolution  $\approx 9 \mu\text{m}$

• Cherenkov (aerogel)



- Spatial resolution  $\approx 100 \mu\text{m}$   
- Energy resolution  $\approx 30$  MeV

• Plasma Light



- Transition Radiation (TR) becomes Coherent (CTR) for  $\lambda > \lambda_z$ , with intensity  $\approx N^2/\lambda_z$ ,  $N$  the number of  $e^-$ /bunch of length  $\lambda_z$
- CTR spectrum extends from  $\lambda_z < \lambda < \lambda_z$ , (i.e., broad spectrum in the IR/FIR)
- CTR spectrum amplitude given by the bunch form factor  $f(\lambda)$ , i.e, the Fourier transform of the longitudinal charge distribution squared (neglecting transverse variations, in the forward direction of observation).

$$I_{total}(\lambda) \approx NI_e(\lambda) \left[ 1 + (N-1)f(\lambda)^2 \right]$$

$\ll$  for  $\lambda < 2\pi c/\lambda_z$

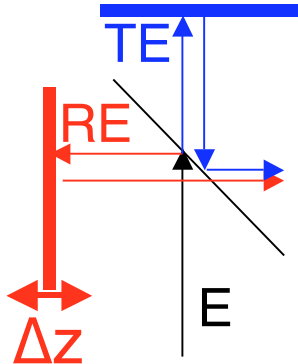
$I_e(\lambda) = |E(\lambda)|^2$ , the TR for a single electron

$$f(\lambda)^2 = e^{(i\lambda\lambda_z/c)^2} \text{ for } E_r(z) \quad n(z) = \frac{1}{\sqrt{2\lambda\lambda_z}} e^{-z^2/2\lambda_z^2}$$

(Gaussian bunch)

- CTR carries longitudinal bunch shape information at long  $\lambda$ 's

- Radiation field in the 2 arms of the interferometer with a time of flight difference  $\Delta t = 2\Delta z/c$ :



$$E_{ref.} = RTE(t)$$

+

$$E_{var.} = TRE(t + 2\Delta z/c)$$

$T, R$  transmission and reflection coeff. of beam splitter  
 Note:  $T=T(\Delta z), R=R(\Delta z)$  !

- Intensity  $I_D = (E_{ref.} + E_{var.})^2$  on autocorrelator detector:

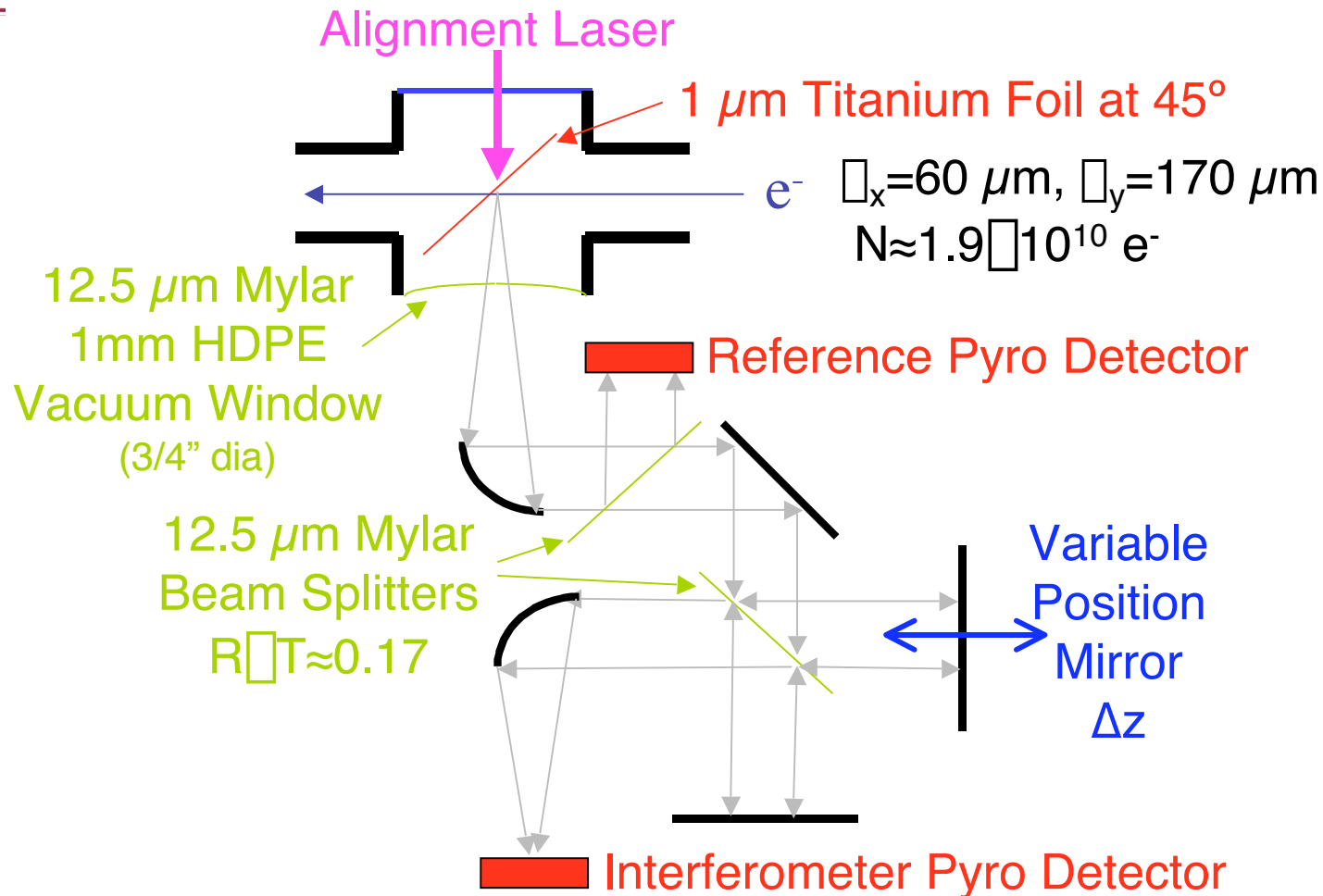
$$I_D(t; \Delta z) = \underbrace{2\Delta z |RTE(t)|^2}_{\text{Background}} dt + \underbrace{2\Delta z |RT|^2 E(t)E(t + 2\Delta z/c)}_{\text{Interferogram/autocorrelation}} dt$$

# USC INTERFEROMETER/ AUTOCORRELATOR



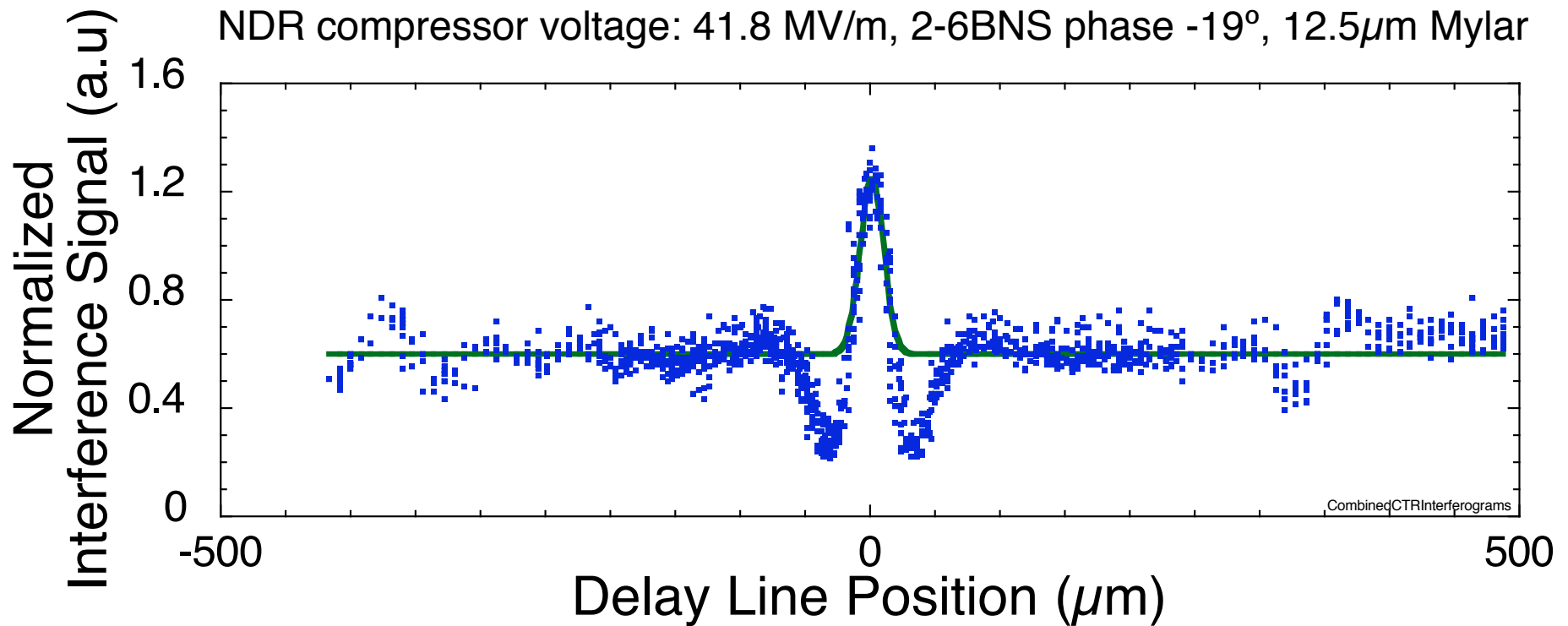
- For each  $\Delta t$  or  $\Delta z$ , measure the energy:  $S_D(\Delta z) = \iint I_D(t; \Delta z) dt ds$
- Autocorrelation signal characteristics:
  - Symmetric (even if the bunch shape is not)
  - Background="2", peak="2"+"2", contrast of 2
  - Extends to long wavelengths, i.e., to long delays (CTR)
  - FFT(interferogram) => bunch spectrum
  - requires multiple (similar) bunches
- Pros and cons of CTR Interferometry
  - Simple and inexpensive (<\$10k)
  - No sophisticated timing required
  - Symmetric trace
  - Multi-bunch measurement
  - Requires knowledge of broadband response of the entire system

# CTR MICHELSON INTERFEROMETER



- Interference signal normalized to the reference signal
- Motion resolution  $\Delta z_{\min} = 1 \mu\text{m}$  or  $\approx 14 \text{ fs}$  (round trip)
- Mylar:  $R \approx 22\%$ ,  $T \approx 78\%$ ,  $RT \approx 0.17$





- Trace is symmetric (even if the bunch shape may not be)
- Peak/background ratio =2
- Large “dips” on either sides of the peak
- Modulation far from the peak



Interferometer “transmission” can be affected by: \*

(amplitude and phase)

- Water absorption in humid air
- Vacuum window size cut-off (long  $\lambda$ )
- Interferometer optics aperture (long  $\lambda$ )
- Pyro-electric detector resonances
- Beam splitter(s)/window Fabry-Perot resonances

\*C. Settakorn, PhD thesis, Stanford (2001).

Thickness  $d$

Index of refraction  $n$

Angle of incidence 45°

$$R(\varphi) = r \frac{1 - e^{i\varphi}}{1 - r^2 e^{i\varphi}}$$

$$T(\varphi) = (1 - r^2) \frac{e^{i\varphi/2}}{1 - r^2 e^{i\varphi}}$$

$$r_{\perp}(\varphi) = \frac{1 - \sqrt{2n^2 - 1}}{1 + \sqrt{2n^2 - 1}} \quad r_{\parallel}(\varphi) = \frac{n^2 - \sqrt{2n^2 - 1}}{n^2 + \sqrt{2n^2 - 1}}$$

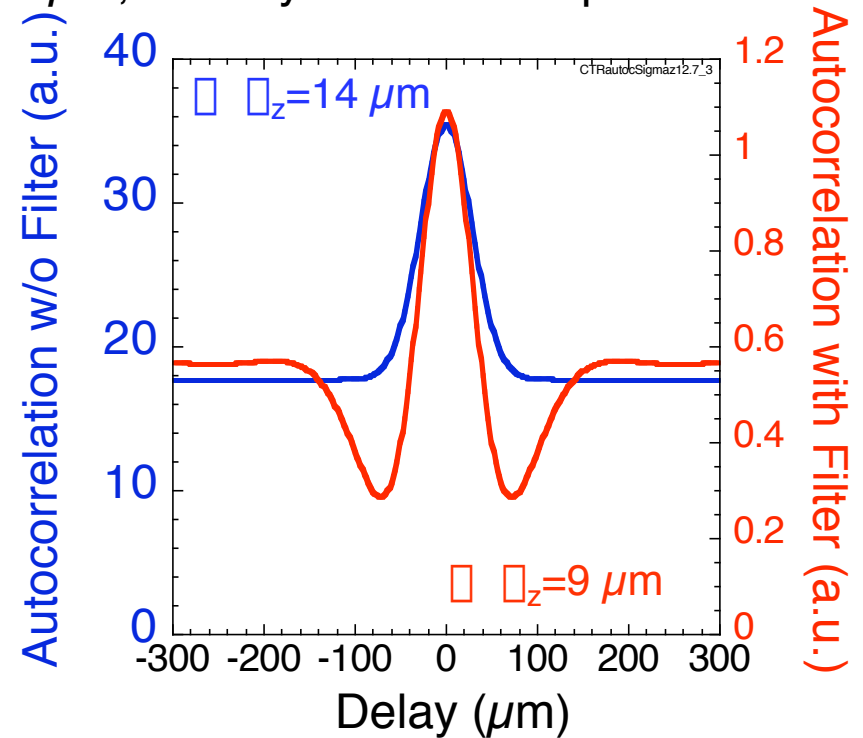
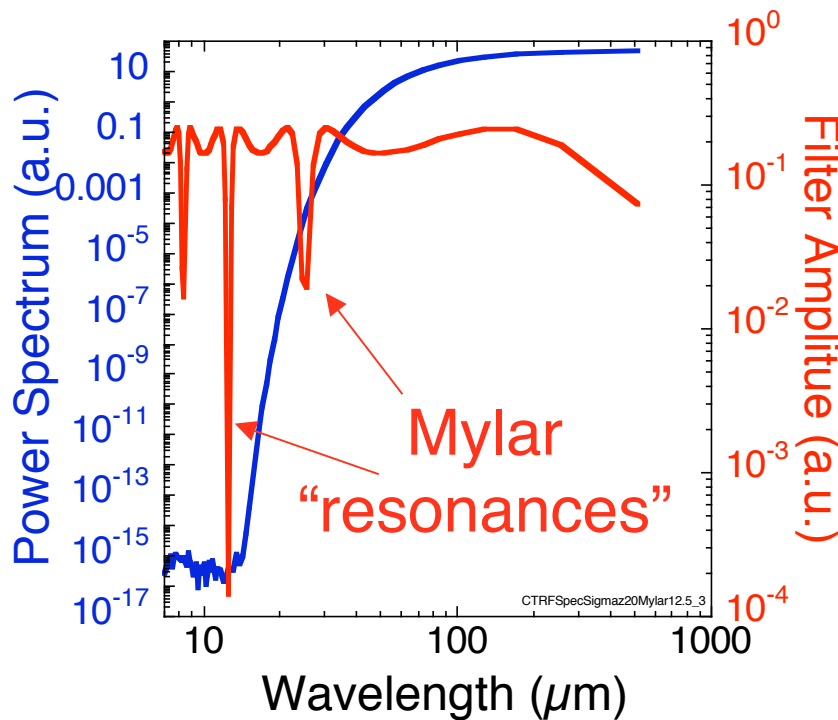
Mylar:  $n=3$ ,  $n=n(\lambda)$ ?

- Include in a simple autocorrelation calculation
- Interferometer delay  $\Delta z$  or  $\varphi \Rightarrow$  relative phase shift  $2k\Delta z$

# MYLAR FABRY-PEROT

Simple model:

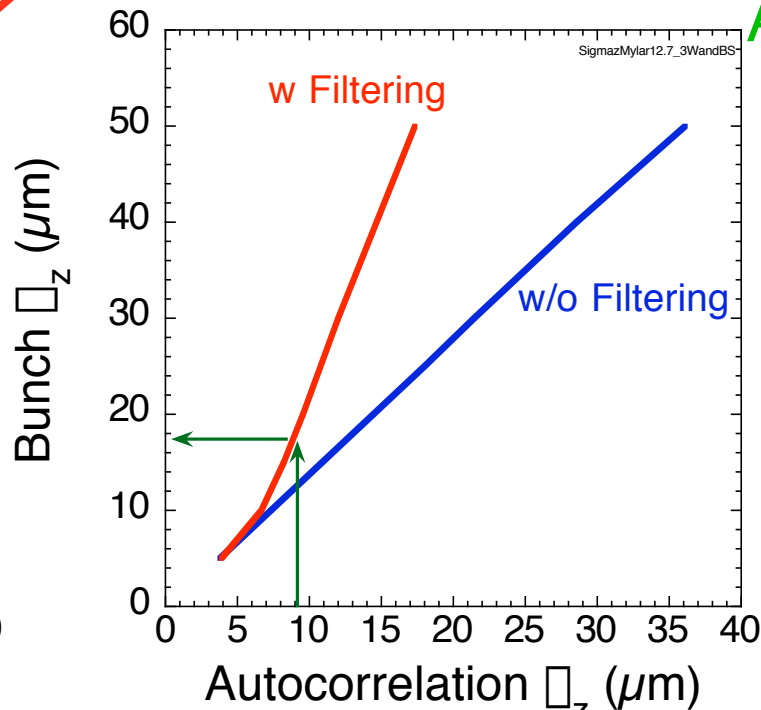
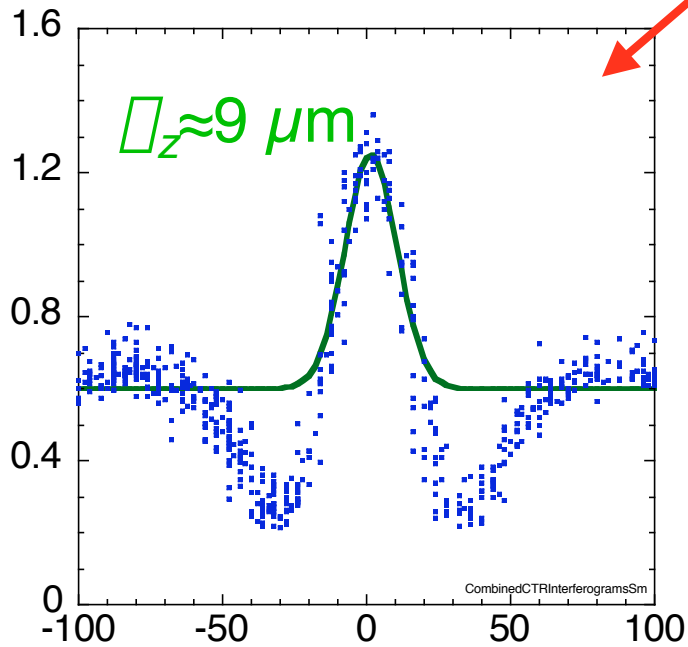
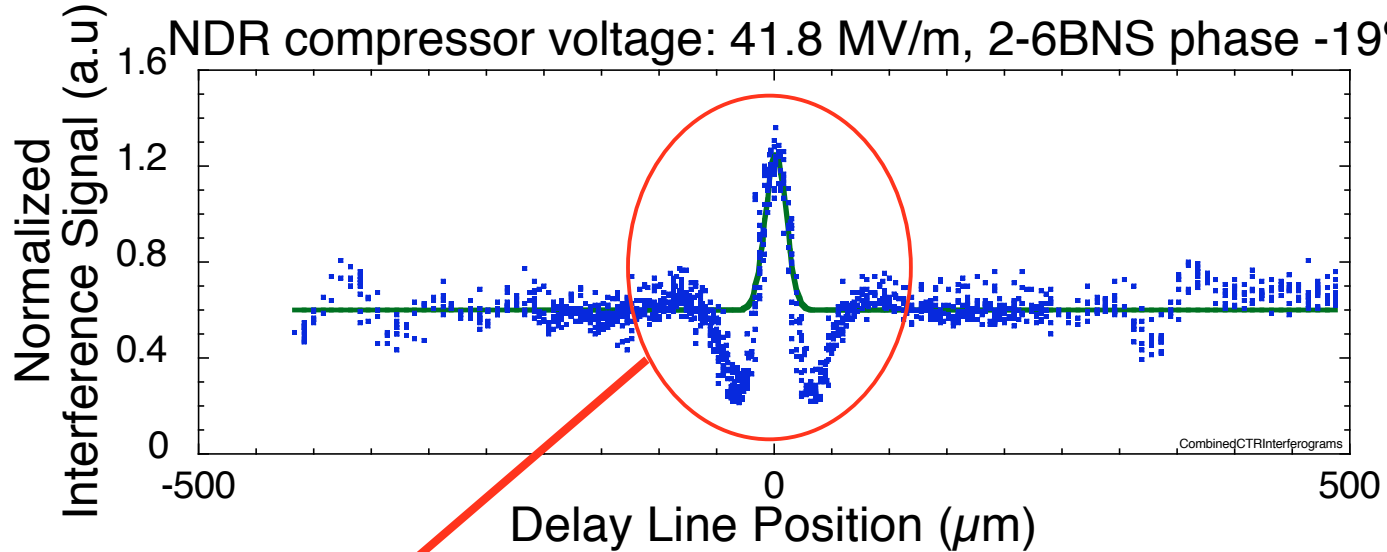
Gaussian,  $\sigma_z = 20 \mu\text{m}$ ,  $d = 12.7 \mu\text{m}$ ,  $n = 3$  Mylar window+splitters



- Fabry-Perot resonance:  $\lambda = 2d/nm$ ,  $m = 1, 2, \dots$ ,  $n = \text{index of refraction}$
- Signal attenuated by Mylar beam splitter:  $(RT)^2$
- Modulation/dips in the interferogram
- Smaller measured width:  $\sigma_{\text{Autocorrelation}} < \sigma_{\text{bunch}} !$

# CORRECTED GAUSSIAN WIDTH

NDR compressor voltage: 41.8 MV/m, 2-6BNS phase  $-19^\circ$



Autocorrelation:

$\Delta z \approx 9 \mu\text{m}$



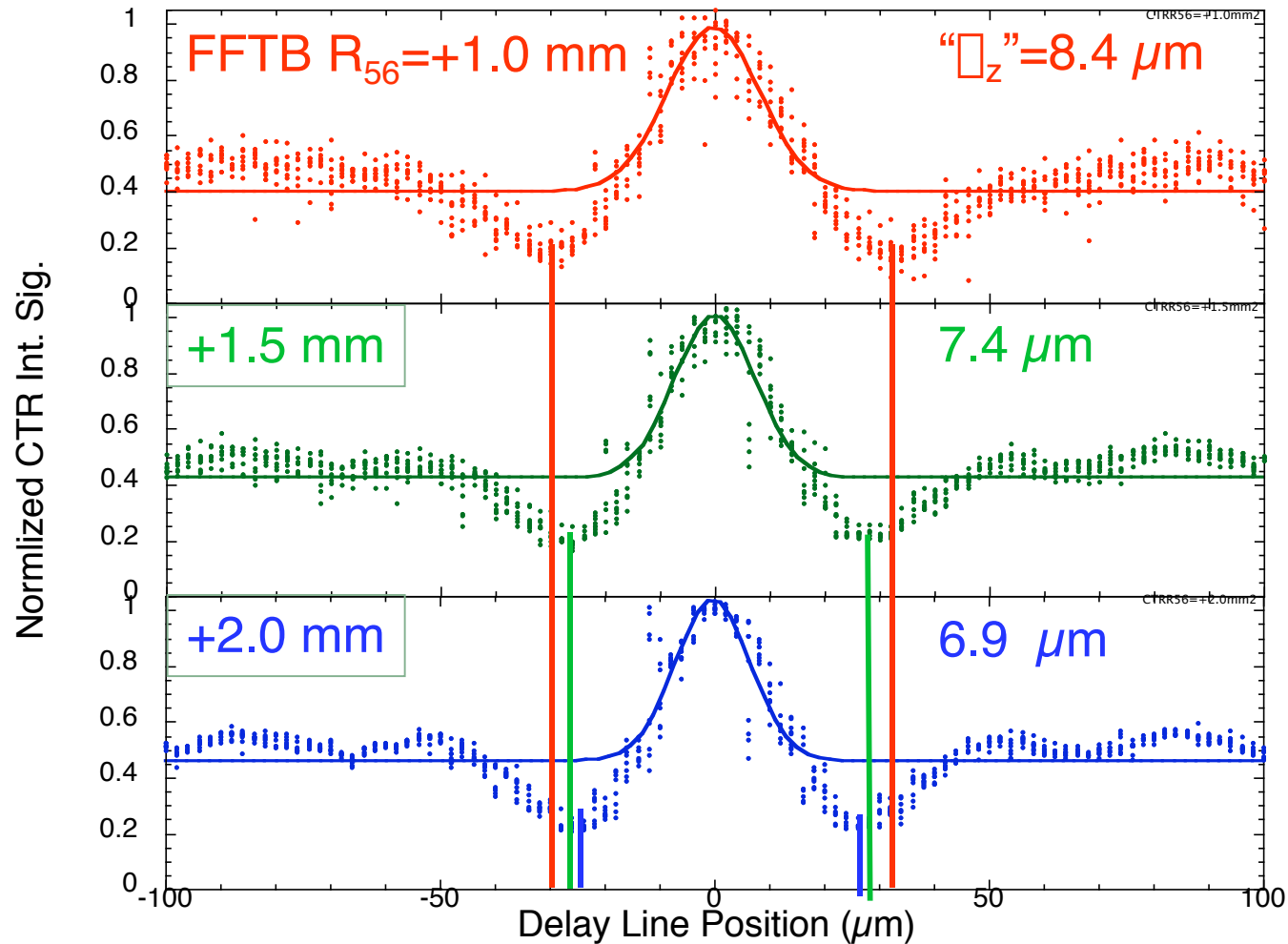
Gaussian Bunch

$\Delta z \approx 18 \mu\text{m}$

or

$\Delta t \approx 120 \text{ fs}$

# FFTB $R_{56}$ DEPENDENCY



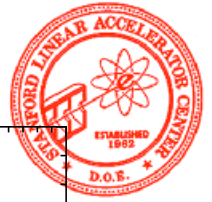
$\sigma_z \approx 17 \mu\text{m}$  or 114 fs  
(corrected)

$\sigma_z \approx 13 \mu\text{m}$  or 86 fs

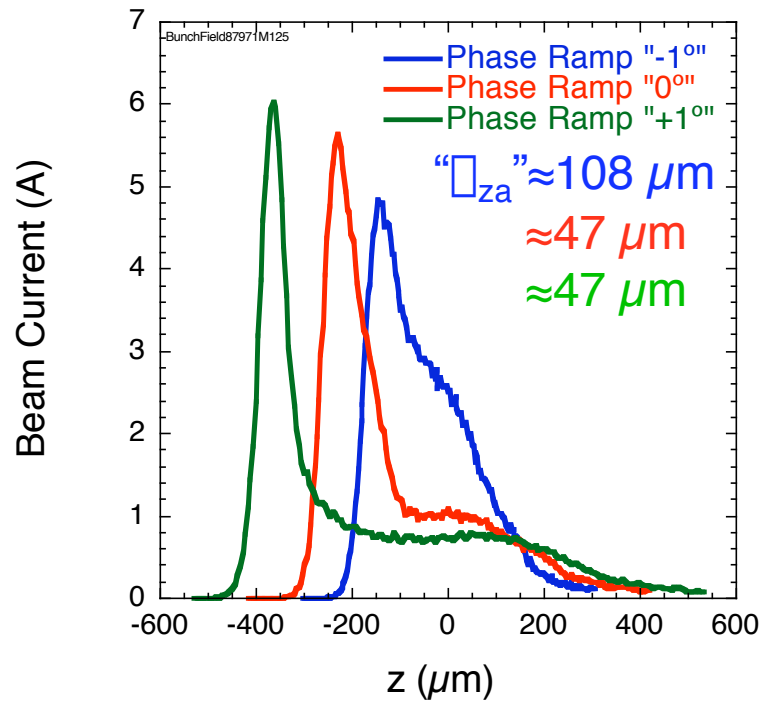
$\sigma_z \approx 11 \mu\text{m}$  or 74 fs

- Measurable, but weak dependency
- Variations masked by beamsplitter transmission characteristics

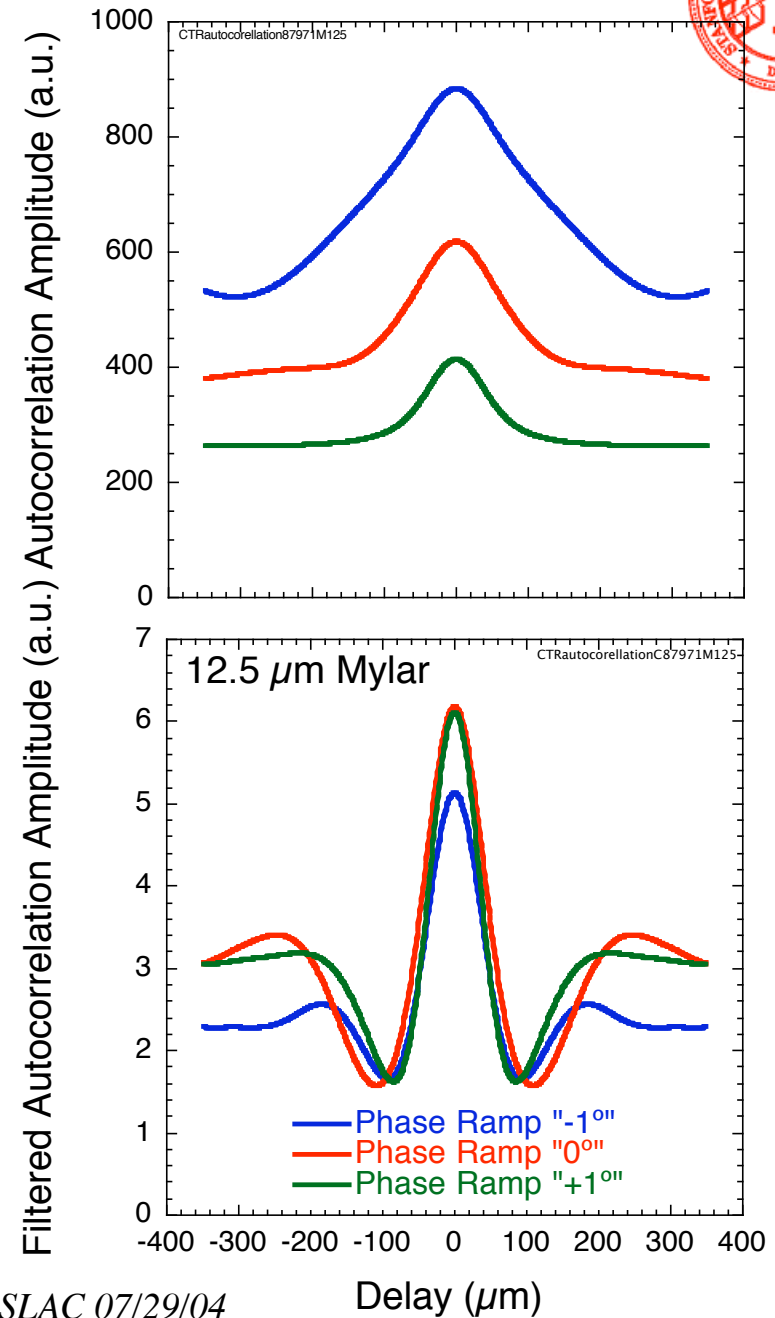
# MYLAR EFFECT (Example)



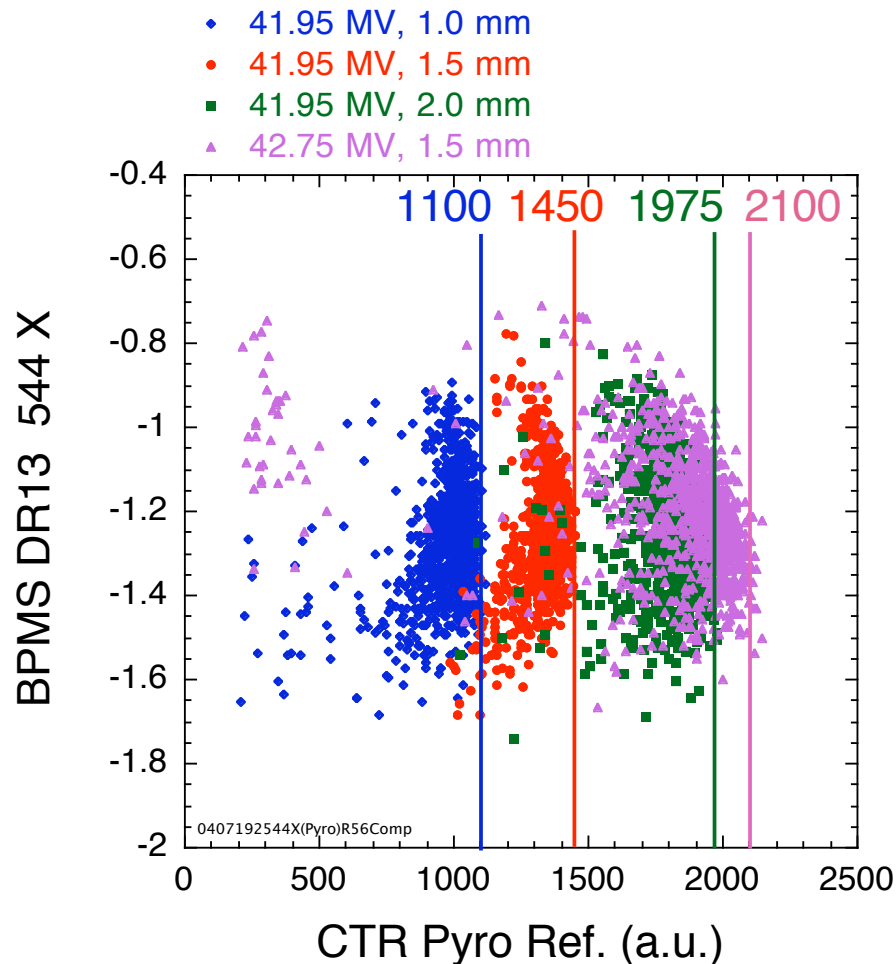
Beam current profiles  
for PWFA



- Beamsplitter "filtering" masks beam profile features



# CTR AMPLITUDE DEPENDENCY @ PEAK COMPRESSION



Gaussian Bunch:

$$E_{\text{CTR}} \approx N^2 / \sigma_z$$

- Amplitude variations are clear(er)
- Amplitude related to bunch current profile

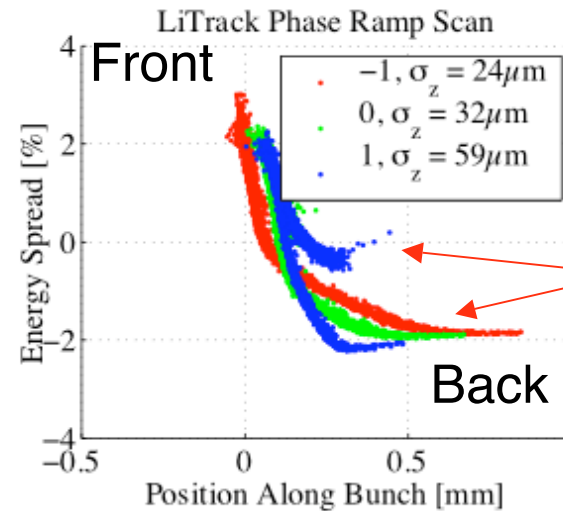
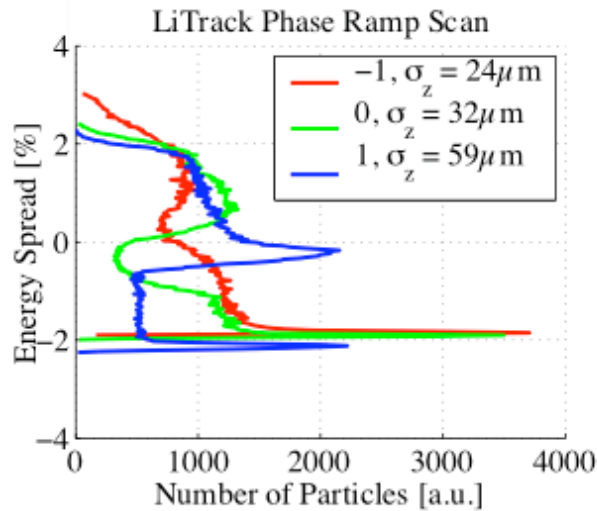
*P. Muggli, XFEL 2004, SLAC 07/29/04*



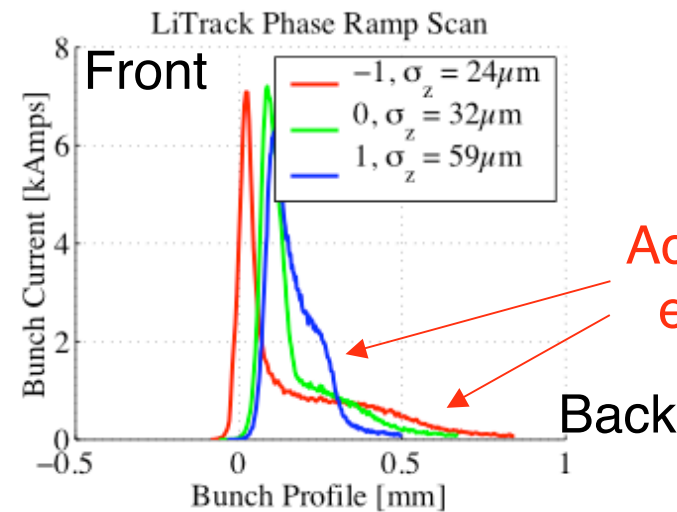
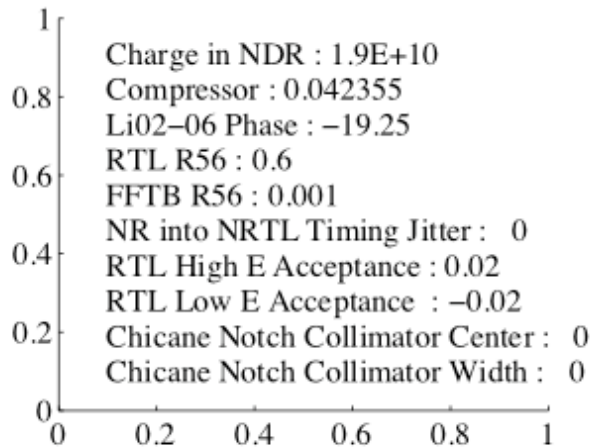
# e<sup>-</sup> BUNCH MANIPULATION



LiTrack  
K. Bane,  
P. Emma



Accelerated electrons



Accelerated electrons

➔ Energy spectrum  $\leftrightarrow$  phase space  $\leftrightarrow$  current profile

➔ " $\sigma_z$ " does not fully describe the bunch shape



SLAC - PUB - 3945

April 1986

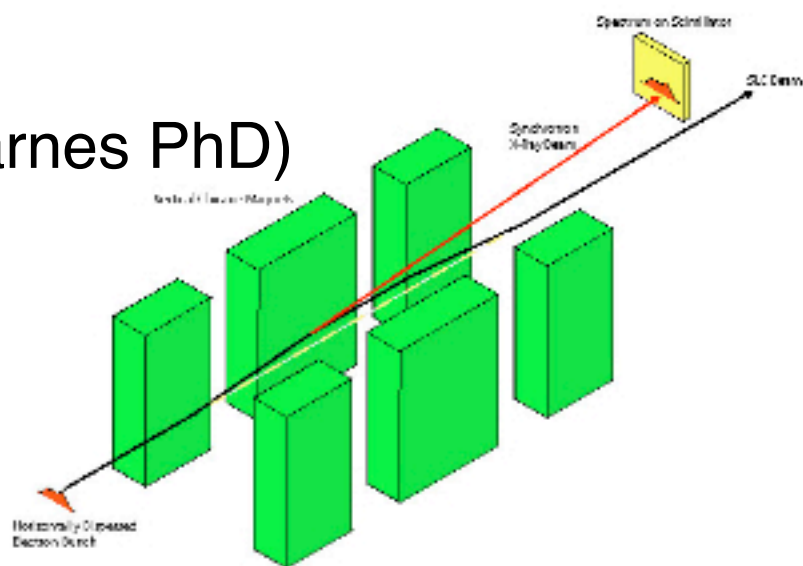
(A)

**SLC ENERGY SPECTRUM MONITOR USING SYNCHROTRON RADIATION\***

J. SEEMAN, W. BRUNK, R. EARLY, M. ROSS, E. TILLMANN and D. WALZ

*Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305*

C. Barnes PhD)



**X-Ray Spectrometer Schematic**

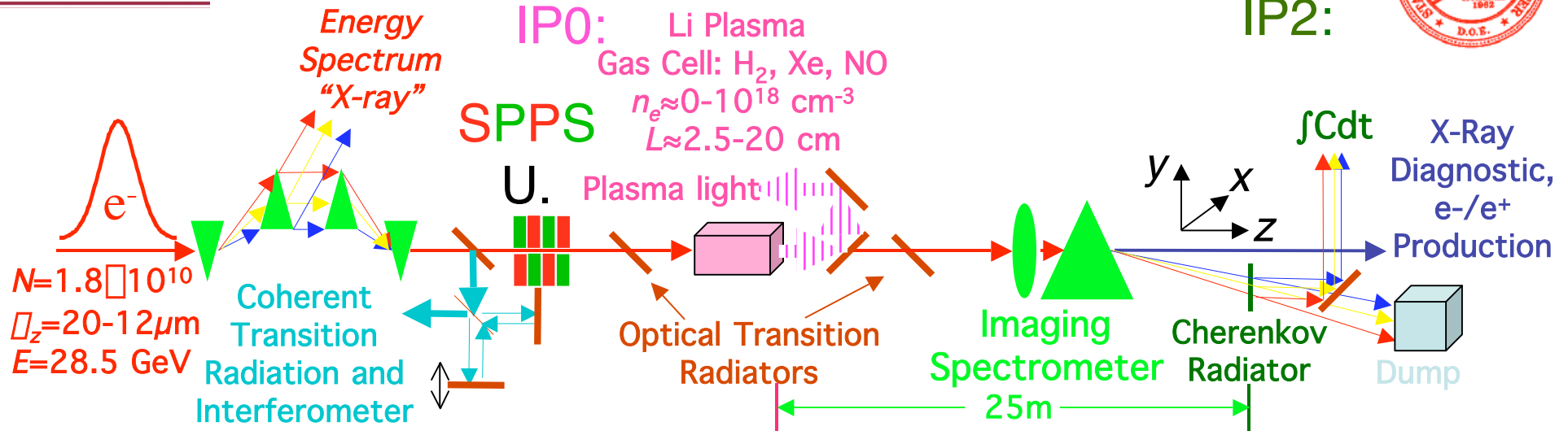


**Spectrometer  
Chicane Magnet**

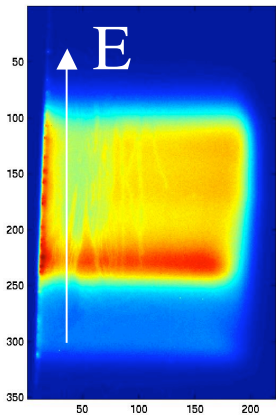


**Scintillato  
Detector**

# EXPERIMENTAL SET UP

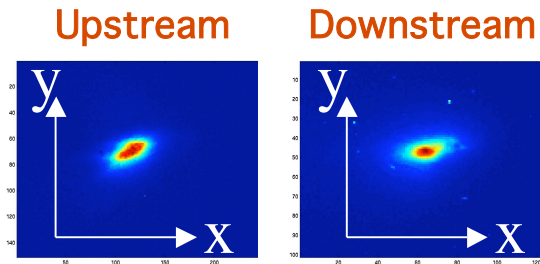


• X-ray Chicane



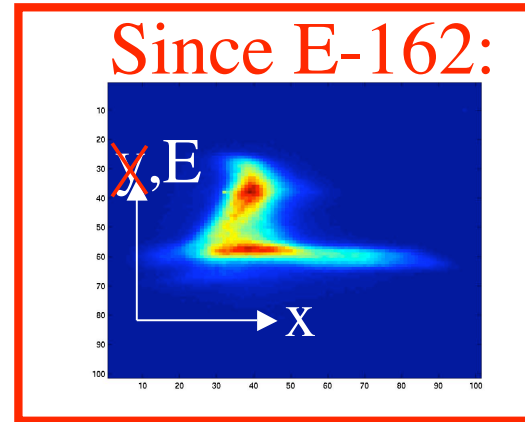
-Energy resolution  $\approx 60$  MeV

• Optical Transition Radiation (OTR)

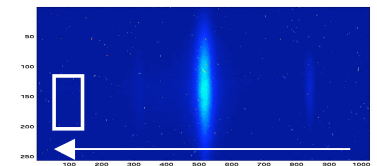


-1:1 imaging, spatial resolution  $\approx 9 \mu\text{m}$

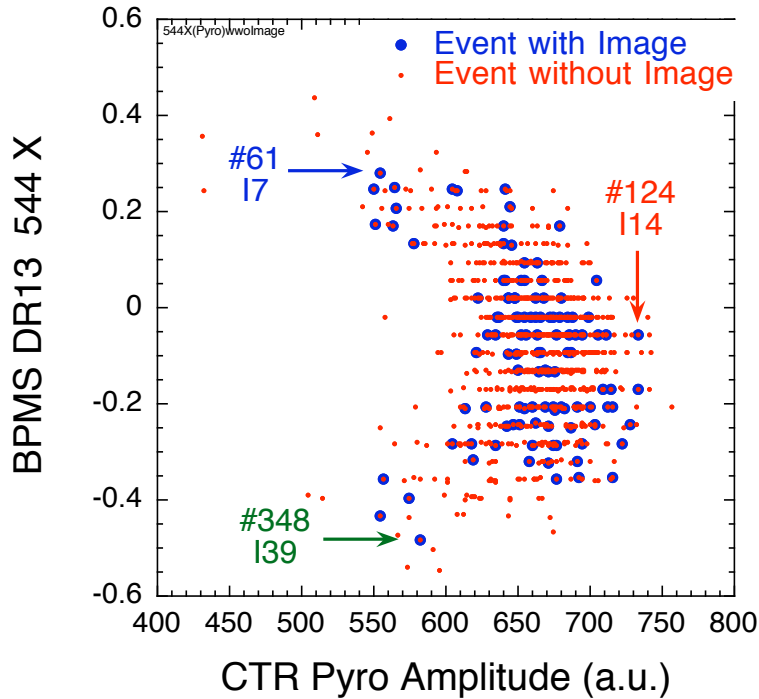
• Cherenkov (aerogel) • Plasma Light



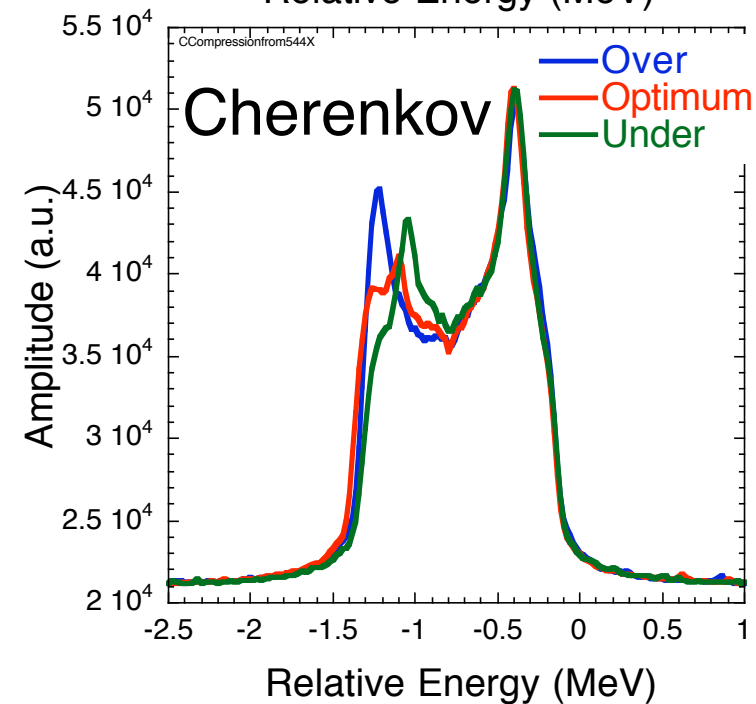
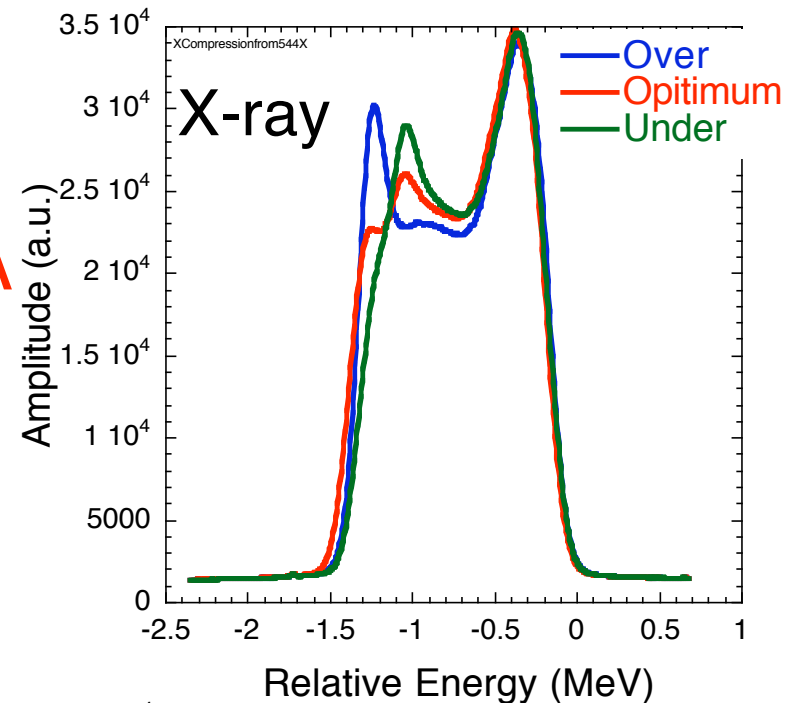
- Spatial resolution  $\approx 100 \mu\text{m}$   
- Energy resolution  $\approx 30$  MeV



# BUNCH COMPRESSION & ENERGY SPECTRA



- Pyro amplitude is ambiguous
- Energy spectra are not
- They are complimentary
- Clear correlation between Energy spectrum and E-164X outcome





# E164X:



# A Plasma Wakefield Acceleration Experiment

C. Barnes, F.-J. Decker, P. Emma, M. J. Hogan, R. Iverson, P. Krejcik, C. O'Connell,  
H. Schlarb, R.H. Siemann, D. Walz

*Stanford Linear Accelerator Center*

C. E. Clayton, C. Huang, C. Joshi, D. Johnson, W. Lu, K. A. Marsh, W. B. Mori

*University of California, Los Angeles*

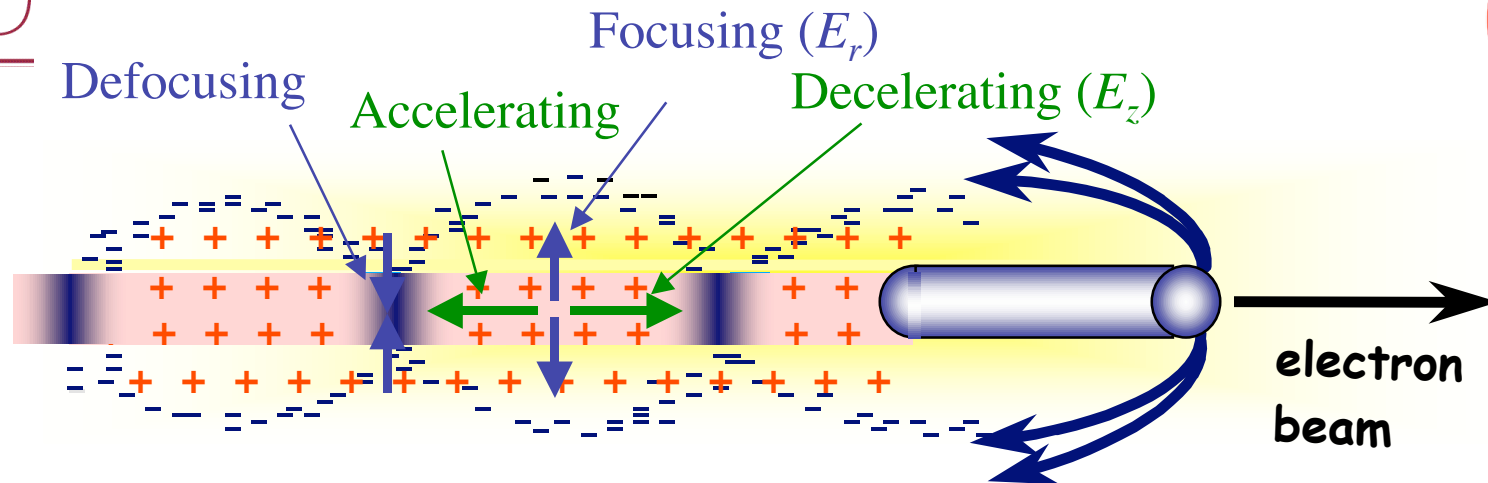
S. Deng, T. Katsouleas, P. Muggli, E. Oz

*University of Southern California, Los Angeles*

*P. Muggli, XFEL 2004, SLAC 07/29/04*



# PLASMA WAKEFIELD ( $e^-$ )



- Plasma wave/wake excited by a relativistic particle bunch
- Plasma  $e^-$  expelled by space charge forces  $\Rightarrow$  energy loss + focusing
- Plasma  $e^-$  rush back on axis  $\Rightarrow$  energy gain

- Linear scaling:  $E_{acc} \approx 110 (MeV/m) \frac{N/2 \times 10^{10}}{(\lambda_z / 0.6mm)^2} \approx 1/\lambda_z^2 @ k_{pe} \lambda_z \approx \sqrt{2}$

- Plasma Wakefield Accelerator (PWFA) = Transformer

**Booster for high energy accelerator**

- At  $n_e = 2.6 \times 10^{17} \text{ cm}^{-3}$ :  $f_{rf} \approx 4.5 \text{ THz}$  accelerator

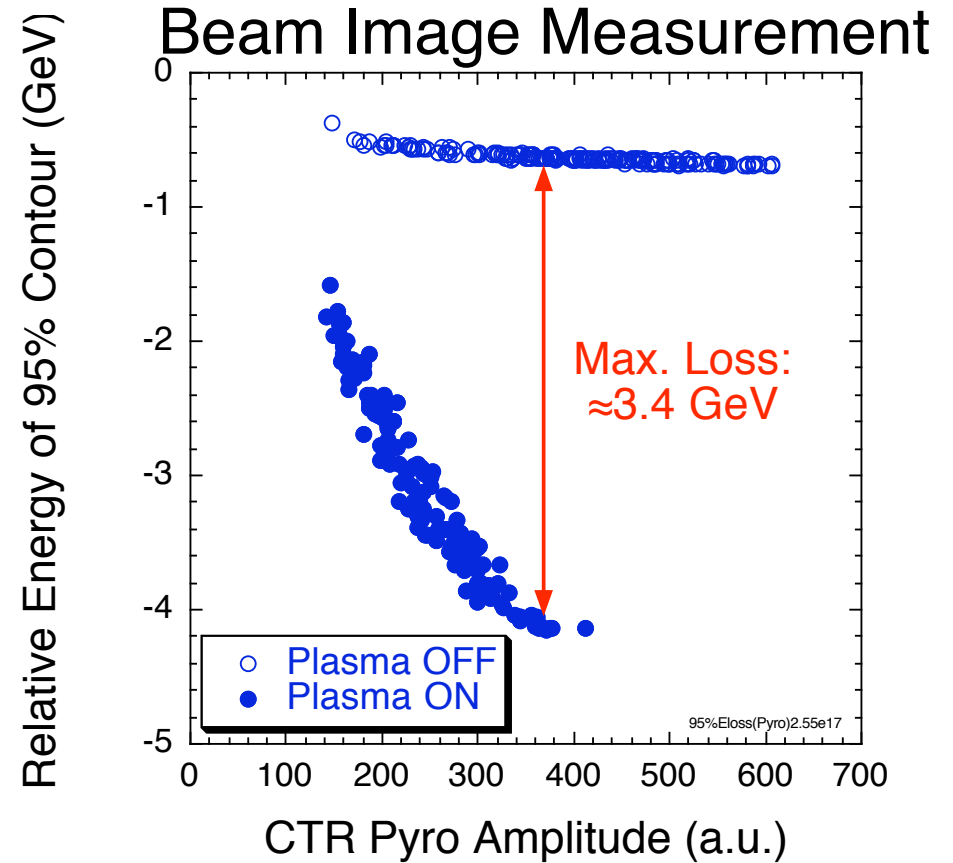
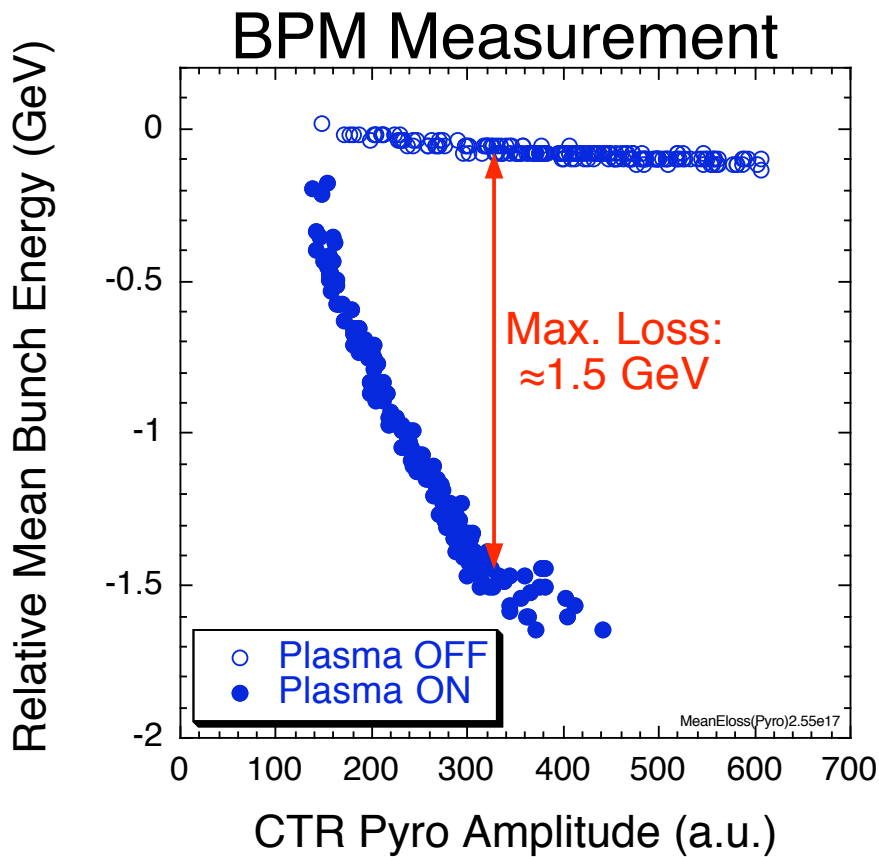
(for  $\lambda_z \approx 20 \mu\text{m}$ )

$E_{acc} \approx 40 \text{ GV/m}$ ,  $B_{\perp}/r \approx 8 \text{ MT/m}$

*P. Muggli, XFEL 2004, SLAC 07/29/04*

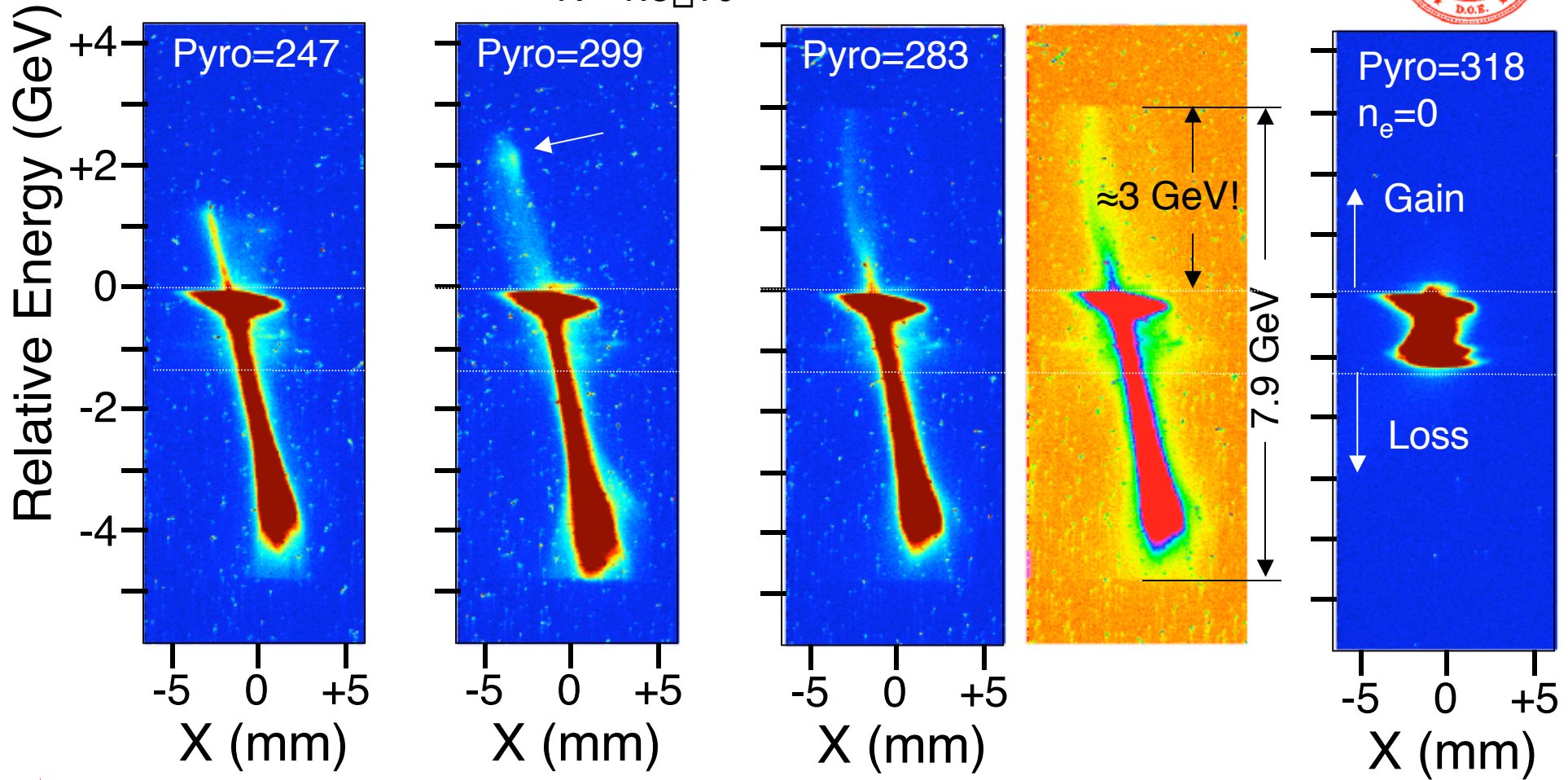


$L \approx 10 \text{ cm}, N \approx 1.8 \times 10^{10}$



➔ Energy loss correlates with CTR energy ( $1/\sigma_z$ ?)

➔ Peak energy gradient 3.4 GeV/10 cm! (or 34 GeV/m!)



- ➔ Energy gain reaches  $\approx 3+1 \text{ GeV}$  or  $\approx 40 \text{ GeV/m}$
- ➔  $\approx 7\%$  of charge or  $\approx 200 \text{ pC}$  with  $E > E_0$
- ➔ Energy gain depends on the details of the incoming beam (x,y,z)



## CONCLUSIONS



- First and only(?) measurement of SLAC short bunches
- CTR interferometry shows bunches as short as 74 fs, but ...
- Beam splitter Fabry-Perot alters the measurement and CTR has limitations: multiple bunches , symmetric
- Short bunch confirmed by ionization of Li, NO, Xe, and H<sub>2</sub>
- Measure single bunch energy spectrum to retrieve profile/current distribution
- CTR interferogram and amplitude, and bunch spectrum are key for E-164X and future E-...
- CTR interferometer can be improved: thinner Mylar splitter, vacuum box, ...
- Retrieve/incorporate bunch current profiles: in CTR and E-164X, work in progress ...